

Jet substructure for everyone

Gregory Soyez

IPhT, CNRS, CEA Saclay

Jets and their substructure from LHC data, May 31-June 4 2021,
CERN (online)

The growing scope of jet substructure

In the early 2000-2010's: Jet substructure was a niche

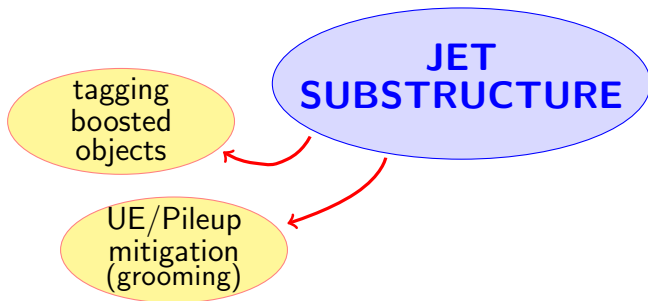
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Over ~ 10 years it has become a standard tool at colliders

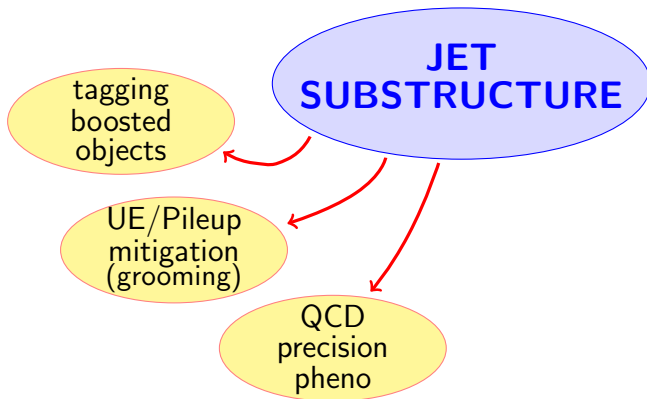


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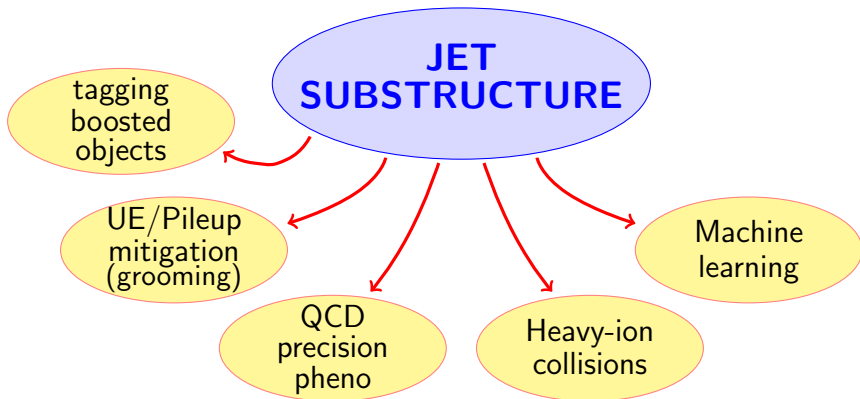


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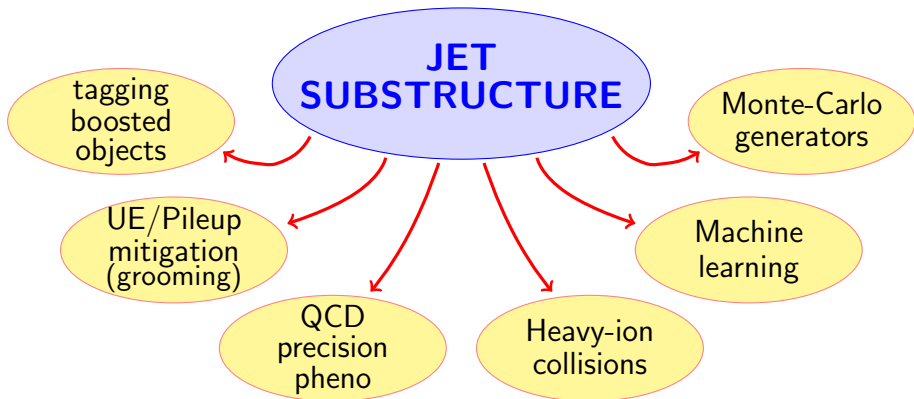


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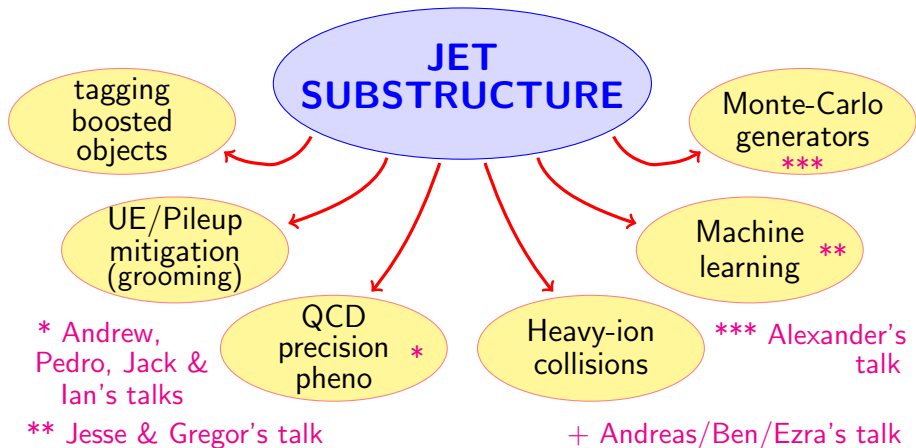


The growing scope of jet substructure

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substructure \equiv internal dynamics of jets

Before getting into applications, a few words about HOW it is done
(excluding ML)

Two main classes of approaches for jet clustering:

- ① Jets as particle branchings \rightarrow pairwise clustering ((anti-) k_t , C/A, ...)
- ② Jets as energy flows \rightarrow cone algorithms (SISCone, MidPoint, ...)

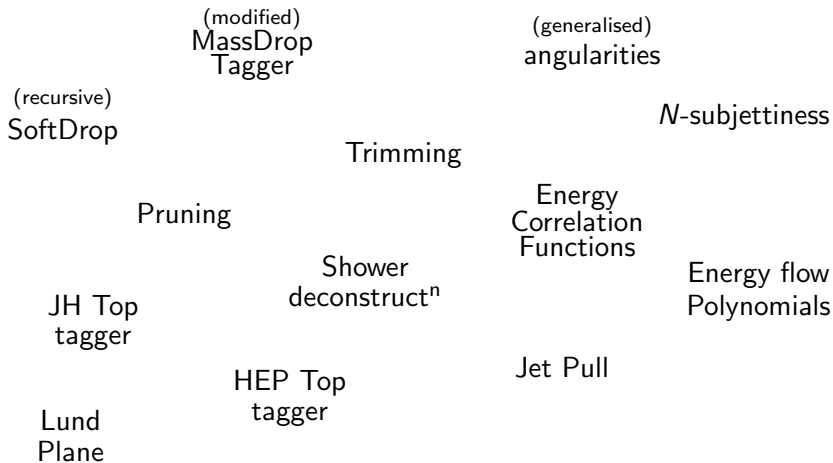
Two main classes of approaches for jet clustering:

- ① Jets as particle branchings \rightarrow pairwise clustering ((anti-) k_t , C/A, ...)
- ② Jets as energy flows \rightarrow cone algorithms (SISCone, MidPoint, ...)

