

# ***New tools in jet physics: SISCone (new cone algorithm) - jet areas (new concept)***

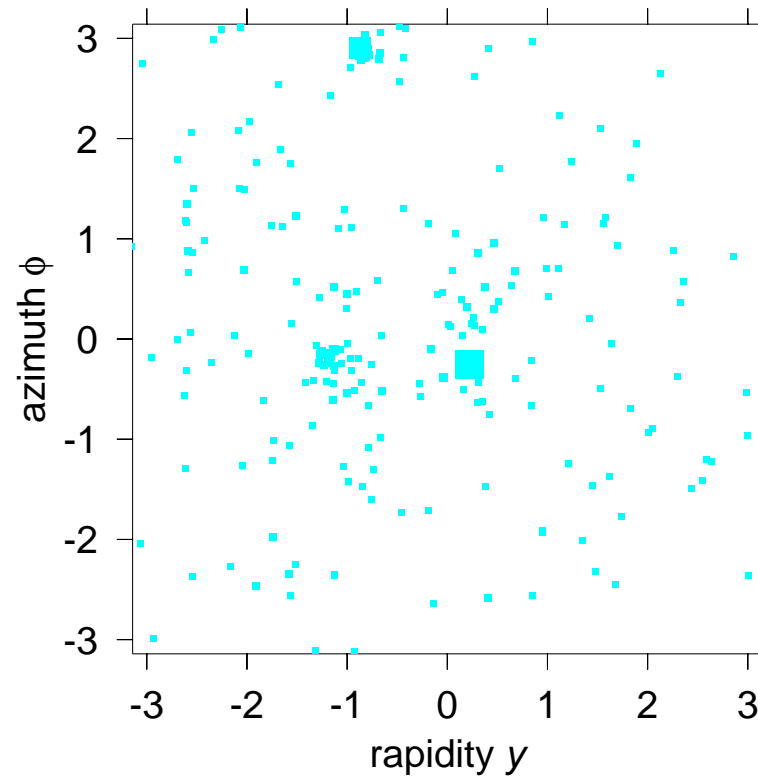
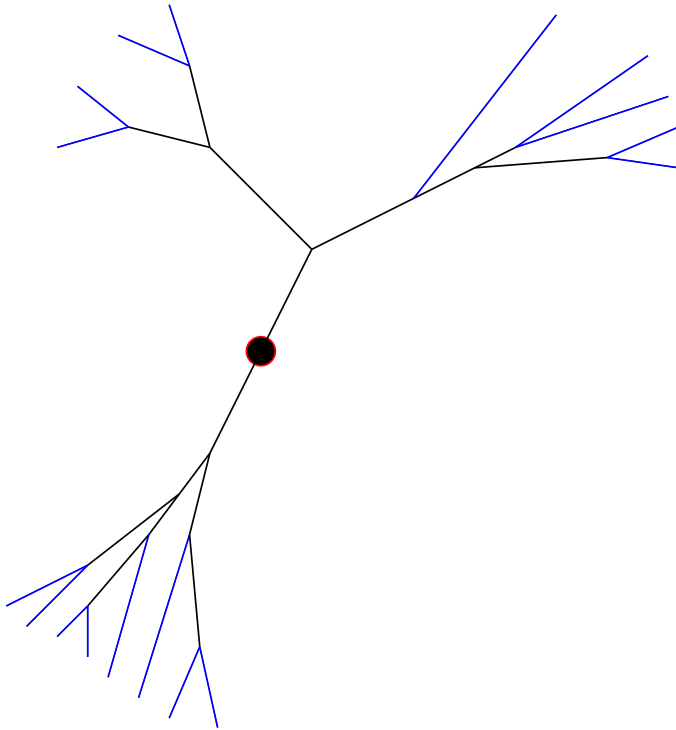
**Grégory Soyez**

