

Jet substructure: what else?

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Harvard University, April 2nd 2019

- Brief introduction to “jets”
- Schematic overview of jet substructure
- **Interlude: A helpful representation of emissions in QCD**
- Substructure ramifications into:
 - ✓ Searches for new physics
 - ✓ Conceptual understandings of QCD
 - ✓ Precision measurements
 - ✓ Heavy-ion collisions
 - ✓ Machine learning

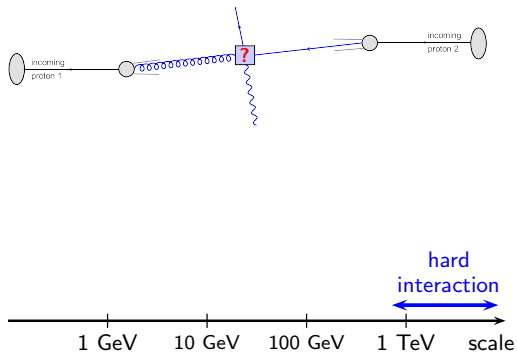
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Disclaimer: although this reviews many aspects of the field,
it remains biased towards my own work

See S.Marzani, GS, M.Spannowski, “looking inside jets: an introduction to jet substructure and boosted objects phenomenology”.]

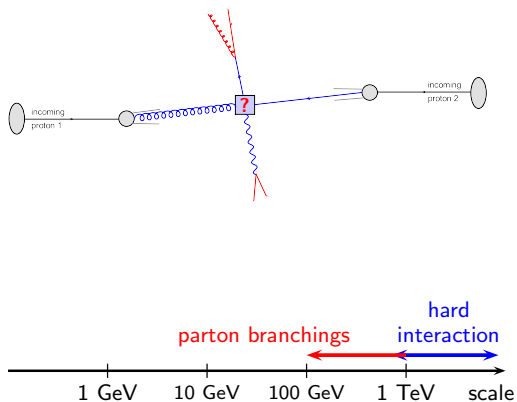
Anatomy of a high-energy collision

Colliders study fundamental interactions at high energy



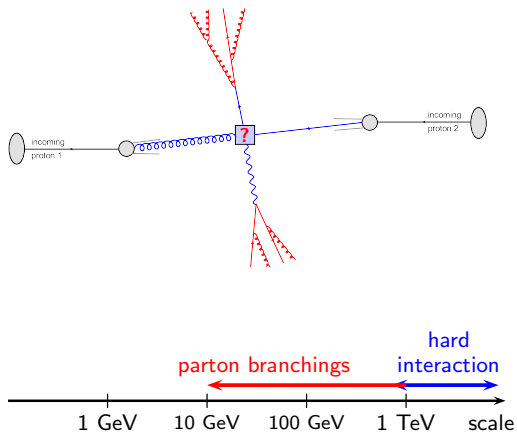
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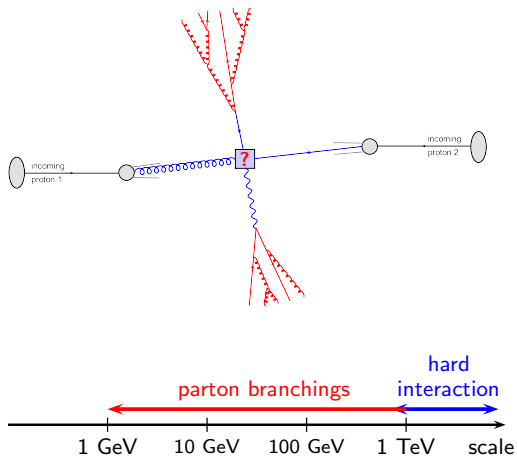
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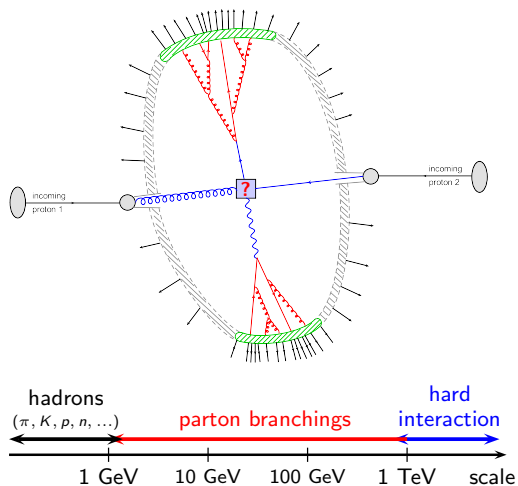
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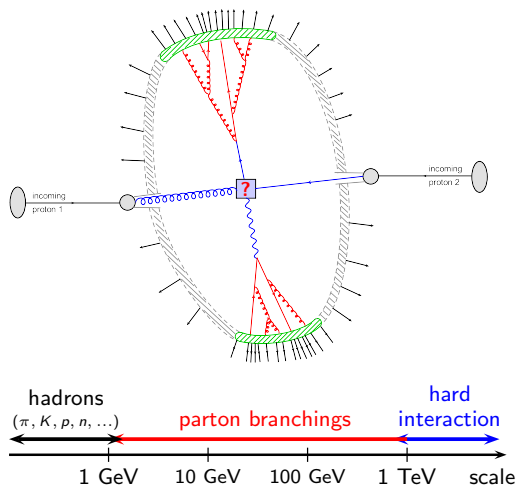
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Anatomy of a high-energy collision

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Hard + branchings

- perturbative QCD
- controlled, solid
- predictive with genuine theory uncertainties

Hadronisation

- NON-perturbative
- needs modelling
- model-dependent

Basic concepts

- “high-energy parton” \rightarrow collimated shower of particles \equiv a **JET**
- **Jets are proxies to hard partons produced in collisions**

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Practically

- obtained by running a clustering algorithm
- the LHC uses the anti- k_t algorithm [M.Cacciari, G.Salam, GS, 08]
- FastJet covers all your numerical needs for clustering [www.fastjet.fr]

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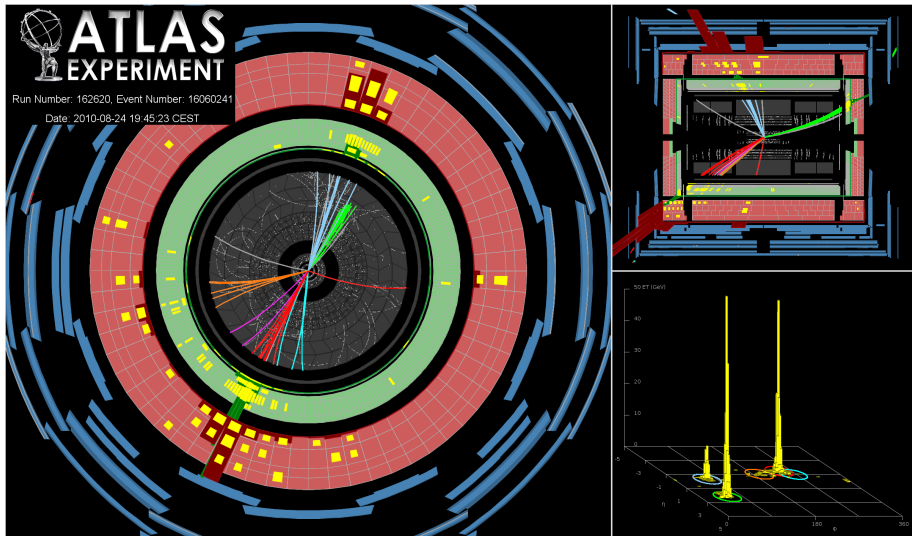
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Applications

- ubiquitous in collider physics
- around since 40 years
- used in at least 60% of LHC analyses