The same broad classes apply to substructure:

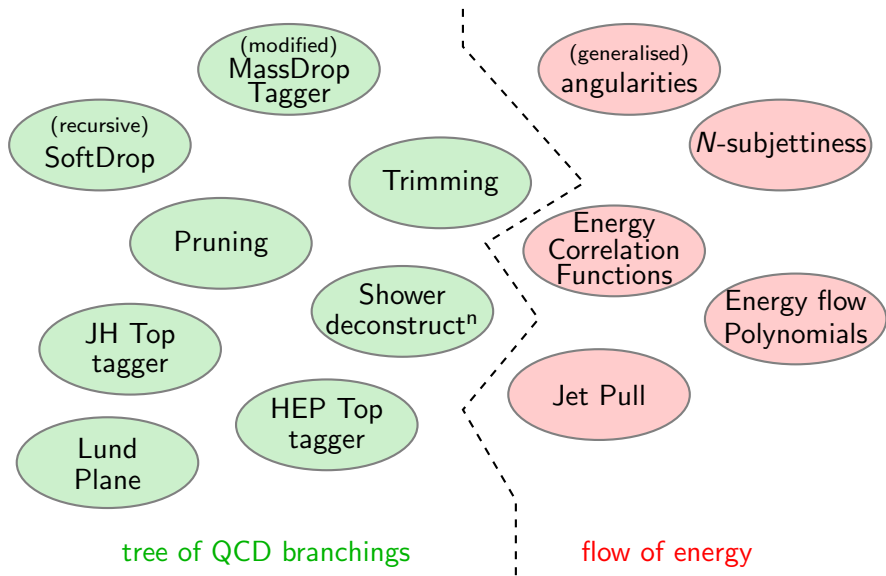
- ① Use particle branchings \rightarrow techniques based on de-clustering the jet
- ② Use energy flows \rightarrow techniques based on (sub)jet shapes

A decade of substructure tools

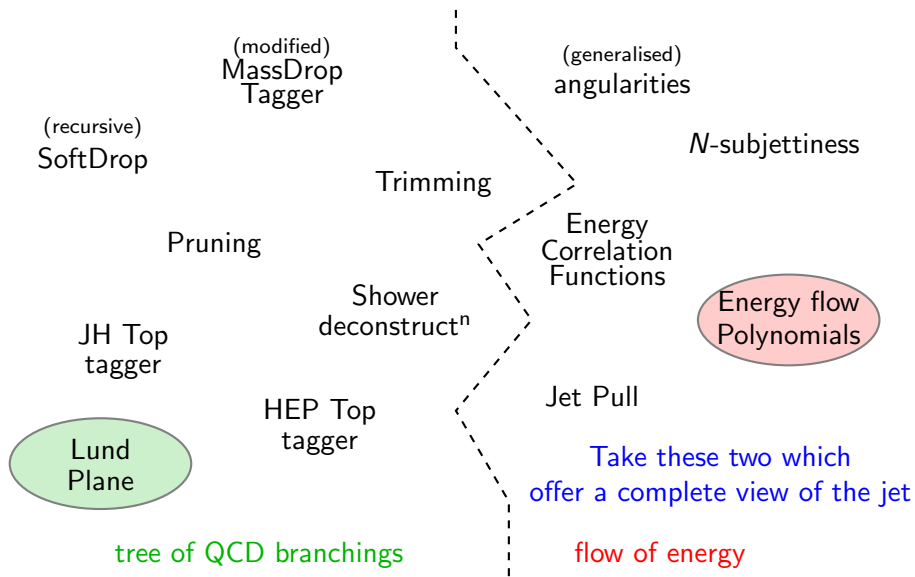


* Non-exhaustive/biased/... list

A decade of substructure tools



A decade of substructure tools



Energy-flow polynomials

$$\text{EFP}_G(\text{jet } j) = \sum_{i_1, \dots, i_N \in j} z_{i_1} \dots z_{i_N} \sum_{(k,l) \in G} \theta_{i_k i_l}$$

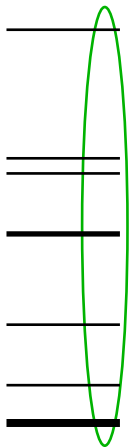
with G a (multi)graph with N vertices and some edges (k, l)

Main properties:

- linear basis for IRC-safe substructure observables
- includes energy-correlation function: $\sum_{i,j} z_i z_j \theta_{ij}^\beta$ (and higher-orders)
widely used for tagging
- Can be used for various ML tagging applications
- Interesting underlying computational structures