**Brookhaven National Laboratory**

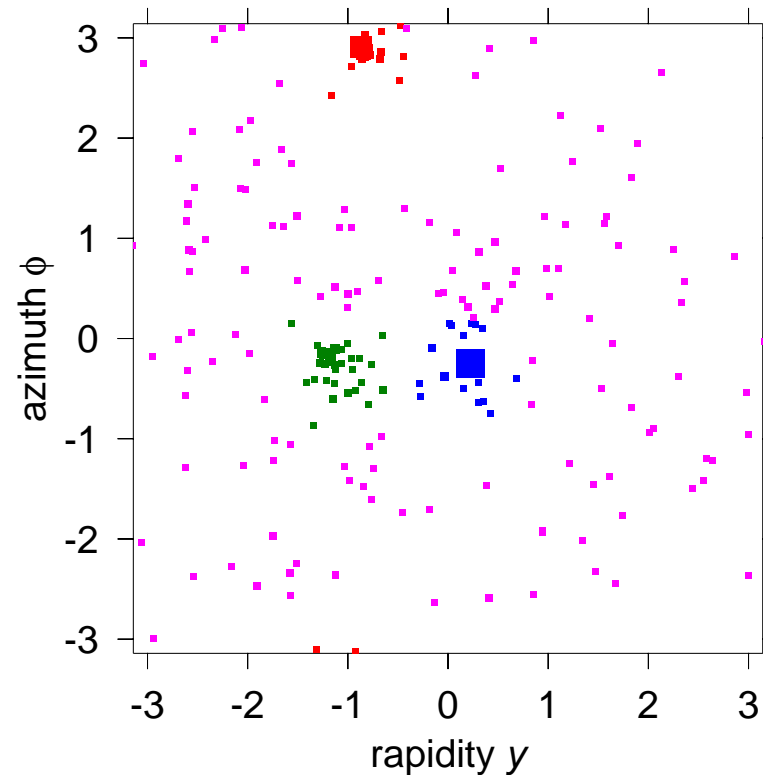
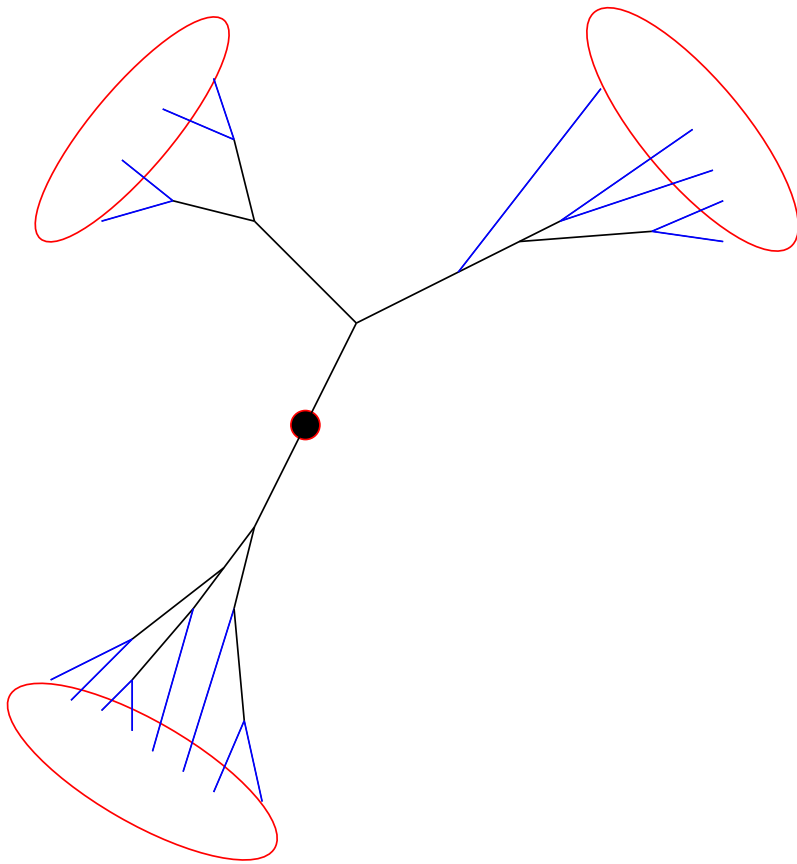
- In collaboration with Gavin Salam
- paper available as JHEP 05 (2007) 086 [arXiv:0704.0292]
- code available at <http://projects.hepforge.org/siscone>  
FastJet plugin: <http://www.lpthe.jussieu.fr/~salam/fastjet>
- Paper with Matteo Cacciari and Gavin Salam in preparation

- Introduction: [jet algorithms](#) in general
- [Infrared-Safety issues](#):
  - Why is this mandatory?
  - IR unsafety of the JetClu and midpoint algorithms
- [SISCone](#): a practical solution
- [Physical consequences](#):
  - Algorithm speed
  - Inclusive jet spectrum
  - Jet mass spectrum in multi-jet events
- [Area of a jet](#)
  - Definition and properties
  - Applications