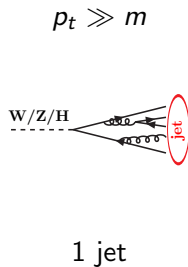
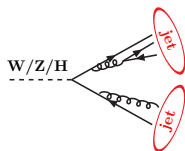
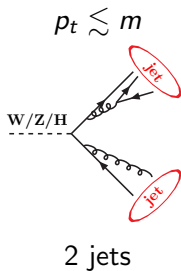
Example of a LHC event



Jet substructure (and boosted objects):

there is more to the picture

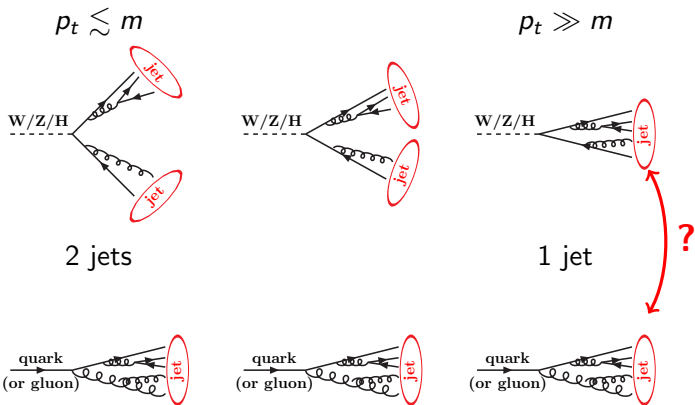
Boosted objects



(massive) objects produced boosted (energy \gg mass) are seen as 1 jet:

$$\theta_{q\bar{q}} \sim \frac{m}{p_t}$$

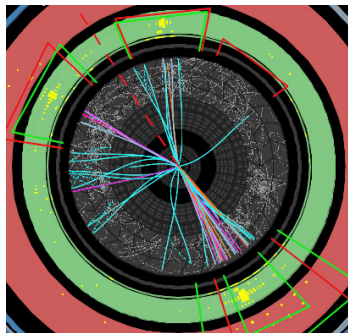
Boosted objects



“Jets” can originate from sth else than a QCD parton (quark/gluon)!
How do we tell?

Other examples

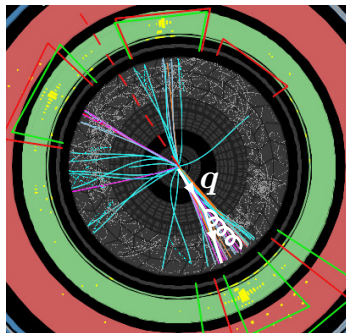
What jet do we have here?



Other examples

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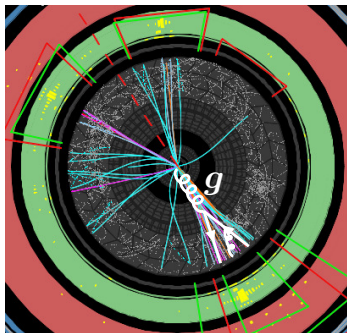
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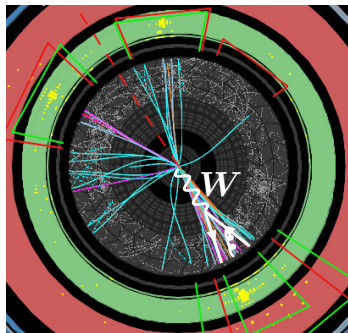
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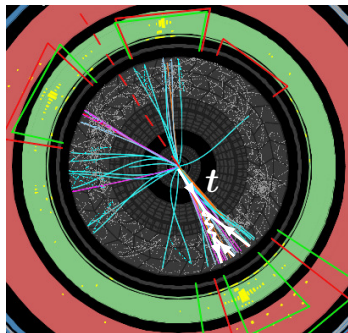
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- a W/Z (or a Higgs)?



Other examples

What jet do we have here?

- a quark?
- a gluon?
- a W/Z (or a Higgs)?
- a top quark?

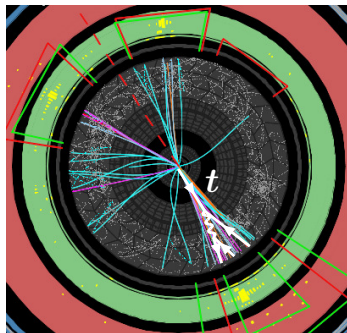


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Source: ATLAS boosted top candidate

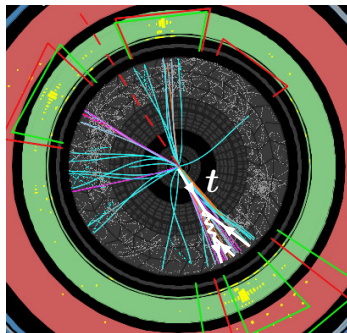


Other examples

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- a quark?
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Main idea

look at the internal dynamics of jets i.e. study their **substructure**
(as opposed to considering jets as monolithic objects)

Main concepts:

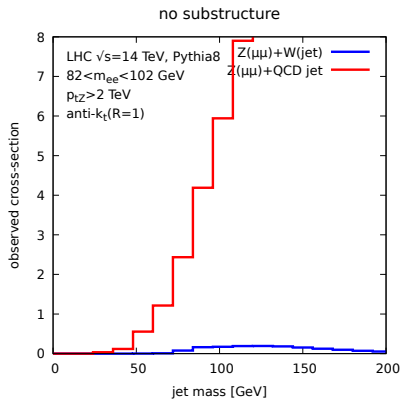
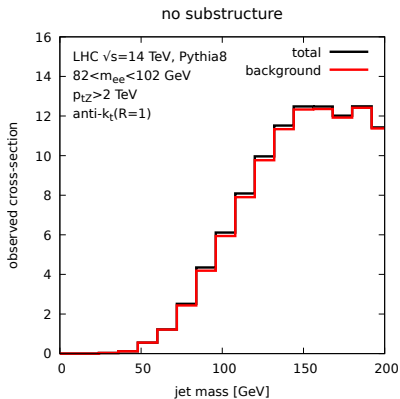
- Compared to standard jets, substructure uses a **large toolkit**
Clearly beyond the scope of this overview

Main concepts:

- Compared to standard jets, substructure uses a **large toolkit**
Clearly beyond the scope of this overview
- Basic tools are organised around $2_{(3)}$ major concepts:
 - ✓ “peak/prong finders” :
 - $W/Z/H/t$ decay into hard partons \Rightarrow jets with multiple hard cores
 - QCD (q/g) jets dominated by soft radiation \Rightarrow single coresTools search for multiple hard cores
 - ✓ Radiation patterns:
colourless $W/Z/H$ has less radiation than q/g jets
Tools (jet shapes) to quantify radiation
 - ✓ (also grooming to remove soft contamination from fat jets)

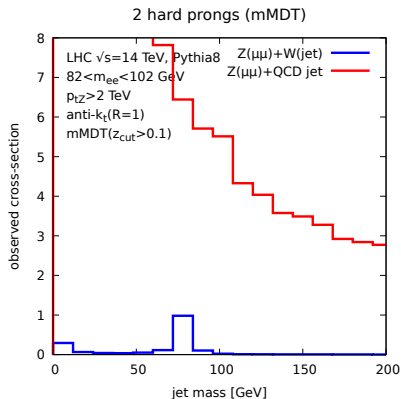
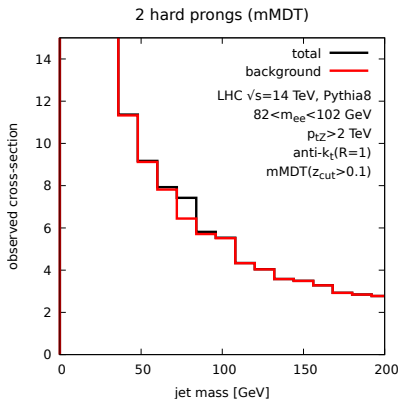
A practical example