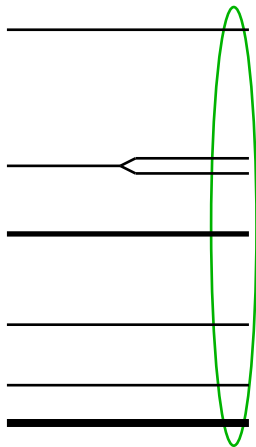
Clustering approach: Cambridge/Aachen

Cambridge/Aachen: iteratively recombine the closest pair



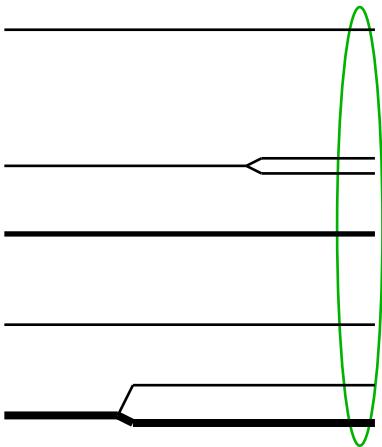
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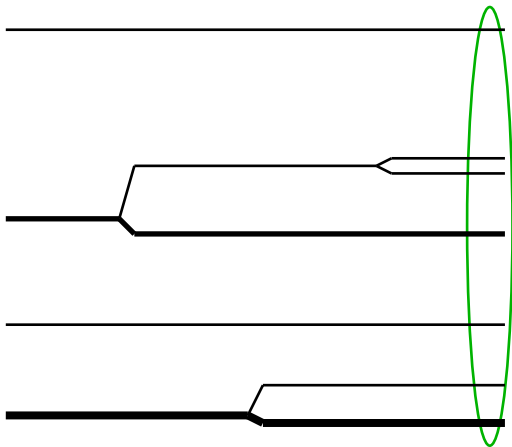
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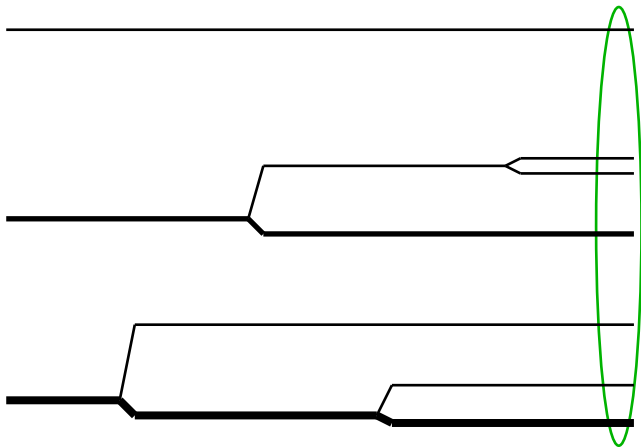
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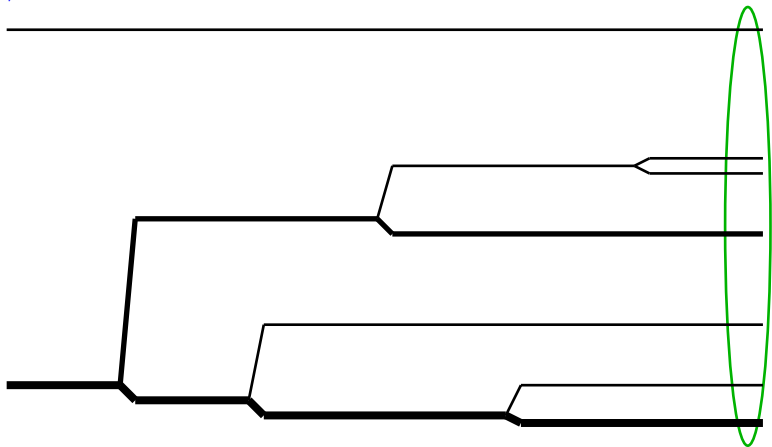
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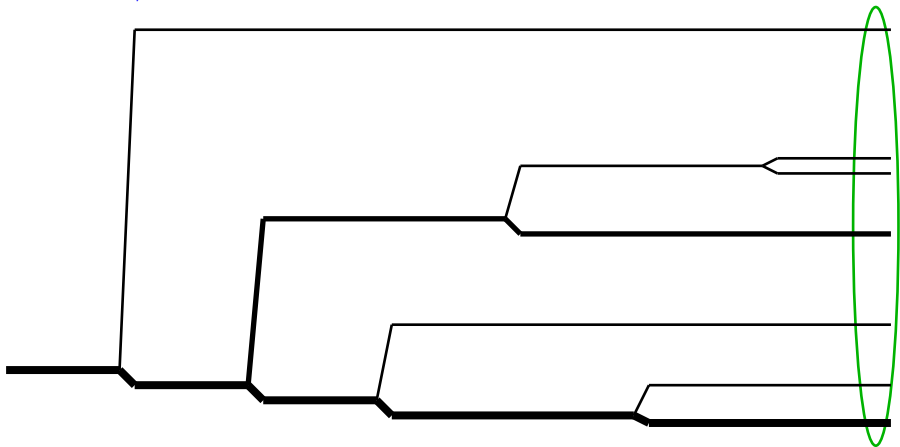
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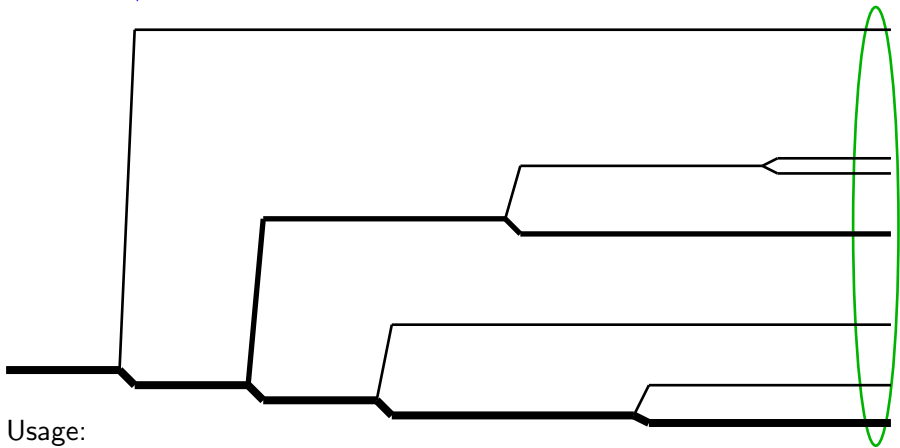
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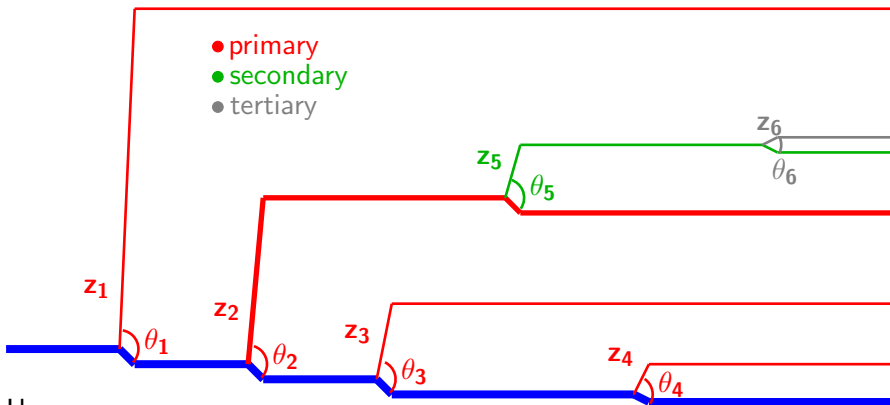


Usage:

- ▶ (iteratively) **undo clusterings** (following hard branch) to find structure (SoftDrop,...)
- ▶ study kinematic properties of the branchings (LundPlane)

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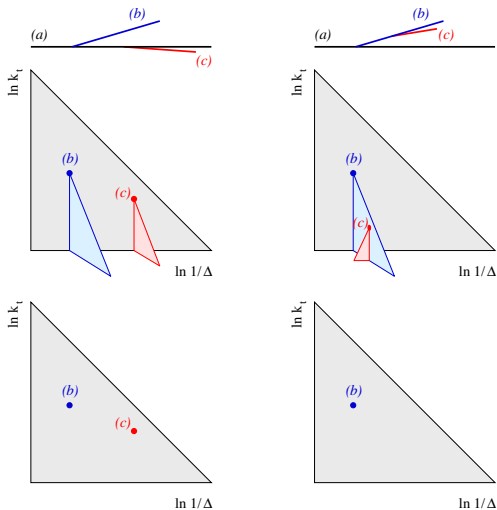
Lund Plane representations

[F.Dreyer,G.P.Salam,GS,1807.04758]

JET

LUND DIAGRAM

PRIMARY LUND PLANE



- ▶ C/A mimics angular ordering
- ▶ structure close to the Lund diagrams used in resummation/MC

Properties at each vertex

$$\mathcal{T}_i = \{\theta_i \equiv \Delta_i, k_{t,i}, z_i, \varphi_i, \dots\}$$

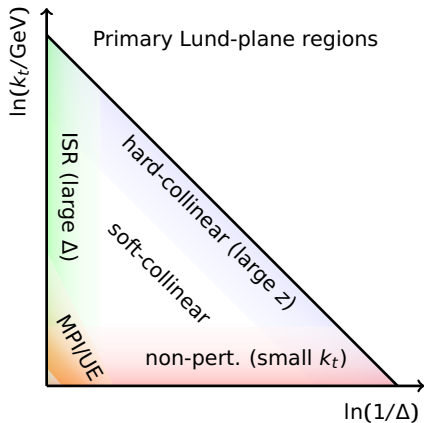
Either primary only:

$$\mathcal{L}_{\text{prim}}(j) = [\mathcal{T}_1, \dots, \mathcal{T}_n]_{\text{primary}}$$

Or full tree

$$\mathcal{L}_{\text{tree}}(j) = [\mathcal{T}_{j \rightarrow j_1, j_2}, \mathcal{L}_{\text{tree}}(j_1), \mathcal{L}_{\text{tree}}(j_2)]$$

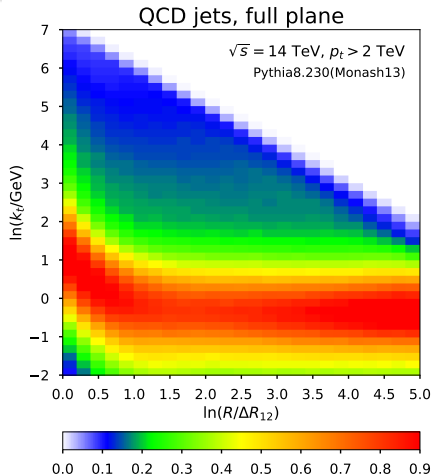
Lund plane physics regions



Different physics contributions in different regions of the (primary) Lund plane

In particular, selecting $k_t \geq k_{t,\text{cut}}$ selects a pQCD region (IRC safety)