- Given: set of  $N$  particles with their 4-momentum



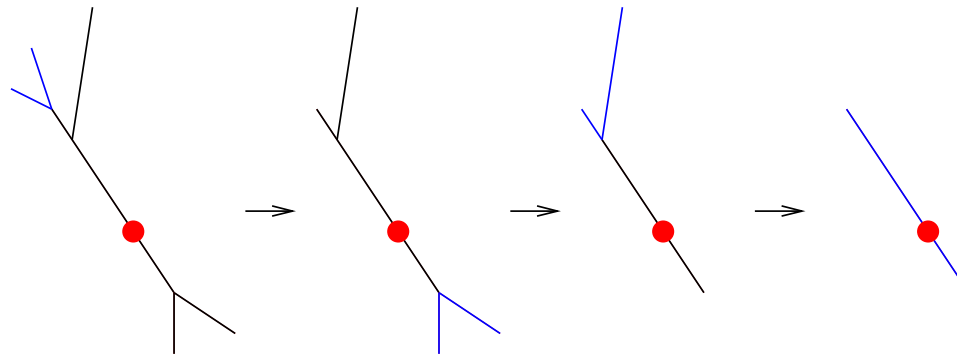
- Given: set of  $N$  particles with their 4-momentum
- Quest: clustering those particles into jets



⇒ understand the original particle-level process

## Class 1: recombination

Successive recombinations of the “closest” pair of particle



- Distance:

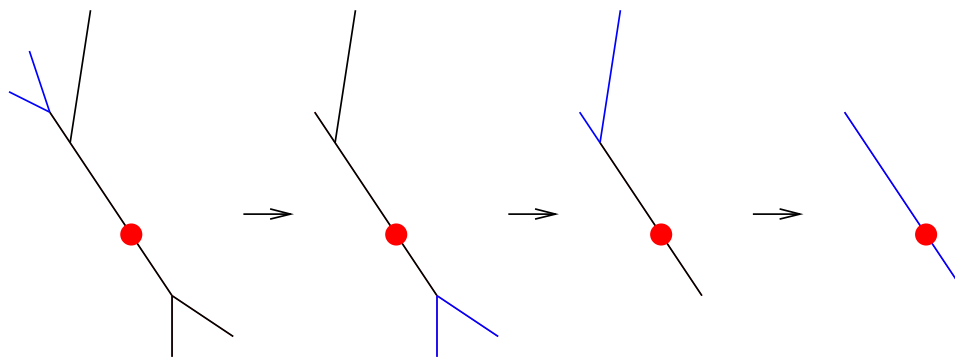
$$\underline{k_t}: \quad d_{i,j} = \min(k_{t,i}^2, k_{t,j}^2)(\Delta\phi_{i,j}^2 + \Delta y_{i,j}^2)$$

$$\underline{\text{Aachen/Cam.}}: \quad d_{i,j} = \Delta\phi_{i,j}^2 + \Delta y_{i,j}^2$$

- stop when  $d_{\min} > R$

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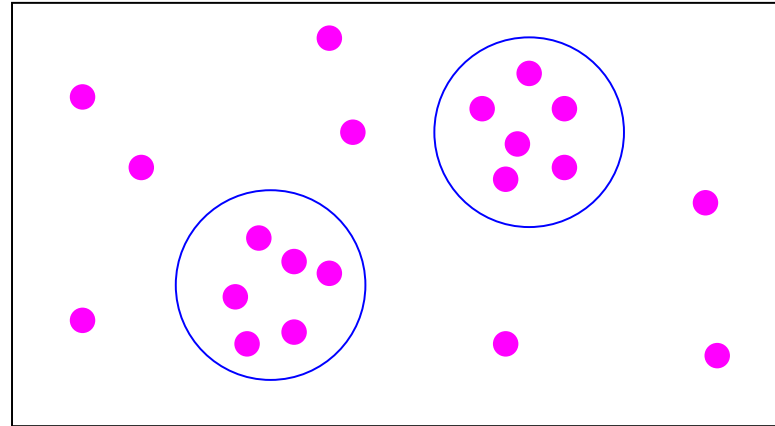
- Often used for  $e^\pm e^\pm$  or  $e^\pm p$