Boosted W jets: separate boosted $W \rightarrow q\bar{q}$ from QCD jets
in $Z(\rightarrow \mu^+\mu^-)+\text{jet}$ events



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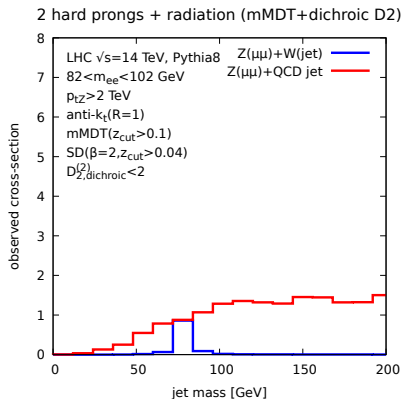
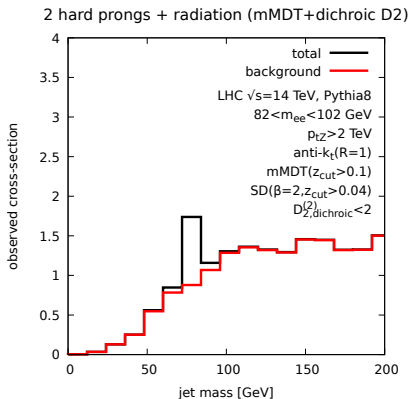
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[mMDT/SD: M.Dasgupta,A.Fregoso,S.Marzani,G.Salam,13; S.Marzani,GS,J.Thaler,14]

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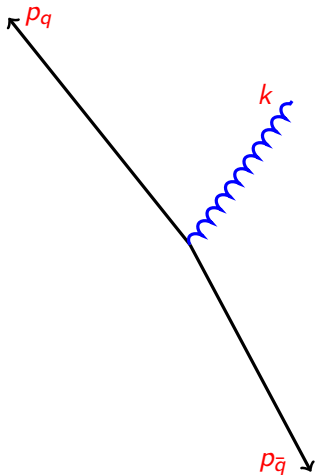
D_2 : A. Larkoski, G. Salam, J. Thaler, 13; I. Moutl, L. Necib, J. Thaler, 16; dichroic: G. Salam, L. Schunk, GS, 16

Interlude:

A useful representation of radiation in a jet

Basic features of QCD radiations

Take a gluon emission from a $(q\bar{q})$ dipole



Emission:

$$k^\mu \equiv z_q p_q^\mu + z_{\bar{q}} p_{\bar{q}}^\mu + k_\perp^\mu$$

3 degrees of freedom:

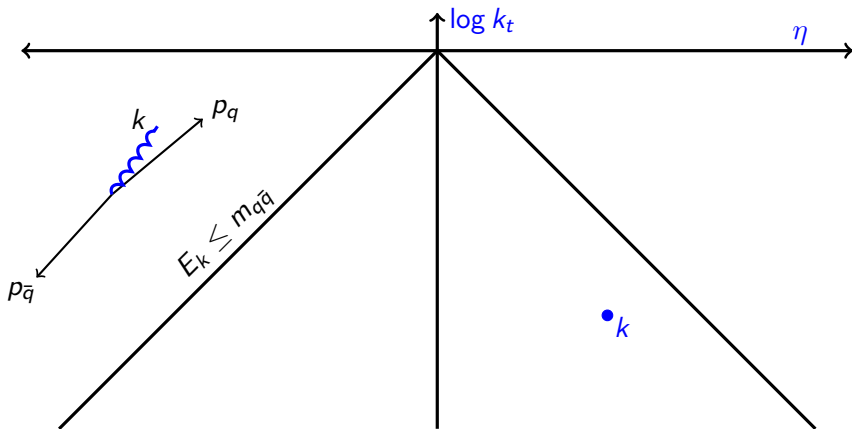
- Rapidity: $\eta = \frac{1}{2} \log \frac{z_q}{z_{\bar{q}}}$
- Transverse momentum: k_\perp
- Azimuth ϕ

In the soft-collinear approximation

$$d\mathcal{P} = \frac{\alpha_s(k_\perp) C_F}{\pi^2} d\eta \frac{dk_\perp}{k_\perp} d\phi$$

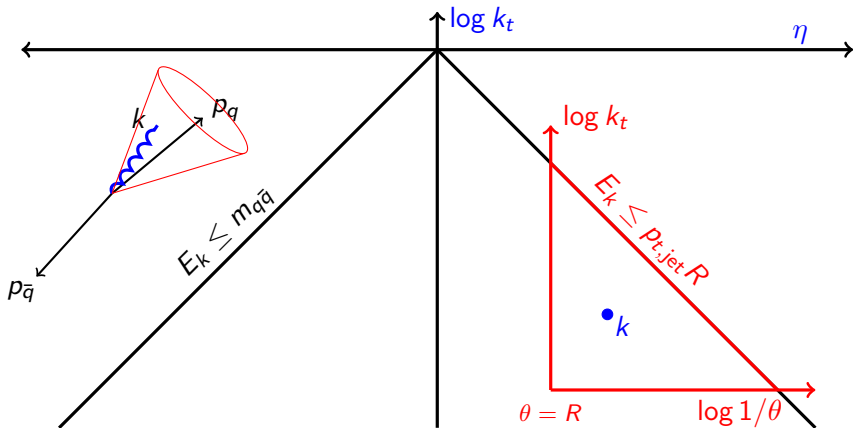
Basic features of QCD radiations: the Lund plane

Lund plane: a natural representation uses η and $\log k_{\perp}$



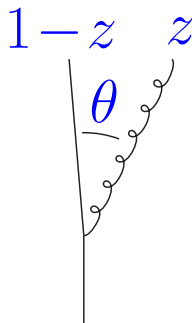
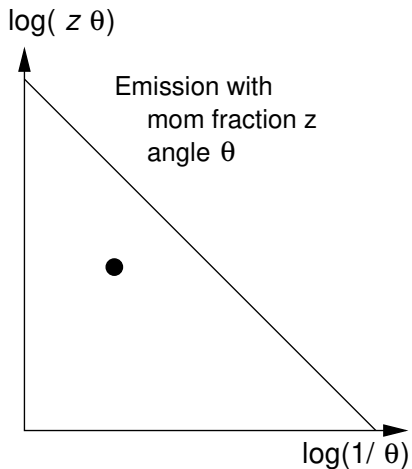
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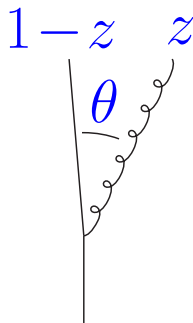
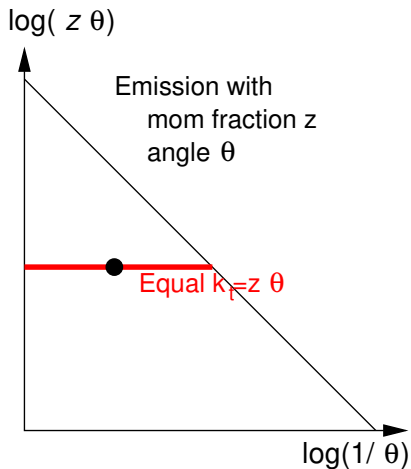