Lund plane physics regions



Different physics contributions in different regions of the (primary) Lund plane

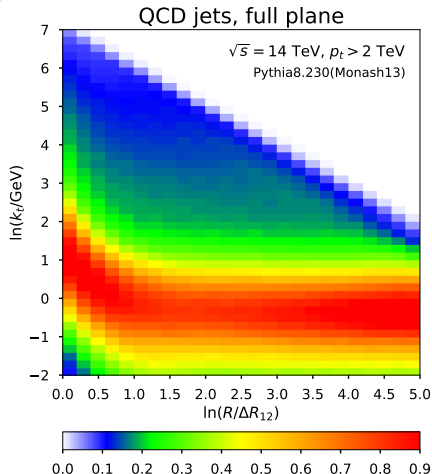
In particular, selecting $k_t \geq k_{t,\text{cut}}$ selects a pQCD region (IRC safety)

Simple observable

Lund plane density:

$$\rho = \frac{1}{N_{\text{jet}}} \frac{d^2 N}{d \ln 1/\Delta d \ln k_t}$$

Lund plane physics regions



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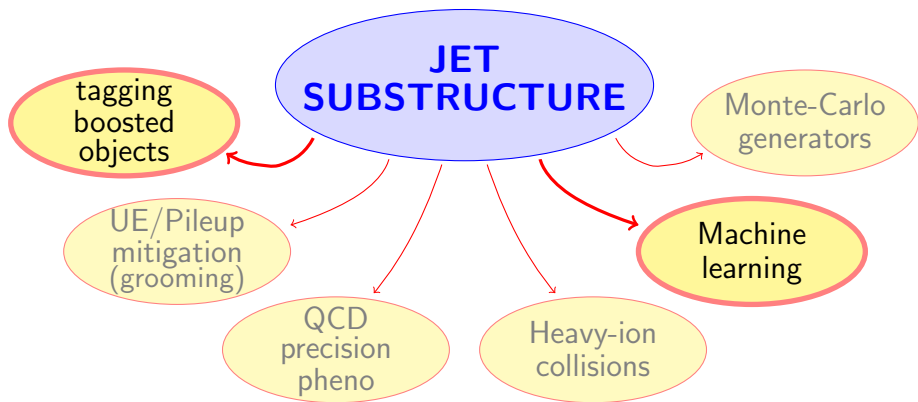
$$\rho = \frac{1}{N_{\text{jet}}} \frac{d^2 N}{d \ln 1/\Delta d \ln k_t}$$

Prospect: trees & E flows are not exclusive: we can define flow/shape observables on tree constructions

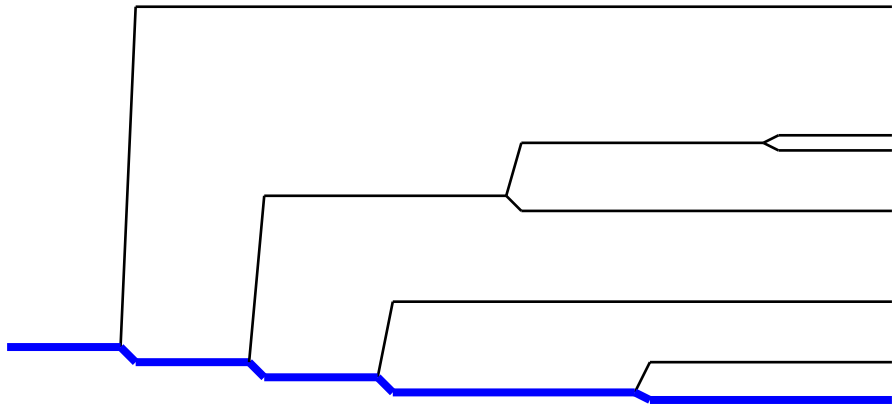
New and exciting progress

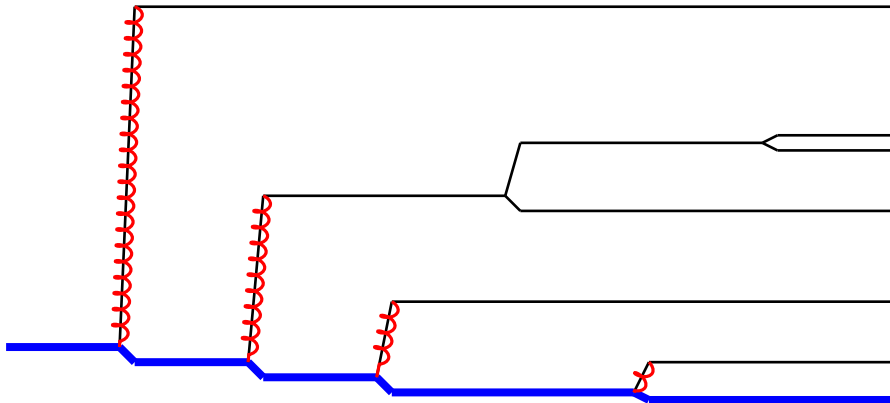
In a nutshell: for a few big applications of substructure I will

- 1 Describe the physical idea (phrasing it in the Lund Plane picture)
- 2 Give (at least one) interesting recent development
- 3 Discuss potential new developments

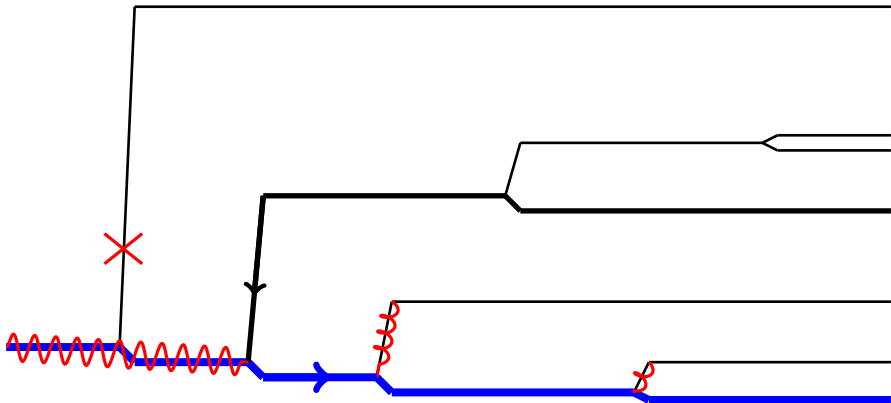


Physics ideas



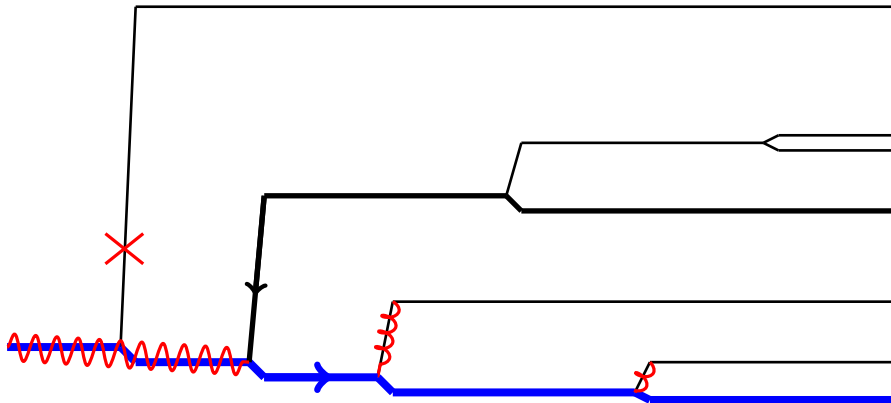


QCD jet: mostly soft gluon emissions



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W jet: hard $W \rightarrow q\bar{q}$ branching + no large-angle emissions