- FastJet : a fast implementation of those algorithms

[www.lpthe.jussieu.fr/~salam/fastjet/](http://www.lpthe.jussieu.fr/~salam/fastjet/) (M. Cacciari, G. Salam)

## Class 2: cone

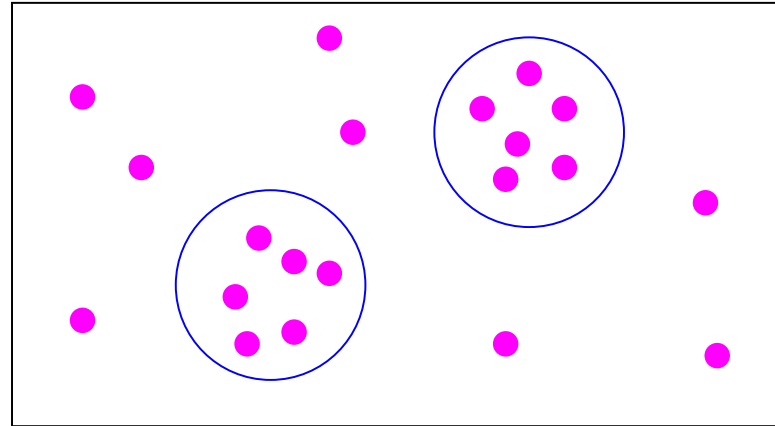
Find directions of dominant energy flow



for a cone of radius  $R$  in the  $(y, \phi)$  plane, stable cones are such that:  
centre of the cone  $\equiv$  direction of the total momentum of its particle contents

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- Often used for  $pp$
- Many cone algorithms: Snowmass, JetClu, PxCone, CDF Midpoint, ...
- BUT none satisfies 1990's requirements



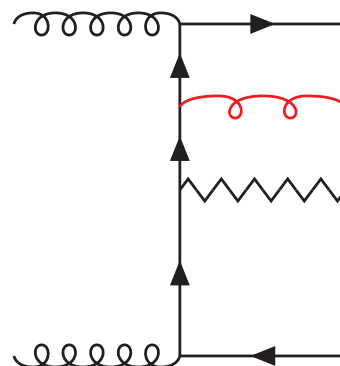
- Snowmass Accord (FERMILAB, 1990):  
any jet algorithm must satisfy
  1. Can be practically used in experimental analysis
  2. Can be practically used in theoretical computations
  3. Can be defined at any order of the perturbation theory
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- Previous cone algorithms:
  - 1, 2 and 4 never satisfied together
  - 5 is unclear (Underlying event and  $R_{sep}$  issues discussed later)

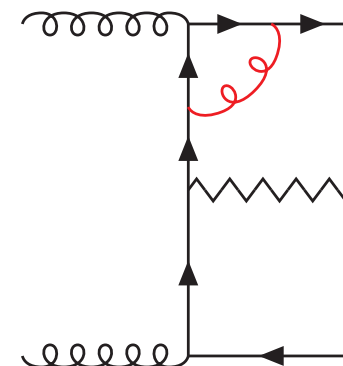
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- This talk shows how to satisfy all these.

Ellipsis: IR safety, i.e. stability upon emission of soft particles, is required for perturbative computations to make sense!

Cancellation of IR divergences between real and virtual emissions of SOFT gluons in QCD



NLO, real



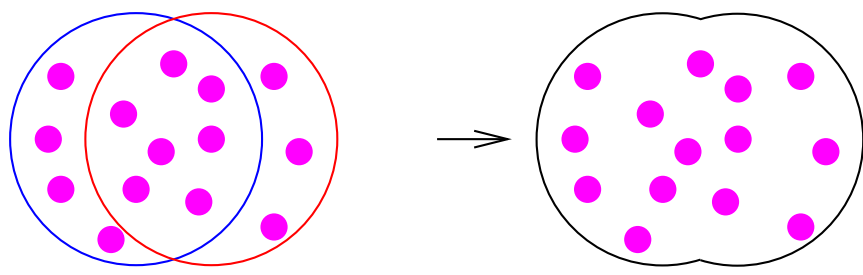
NLO, virtual

- IF Jet clustering is different in both cases, THEN the cancellation is not done and the result is not consistent with pQCD
  - ⇒ **Stable cones must not change upon addition of soft particles**
- Note: 100 GeV jet cannot change by adding a 1 GeV particle  
This would break parton/hadron correspondence