For a jet: $\eta = -\log \tan \theta/2 \approx \log 1/\theta$, $\theta < R$

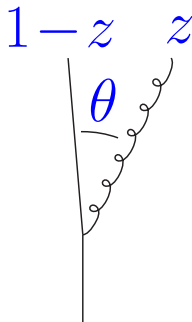
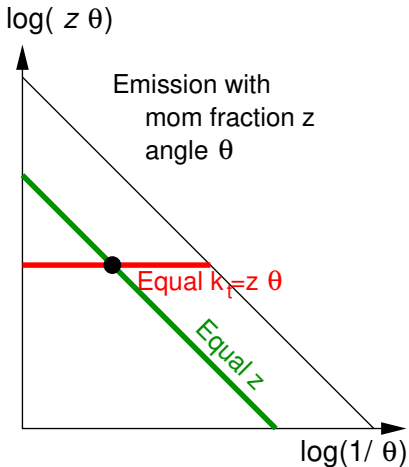
A look into the Lund plane kinematics



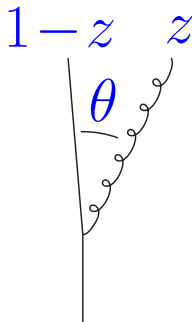
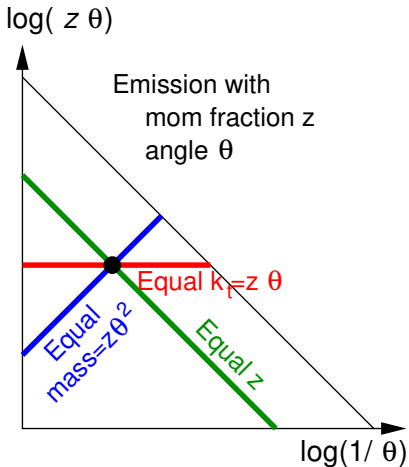
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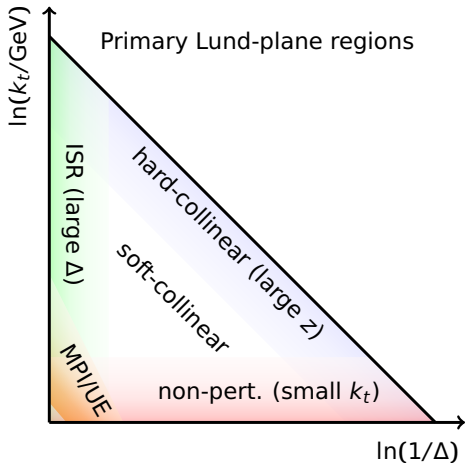
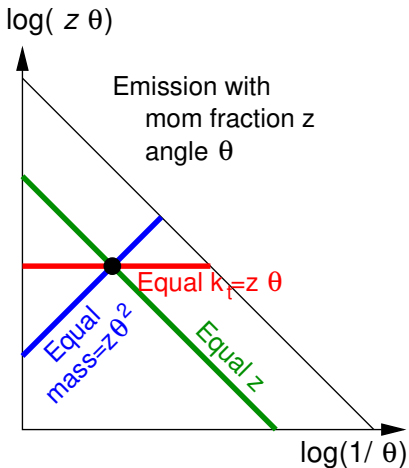
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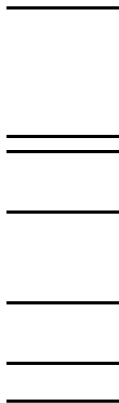


Jet substructure:

A few examples

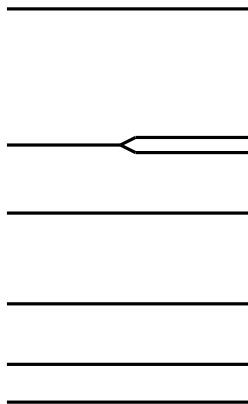
Frequent tool: Cambridge/Aachen (de-)clustering

Cambridge/Aachen: iteratively recombine the closest pair



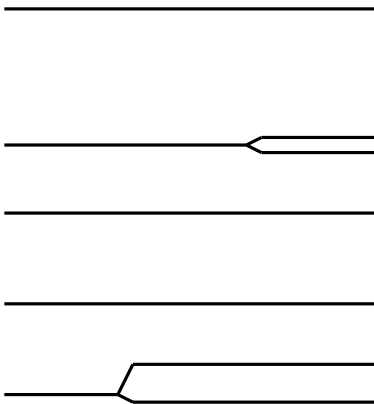
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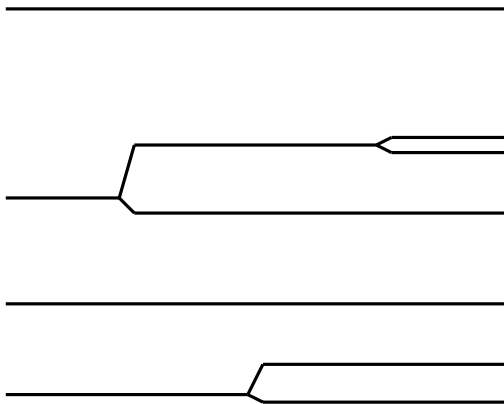
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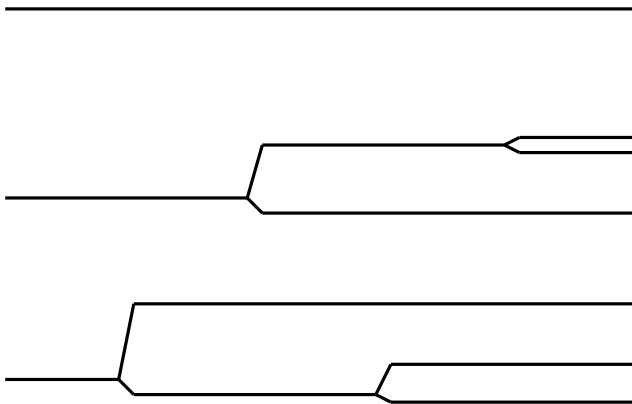
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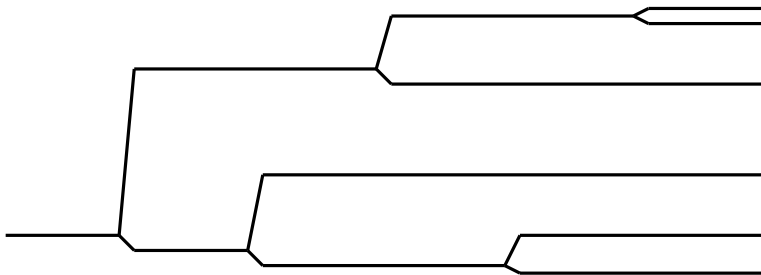
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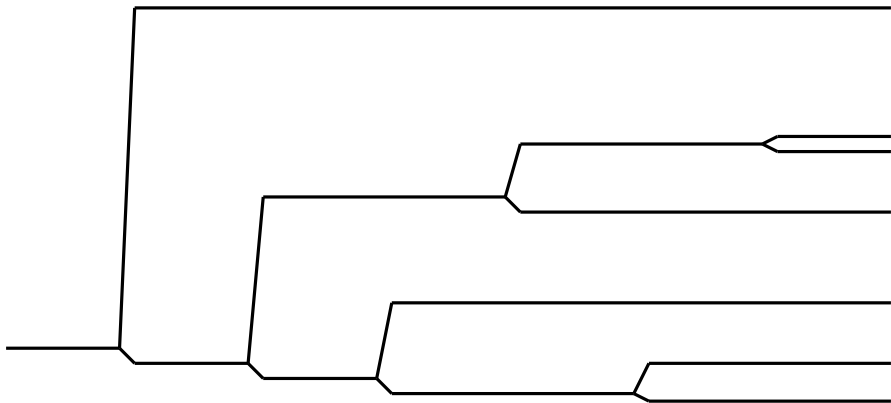
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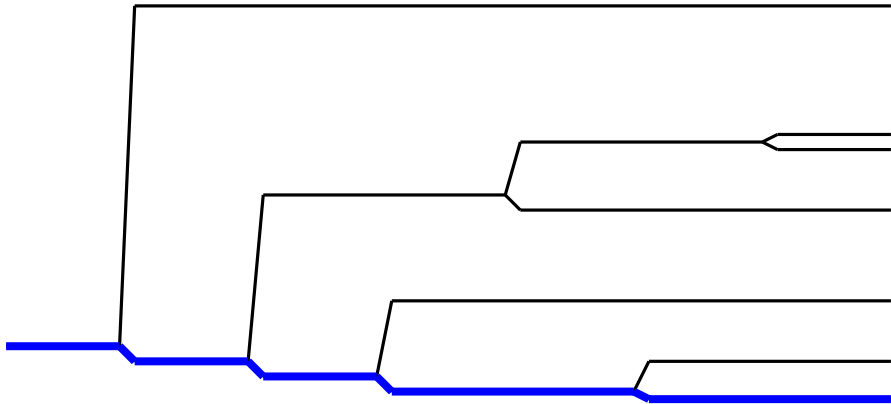
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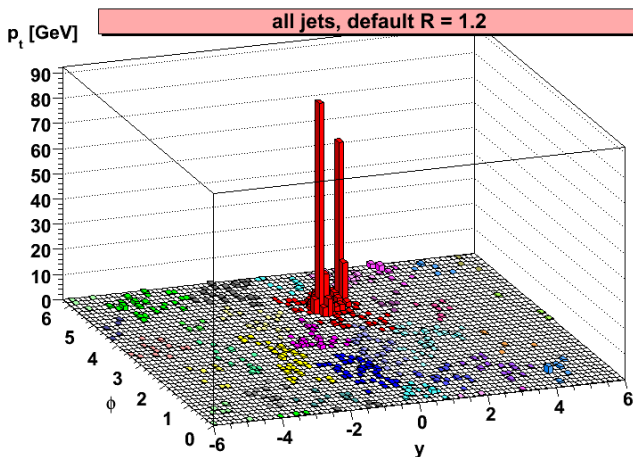