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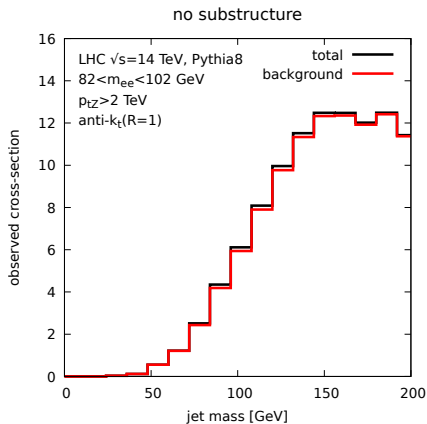
typically tree

typically shape

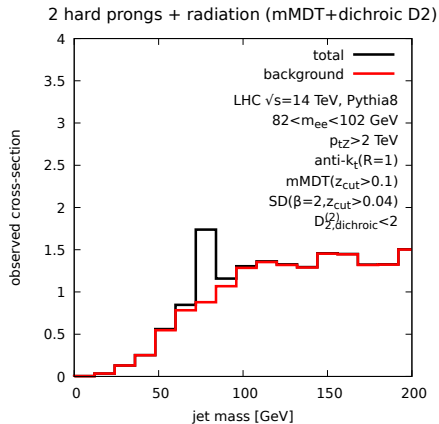
Illustrative example

Tagging a boosted W boson (using $Z(\rightarrow \mu\mu) + W(\text{jet})$ vs. $Z(\rightarrow \mu\mu) + \text{jet}$)

no substructure

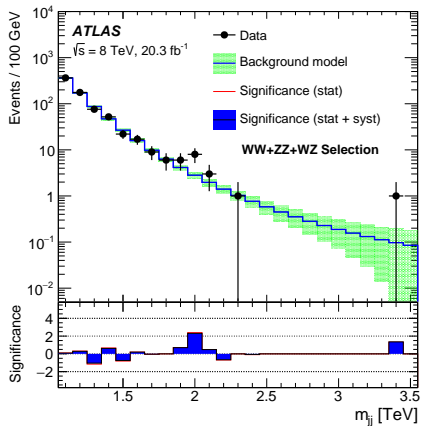


with substructure



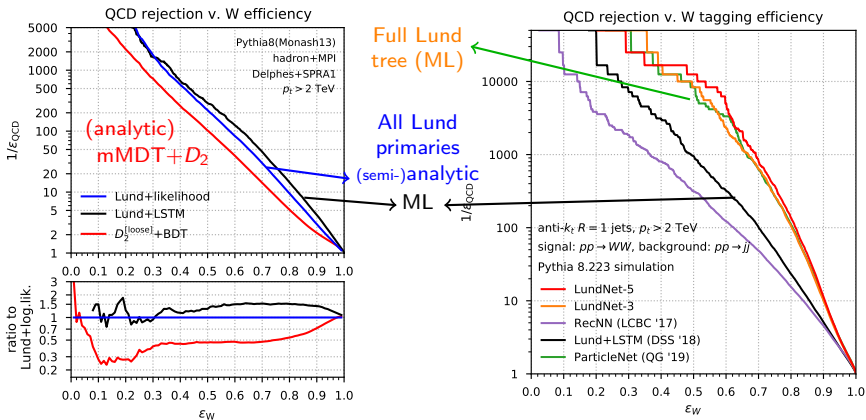
mMDT: 1307.0007; D_2 : 1305.0007; dichroic: 1612.03917

Searches and measurements

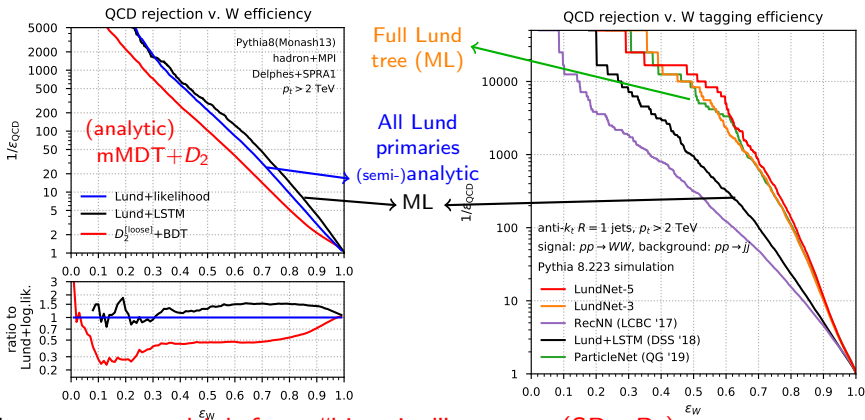


(now-gone) di-boson “excess” (end of Run-I)

Maximise background rejection for given signal efficiency



Maximise background rejection for given signal efficiency

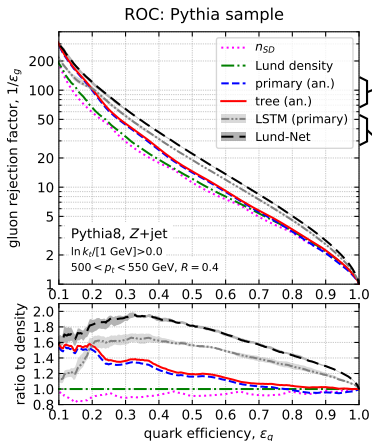


Messages: - good job from “historical” taggers ($SD+D_2$)

- Including all (primary) declusterings help [F.Dreyer,G.Salam,GS,1807.04758]
- ML can extract some additional information (\sim ParticleNet w smaller cost [Gregor's])
- clear gain including the full tree [F.Dreyer,H.Qu,2012.08526]

analytic pQCD and ML for q/g discrimination

[F.Dreyer,GS,A.Takacs,soon]



Use Lund declusterings
(primary or full tree)

Either compute analytically: (*)

$$\mathbb{L} = \frac{p(q|\mathcal{L})}{p(g|\mathcal{L})}$$

Or use as ML input

Main messages:

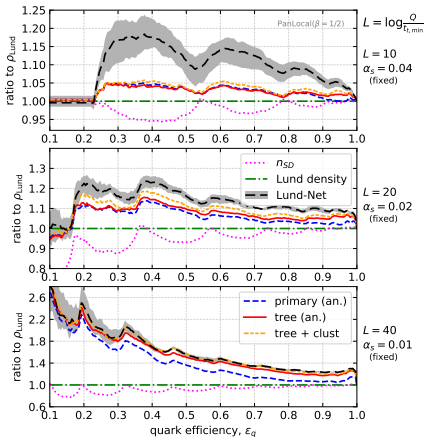
- ✓ Nice analytic performance
- ✓ Better gain for ML

(*) \sim NLL generalisation of n_{SD}

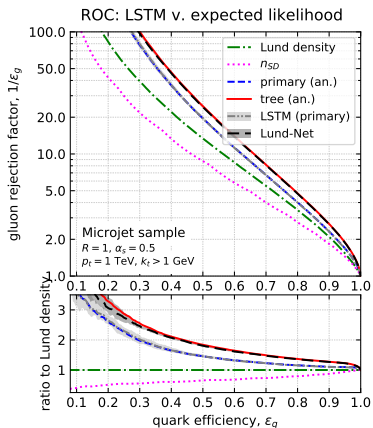
Analytic pQCD and ML for q/g discrimination

If we increase the Boost (fixing $\alpha_s \log(p_t/k_{t,\min})$) the gap between analytic and ML closes

- Great validation
- Question: extra information used by ML?
- Question: MC accuracy? is that extra information well-described in MC?