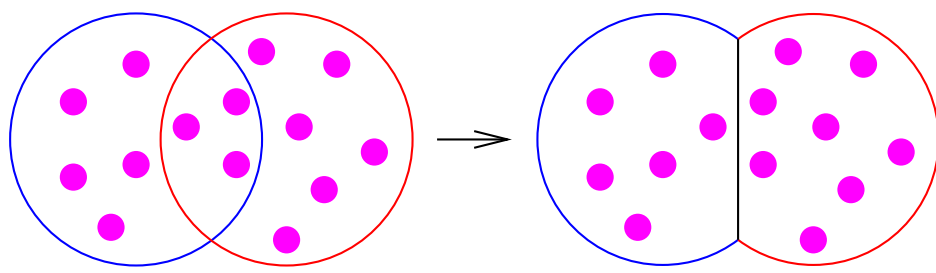
## Modern cone jet algorithm (Tevatron Run II type):

- **Step 1:** find **ALL** stable cones of radius  $R$
- **Step 1':** if some of the particles are not in stable cones, rerun Step 1 with the remaining ones.
- **Step 2:** run a split-merge procedure with overlap  $f$  to deal with overlapping stable cones

$$\tilde{p}_{t,\text{shared}} > f\tilde{p}_{t,\text{min}}$$



$$\tilde{p}_{t,\text{shared}} \leq f\tilde{p}_{t,\text{min}}$$



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This talk: **Why** finding **all** stable cones and **how**.

→ C++ implementation: Seedless Infrared-Safe Cone algorithm (SISCone)

Usual **seeded** method to search stable cones: **midpoint cone algorithm**

- **For an initial seed**
  1. sum the momenta of all particles within the cone centred on the seed
  2. use the direction of that momentum as new seed
  3. repeat 1 & 2 until stable state cone reached



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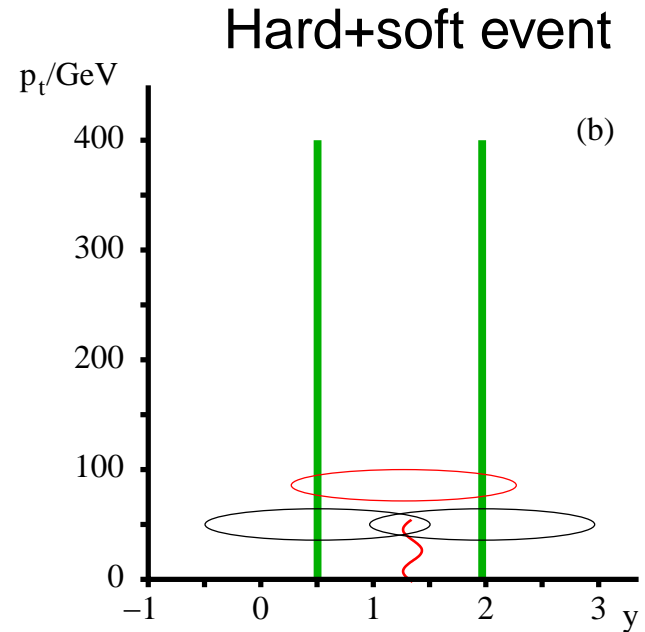
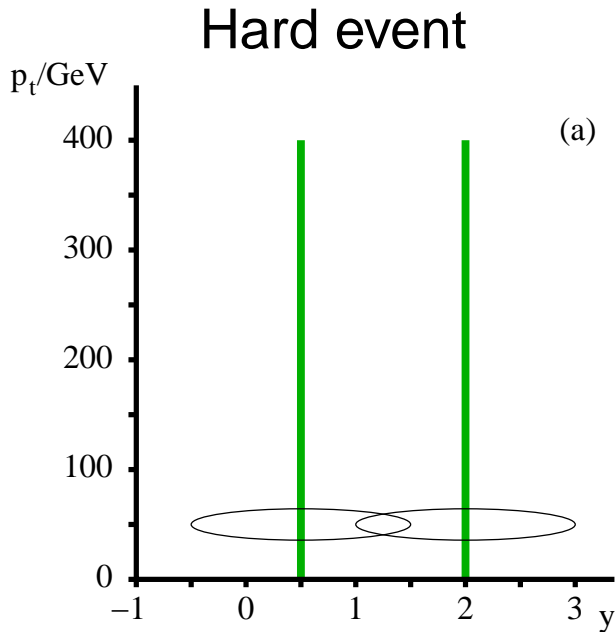
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## Problems:

- the  $p_t$  threshold  $s$  is collinear unsafe
- seeded approach  $\Rightarrow$  stable cones missed  $\Rightarrow$  infrared unsafety
- NB.: addition of soft particles does not modify the set of stable cone, the question is “does our algorithm find all of them”?