Usage: iteratively undo the clustering to study internal jet dynamics

Typically: follow the hardest branch (largest p_t or z)

Example: mMDT/SoftDrop prong finder

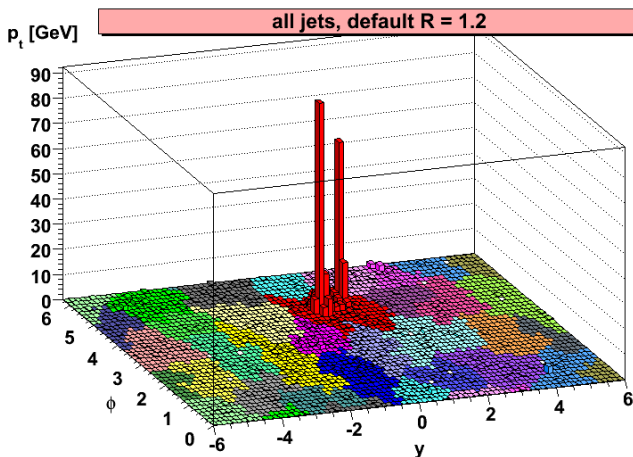
[J.Butterworth,A.Davison,M.Rubin,G.Salam,08]



(modified)MassDrop

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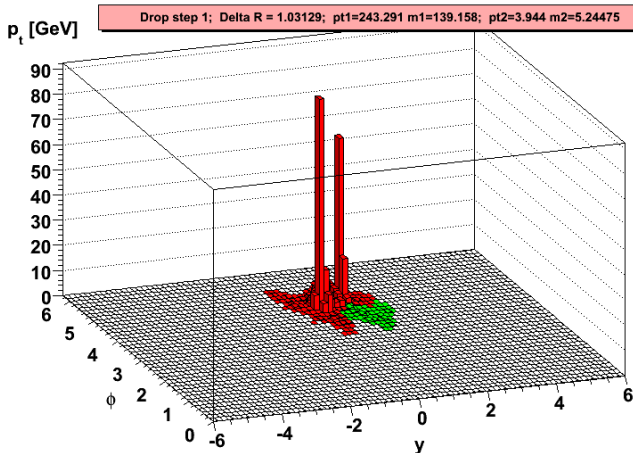


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Idea: undo clustering
until $z > z_{\text{cut}} \approx 0.1$

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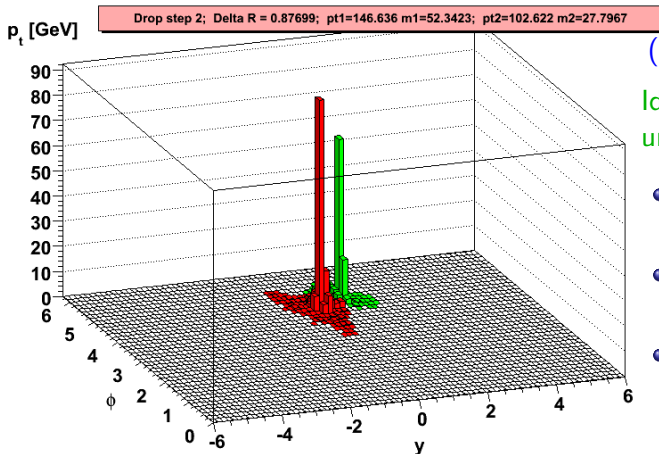
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- undo the last clustering step
- $z = 0.016 < 0.1$
carry on

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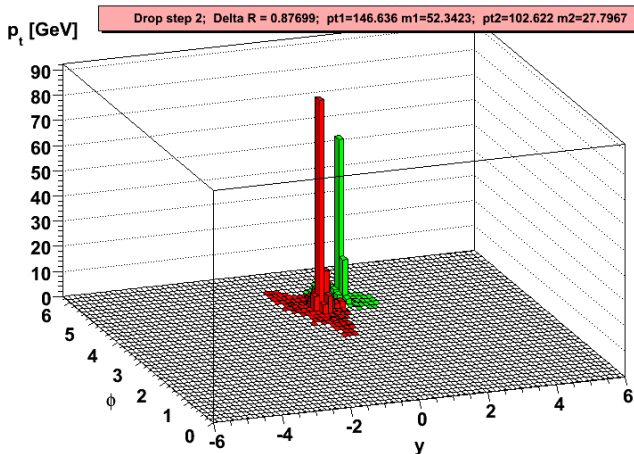
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- $z = 0.41 > 0.1$
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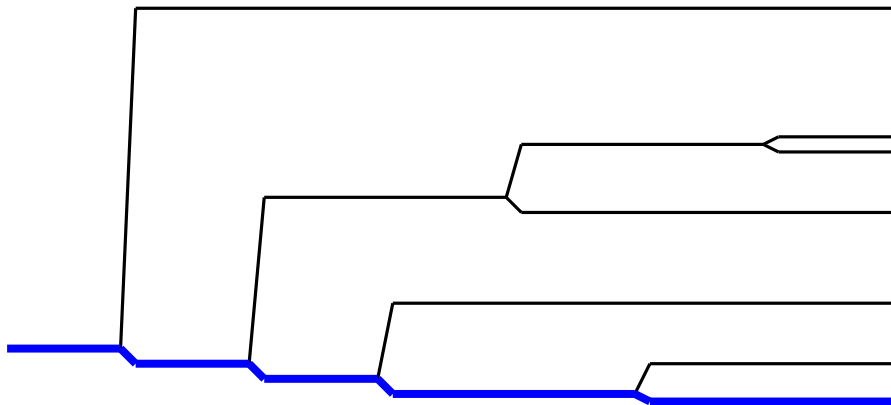
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Variant: **SoftDrop**: impose $z > z_{\text{cut}} \theta^\beta$