Fun with taggers: validate ML with QCD

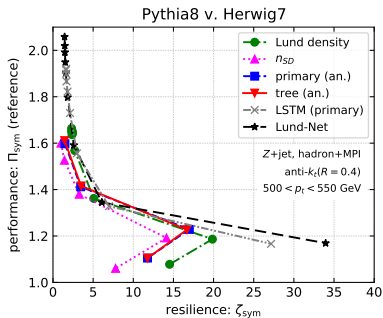
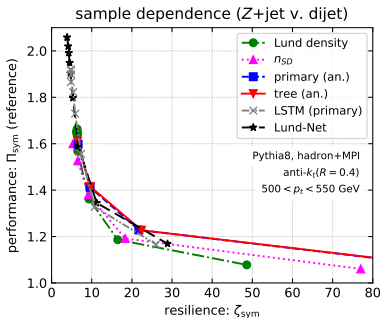


Use a sample with exact LL angular ordering (*) and compare analytics to ML

Shows very good agreement

(*) [F.Dreyer,M.Dasgupta,G.Salam,GS,1411.5182]

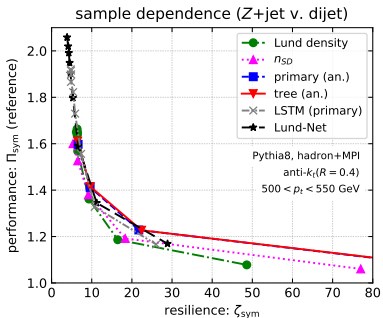
Performance v. resilience



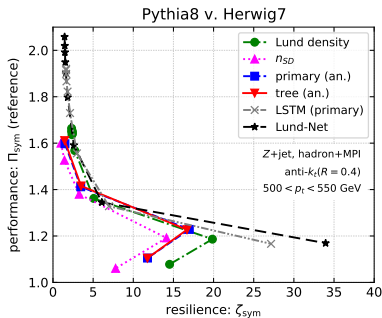
Performance v. resilience

Less sensitive to process (better)

Less sensitive to MC choice (better)



Better discrimination



- Generic trade-off between discriminating power and resilience
- ML gain mostly at small k_t where modelling more important
- some ML gain at larger k_t . Accessible in pQCD?

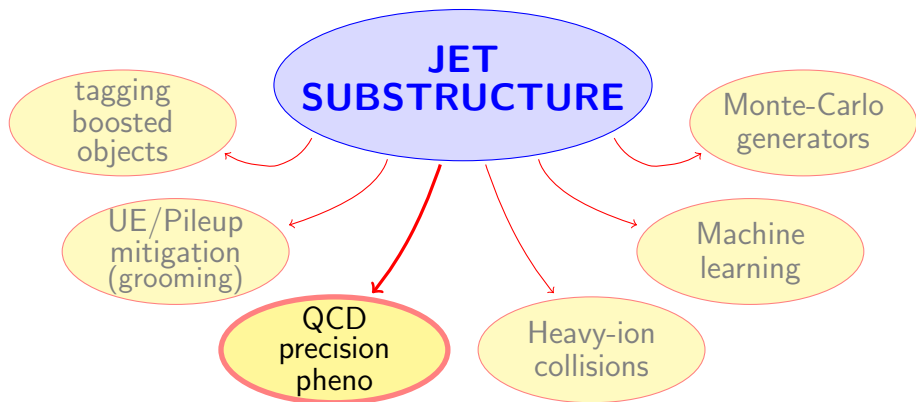
What to look for in the future

Tagging progress is (mostly) ML-oriented today

There are nonetheless some interesting directions where “QCD” can help

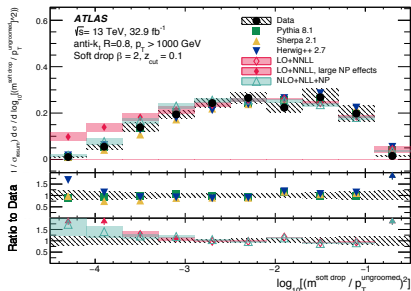
- Improved inputs/architecture
Better control, faster convergence,...
- QCD analytics can be used as a validation of ML in known limits
- Trade-off between performance and “resilience”
- Room for “simple” QCD-based taggers (like the above Lund-plane, or arXiv:2006.10480)

More in Gregor&Jesse'talks (ML) and in Jack's talk (analytics)



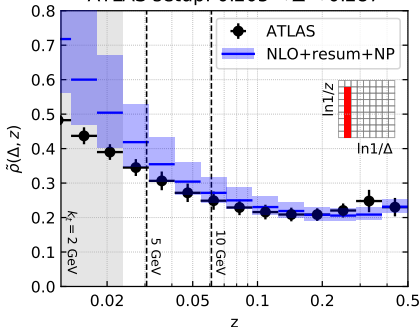
- **What:** compute substructure observables in pQCD
- **Why:** gain understanding on tools, compare to data, ...
- **How:** substructure often probes physics at scales \ll jet p_t
→ **need for resummation**
 - from “standard” QCD and SCET
 - State-of-the-art: NLL (or NNLL) matched to NLO
 - intimate link with Parton Showers (more on this later)
- **A nice benefit:** “groom” soft & large-angle radiation
 - makes **calculations somewhat easier** (mostly collinear physics)
 - **reduced non-perturbative effects**, pushed them to lower scales

SoftDrop jet mass



Lund-plane density

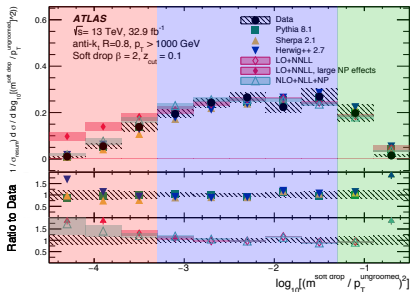
ATLAS setup: $0.205 < \Delta < 0.287$



- Regions dominated by either NP, resummation or fixed-order
- Unique framework for new probes of QCD over several scales
- Question: does substructure help for α_s or PDF extraction?
- See e.g. [1711.08341](#), [1603.09338](#), [1704.02210](#), [1712.05105](#), [1807.05974](#), [2104.06920](#), [CMS-PAS-SMP-20-010](#)