[A.Larkoski,S.Marzani,GS,J.Thaler,14]

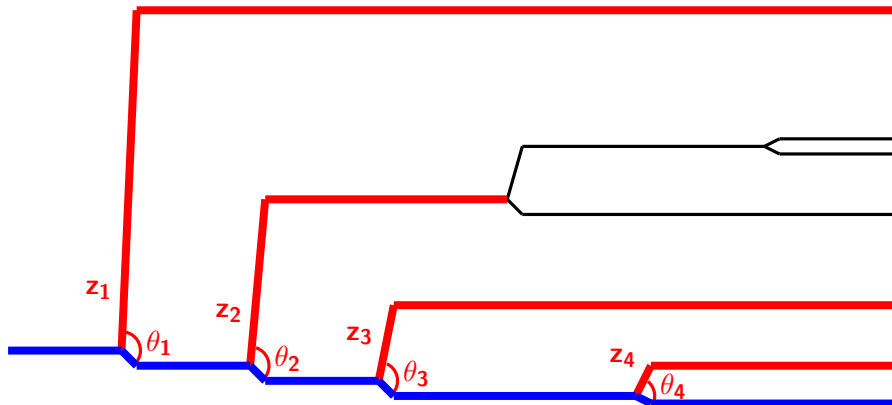
Visualising the sustructure with the Lund plane

[F.Dreyer,G.Salam,GS,18]



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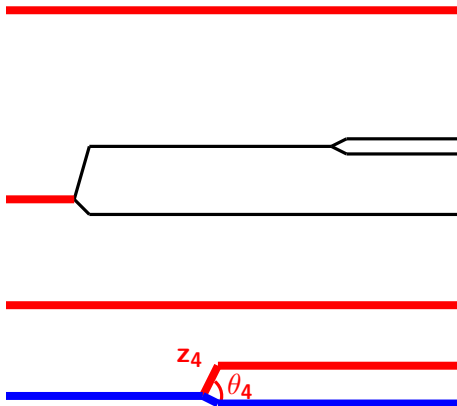
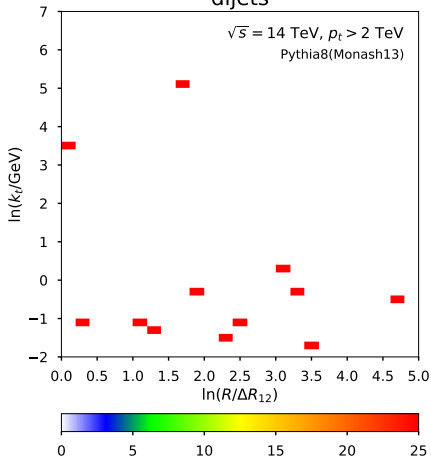


Consider all the emissions from the hardest branch

Visualising the sustructure with the Lund plane

[F.Dreyer,G.Salam,GS,18]

One jet
dijets

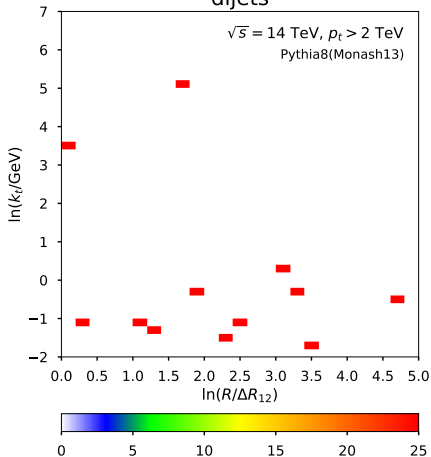


Consider all the emissions from the hardest branch
Put them in the Lund plane

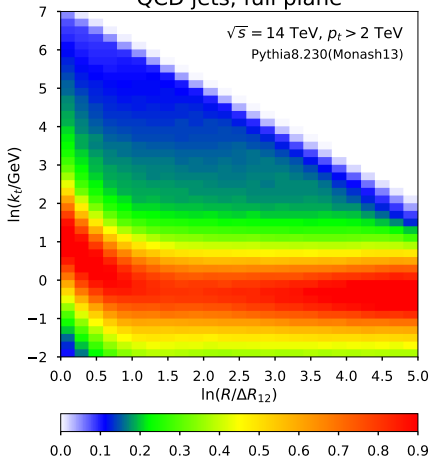
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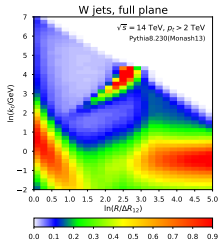
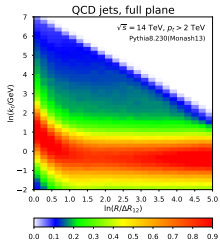


Average over jets
QCD jets, full plane



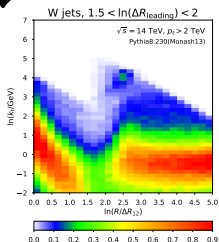
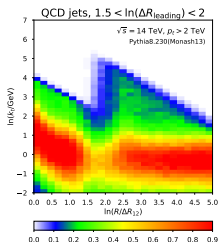
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Lund plane and W tagging

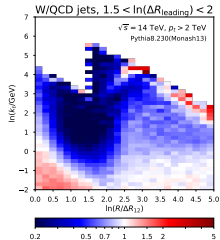


- In practice: split into a “leading” emission and Lund plane for all the others
- Use ratio to build a log-likelihood discriminant

↓
Lund plane
after leading removal



ratio

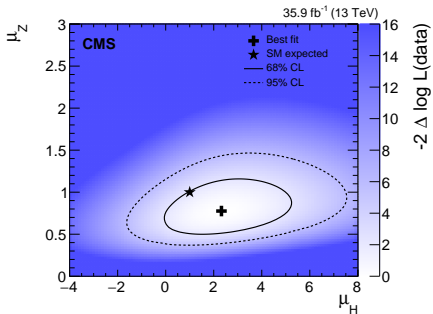
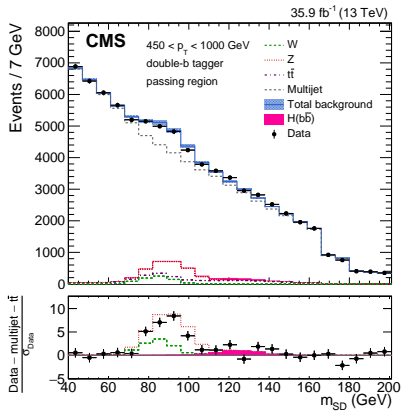


Jet substructure:

Measurements and searches

Measurement example: boosted $H \rightarrow b\bar{b}$

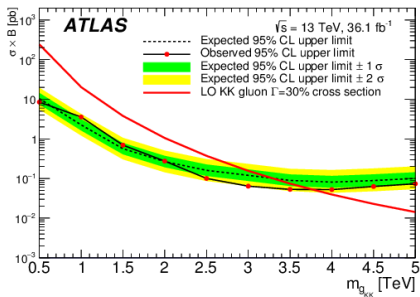
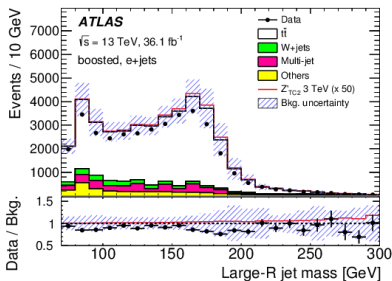
Jet mass after boosted 2-prong tagging: prong finder (mMDT/SD)
+ radiation constraint ($N_2^{(1,DDT)}$)
+ double b tagging



[CMS, 1709.05543]