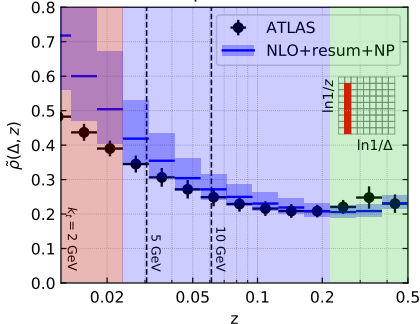
More in Andrew, Ian and Jack's talks

SoftDrop jet mass



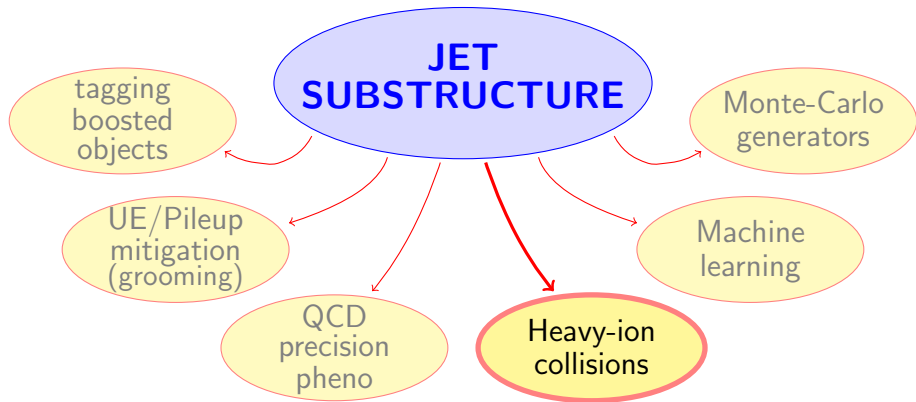
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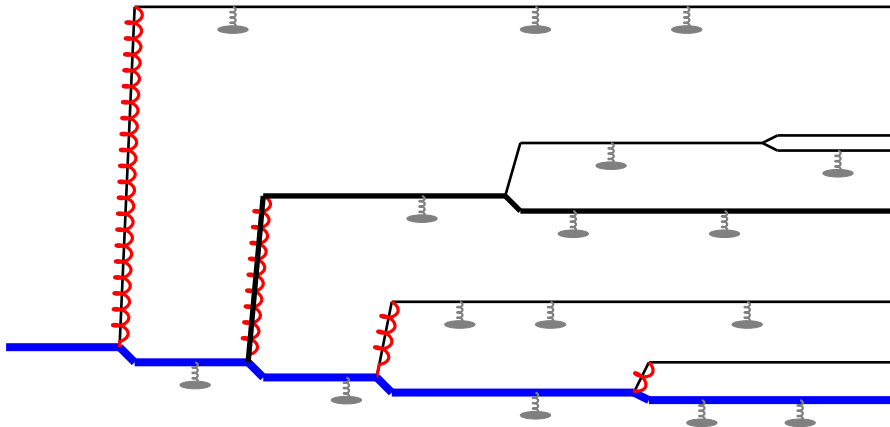


- Regions dominated by either **NP**, **resummation** or **fixed-order**
- Unique framework for new probes of QCD over several scales
- Question: does substructure help for α_s or PDF extraction?
- **Prospect: study more complicated/differential quantities**

More in Andrew, Ian and Jack's talks



Idea: interaction with the quark-gluon plasma

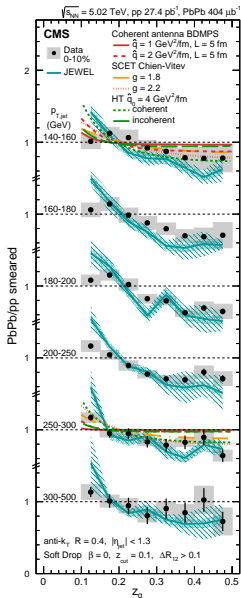


QGP affects the jet dynamics \Rightarrow probe with substructure

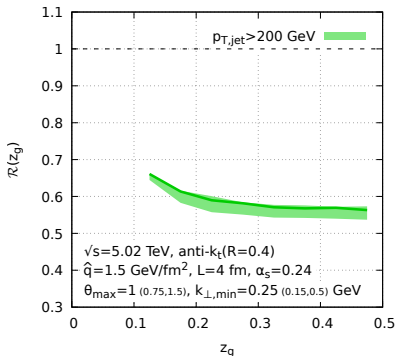
Measuring the splitting function

CMS (CMS-HIN-16-006)

[P.Caucal,E.Iancu,GS,1801.09703,1907.0486617]



$N_{\text{jets-norm}}$ z_g distribution: $p_{T,\text{jet}}$ dependence

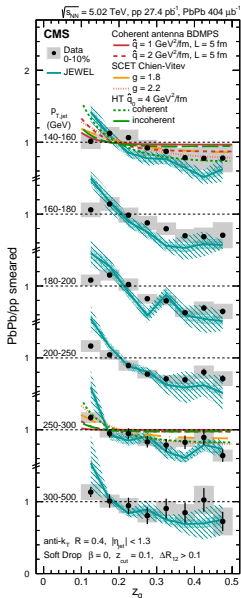


Based on perturbative QCD
 At LL: factorisation between
 “vacuum” (standard) shower and
 medium effects.

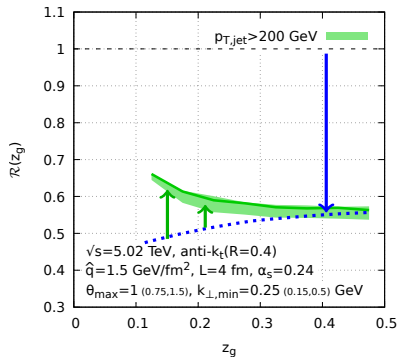
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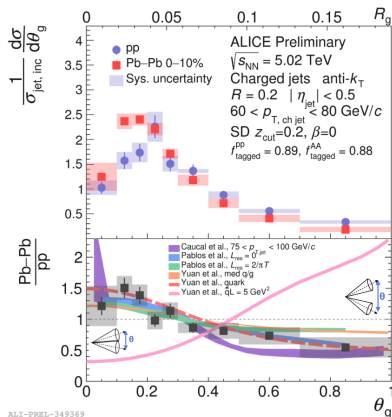
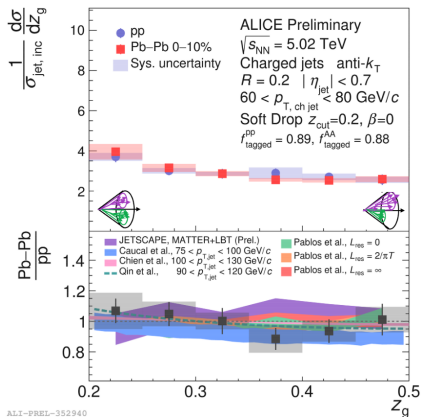


N_{jets}-norm z_g distribution: p_{T,jet} dependence



- Reduction from E loss
- Peak from extra emissions

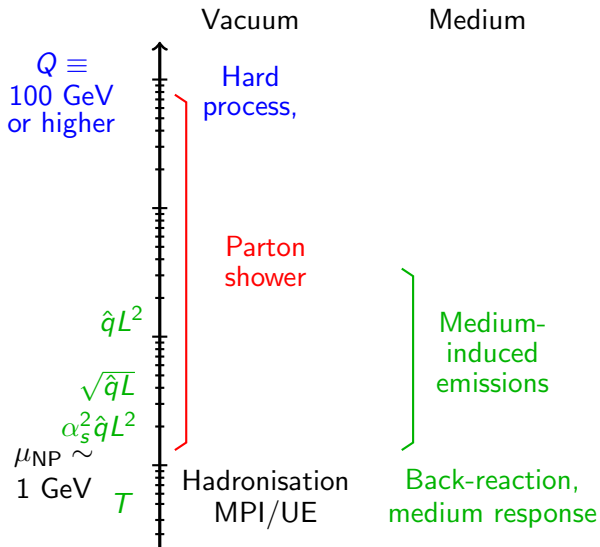
Recent measurement by the Alice collaboration



- Increasing number of substructure measurements at the LHC
- Comparisons to QCD calculations and MC simulations