Search example: $g_{KK} \rightarrow$ boosted $t\bar{t}$

Boosted top identified via: prong finder (trimming)
+ radiation constraint (τ_{32})



[ATLAS, 1804.10823]

- One probes physics at increasingly larger scales
- New physics scales are pushed towards larger scales
- Collision energies could increase

Jet substructure will be increasingly relied upon

Jet substructure:

Analytic understanding in QCD

Analytic understanding of substructure

Idea: boosted $\equiv m \ll p_t \Rightarrow$ expect $\log p_t/m \Rightarrow$ resummation

Analytic understanding of substructure

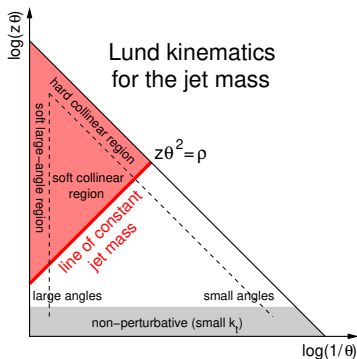
Idea: boosted $\equiv m \ll p_t \Rightarrow$ expect $\log p_t/m \Rightarrow$ resummation

Jet mass: we have

- one emission with $z\theta^2 = \frac{m^2}{p_t^2 R^2}$
→ factor $\color{red}{/}$
- no emission at larger $z\theta^2$
→ factor $\exp(-\color{red}{\blacktriangleright})$

Giving $\bar{\alpha}_s = \frac{\alpha_s C_R}{\pi}$

$$\frac{m}{\sigma} \frac{d\sigma}{dm} = \bar{\alpha}_s \log \frac{p_t R}{m} \exp \left[-2\bar{\alpha}_s \log^2 \frac{p_t R}{m} \right]$$



Analytic understanding of substructure

Idea: boosted $\equiv m \ll p_t \Rightarrow$ expect $\log p_t/m \Rightarrow$ resummation

Jet mass: we have

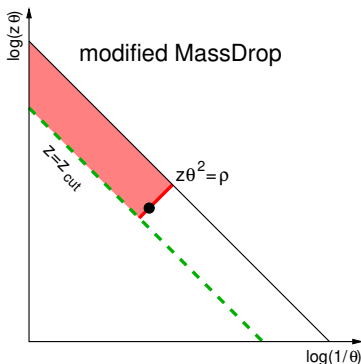
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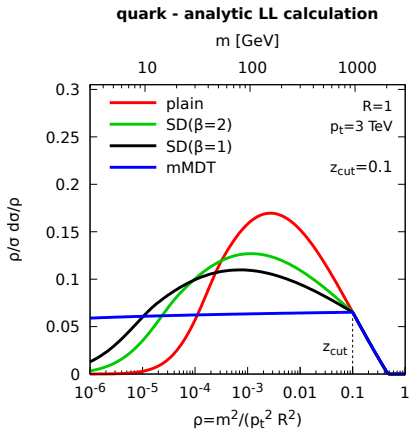
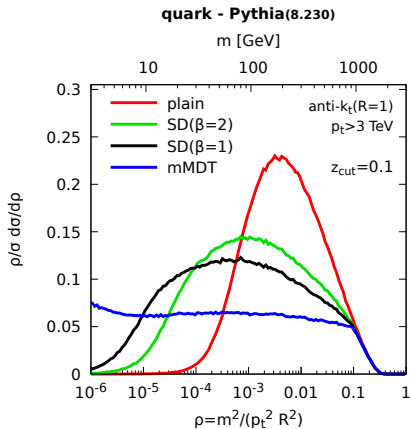
mMDT jet mass: same but $z > z_{\text{cut}}$

$$\frac{m}{\sigma} \frac{d\sigma}{dm} = \frac{\bar{\alpha}_s}{2} \log \frac{1}{z_{\text{cut}}} \exp \left[\bar{\alpha}_s \log \frac{1}{z_{\text{cut}}} \log \frac{p_t R}{m} \right]$$



[M. Dasgupta, A. Fregoso, S. Marzani, G. Salam, 13]

Analytic v. Monte Carlo

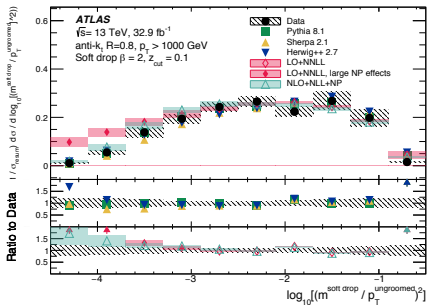
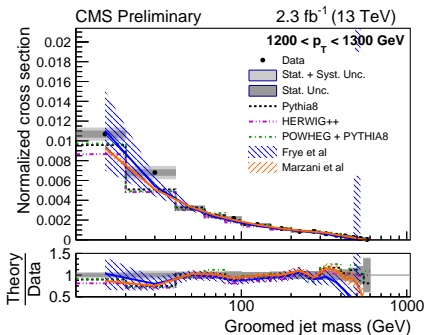


The big picture

- Now a wide range of tools are “calculable”
Almost all 2-prong finders, a series of jet shapes, basic 3-prong finders
- brings a better understanding of the details at play
source of performance, undesirable features, transition points,...
- has allowed for the development of improved tools
e.g. mMDT, D_2 , generalised ECFs, dichroic ratios
- Approached from “standard QCD” or SCET
- has allowed for the development of improved resummation techniques

Jet substructure: Precision measurements

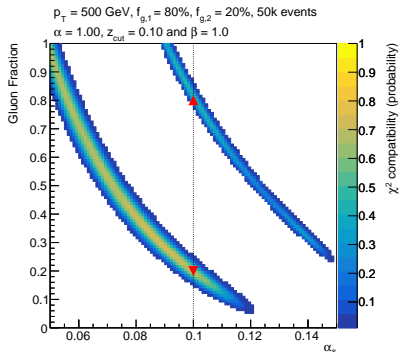
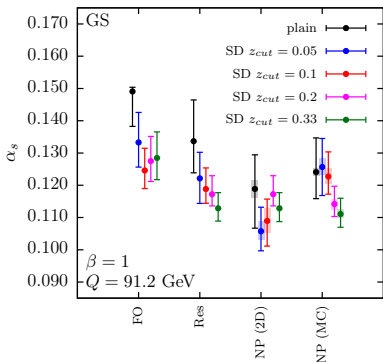
- ▶ LHC Measurements (CMS-PAS-SMP-16-010, ATLAS CERN-EP-2017-231)
- ▶ NNLL+LO in SCET (Frye,Larkoski,Schwartz,Yan; assumes small z_{cut})
- ▶ NLL+NLO in "standard QCD" (Marzani,Schunk,GS; includes (LL) finite z_{cut})



good overall agreement with the data, small non-perturbative effects

Towards measuring α_s

Precise+small NP effects suggests we use it for precision measurements



Already a possible gain at LEP

[S.Marzani,D.Reichelt,S.Schumann,GS,
V.Theeuwes, in prep]

Large potential at the LHC

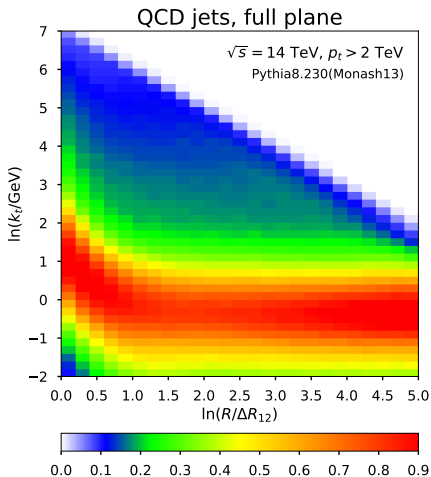
Still key pieces missing

[Study at Les-Houches 2017]

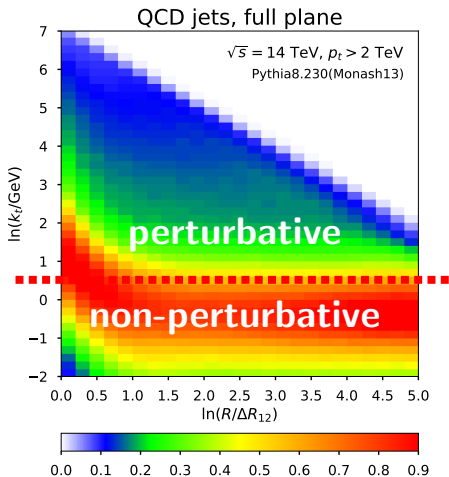
Jet substructure:

Shower constraints

Lund plane and Monte-Carlo generators

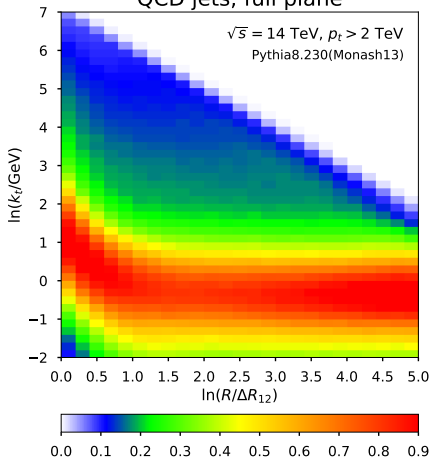


Lund plane and Monte-Carlo generators

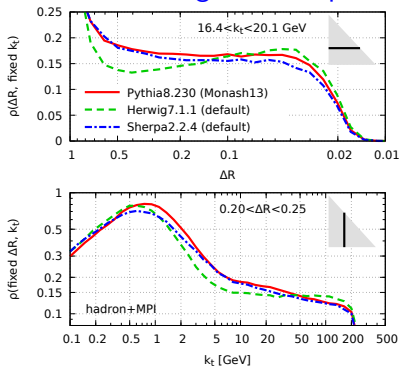


Lund plane and Monte-Carlo generators

QCD jets, full plane



Slices through the 2D plane



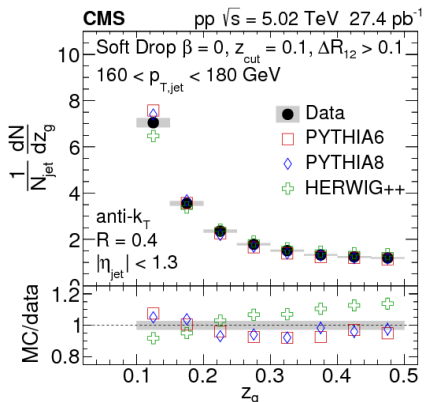
- Flat at small angles (until ISR)
- $\alpha_s(k_t)$ then non-pert bump
- Differences between MCs
- **calls for measurement**

Jet substructure:

Usage in heavy-ion collisions

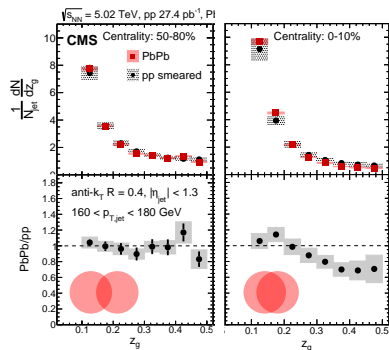
The mMDT/SD grooming momentum fraction z_g

Example: $z_g \equiv$ the z fraction that passes the mMDT/SD condition



[CMS,1708.09429]

- \approx access to the splitting functions
- Very interesting analytic structure

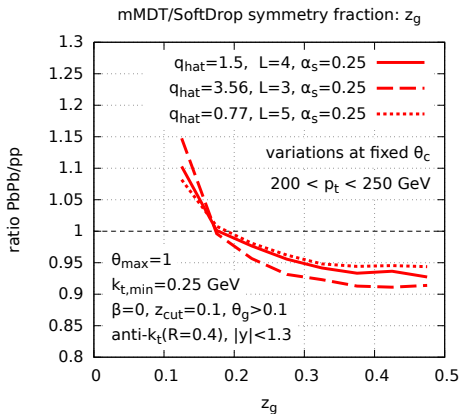
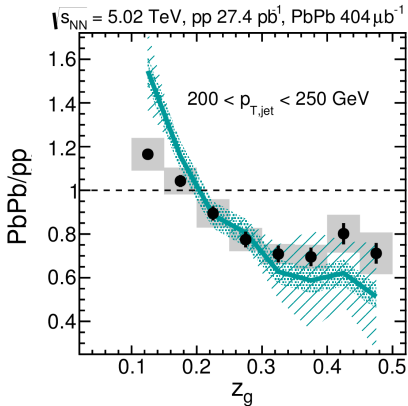


- Measured in pp and $PbPb$
- First use of CMS Open Data

[Larkoksi,Marzani,Thaler,Tripahee,Xue,17]

The mMDT/SD grooming momentum fraction z_g

Modifications due to interactions with the quark-gluon plasma



Work in progress to calculate this in QCD

[P.Caual,E.Iancu,GS,soon]

Jet substructure: Machine Learning

Huge effort in using deep learning in the context of jet substructure

Applied to many systems

- Boosted topologies: $W/Z/H$ bosons, top quarks, ...
- b tagging, quark/gluon separation
- pileup mitigation
- fast detector simulation

Several approaches

- Inputs: jet variables, images of jets, jet constituents, subjets/clustering trees
- Architectures: CNN, DNN, ANN, LSTM

Lund plane as an example

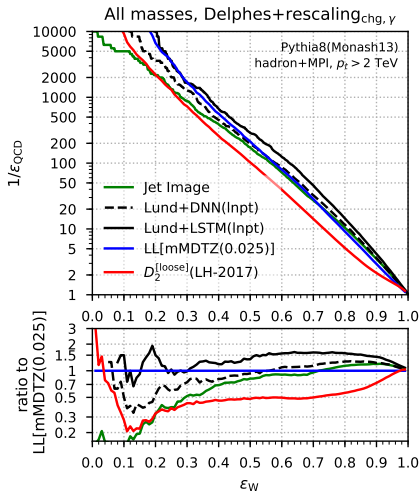
Example using our “Lund plane” approach:

- “Lund image” fed to a Dense Neural Network
- “Lund coordinates” fed to a Long Short Term Memory network

Lund plane as an example

Example using our “Lund plane” approach:

- “Lund image” fed to a $D_{\text{ense}} N_{\text{eural}} N_{\text{etword}}$
- “Lund coordinates” fed to a $L_{\text{ong}} S_{\text{hort}} T_{\text{erm}} M_{\text{emory}}$ network



- great performance
- LSTM does even better than Log-Likelihood
- Note: input motivated by QCD
See also: energy-flow polynomials

[Lund: F.Dreyer, G.Salam, GS, 18]
[Jet Image: J.Cogan, M.Kagan, E.Strauss, A.Schwartzman, 14; L.de Oliveira, M.Kagan, L.Mackey, B.Nachman and A.Schwartzman, 15]

Take-home messages

Jet substructure has gained a lot of importance in the past decade

- Important tool for LHC physics (searches and measurements)
- exciting pQCD phenomenology
 - ▶ understanding and development of tools
 - ▶ precision pheno at the LHC
 - ▶ interesting QCD structure emerging (not covered here)
- Expansion towards new horizons:
 - ▶ heavy-ion hard probes
 - ▶ machine learning
- Recent work: Lund planes are useful in many aspects