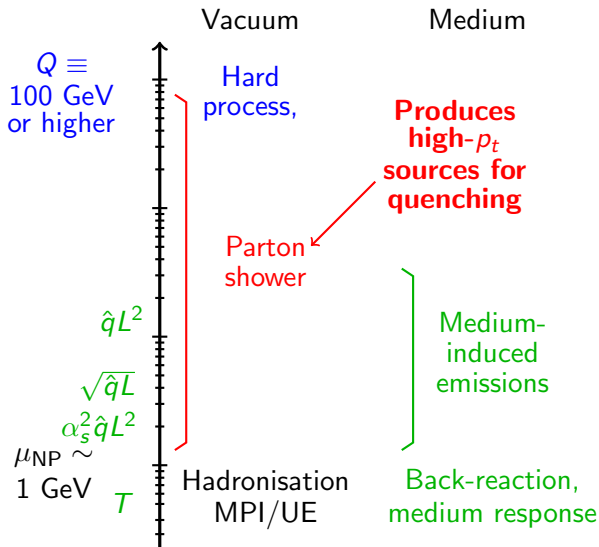
see also Pedro's talk

One aspect (I think) is key for the future



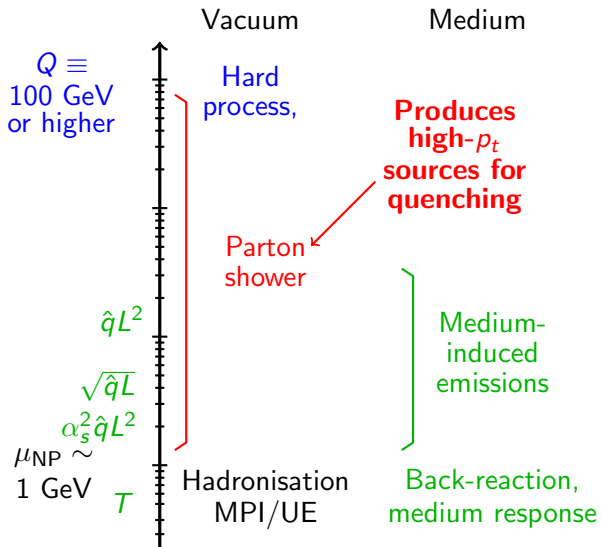
- The QGP brings new physics scales

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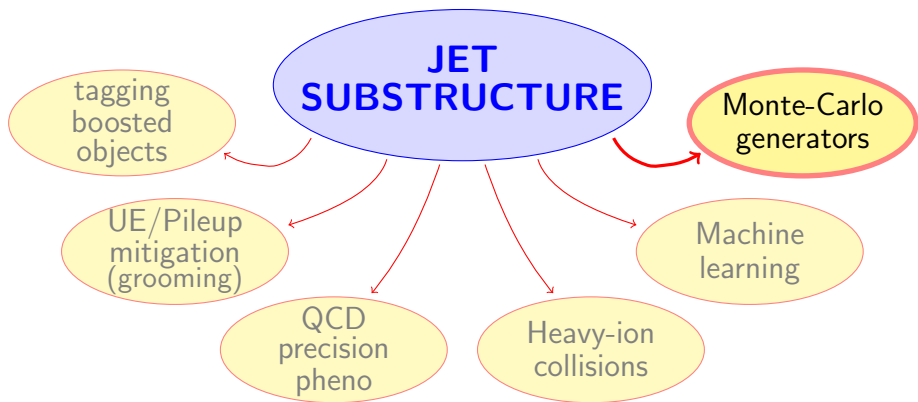


- The QGP brings new physics scales
 - Large k_t dominated by vacuum physics
 - Use substructure to “select” the structure of the jet propagating through the medium
- ↓
- fine-grained/differential study of the QGP.

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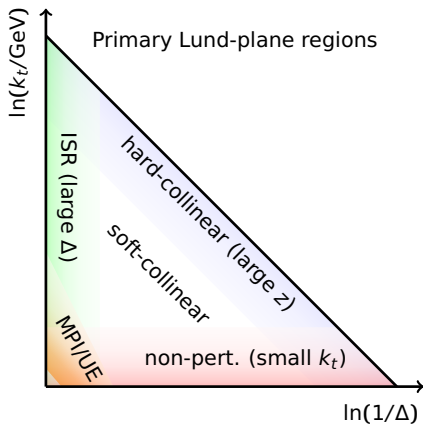


- The QGP brings new physics scales
- Large k_t dominated by vacuum physics
- Use substructure to “select” the structure of the jet propagating through the medium
↓
fine-grained/differential study of the QGP.
- Exp challenge: requires high- p_t



Substructure for MC development

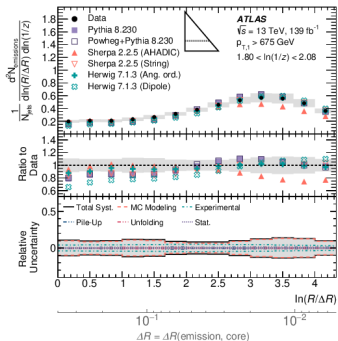
Main idea: substructure observables probe QCD dynamics



Substructure for MC development

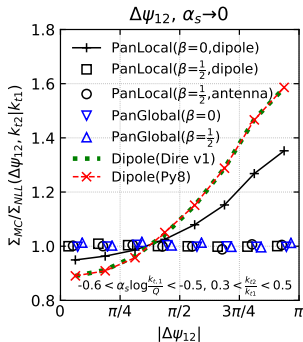
Main idea: substructure observables probe QCD dynamics

direct comparison
between data and MC



[ATLAS,2004.03540]

observables for
accuracy tests/developments

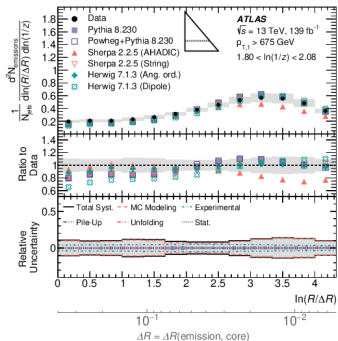


[M.Dasgupta,F.Dreyer,K.Hamilton,
P.Monni,G.Salam,GS,2002.11114]

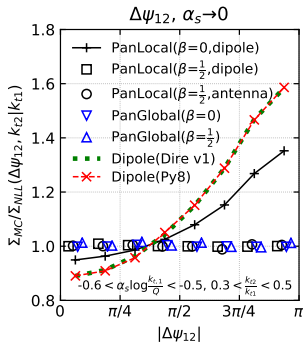
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observables for
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Better constraints \Rightarrow less modelling uncert. \Rightarrow improved searches

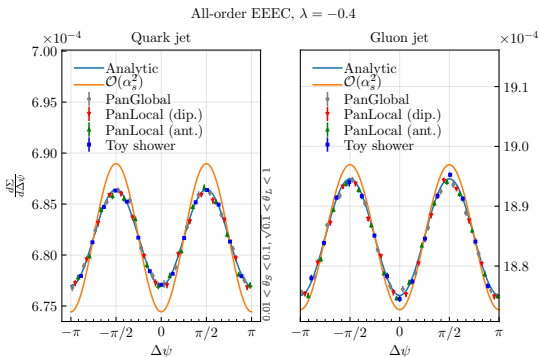
Versatile tool for future developments

Tweak the tool to
match your needs

Connection with
precision calculation

Example: Energy³
Correlation functions
sensitive to spin
correlations at NLL

See Ian's talk



[A.Karlberg,G.Salam,L.Scyboz,
R.Verheyen,2103.16526]

Take-home messages

- **Substructure is now mainstream and is here to stay**
- **Wide range of applications (Taggers, pQCD, HI, MC, ML)**
- **Active exploration ground/laboratory for QCD, exploiting the large phase-space offered by the LHC**

Looking towards the future

- Expect more analyses with boosted jets
- Recent (and on-going) deep-learning revolution
- Need more calculations & (unfolded) substructure measurements
- Lots to do in substructure-based QGP studies
- **Almost endless possibilities to test ideas/MCs/...**

(Online) BOOST2021: <https://indico.cern.ch/event/1037559/>