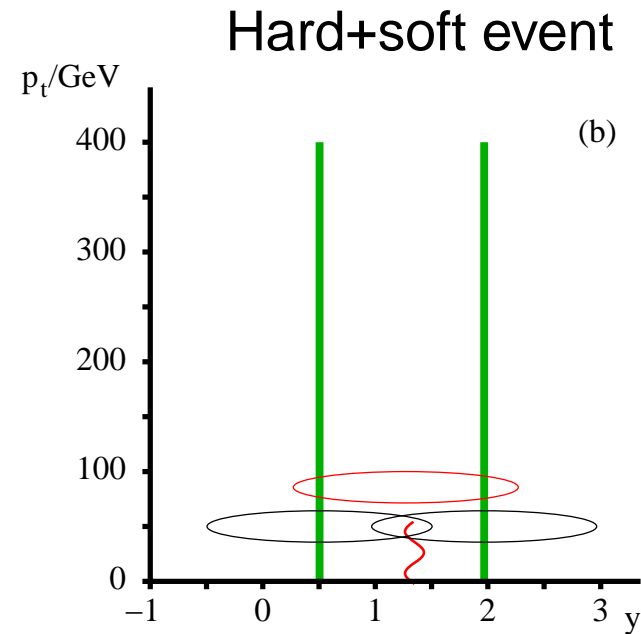
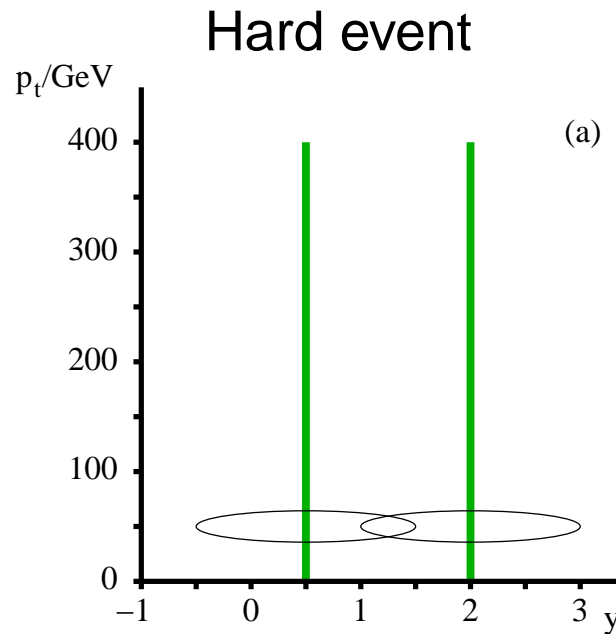


Stable cones:

JetClu:

{1} & {2}

{1} & {2} & {1,2}



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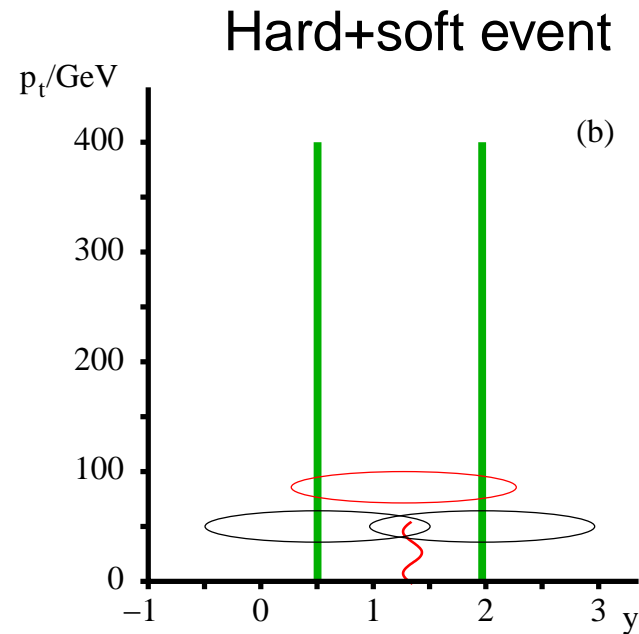
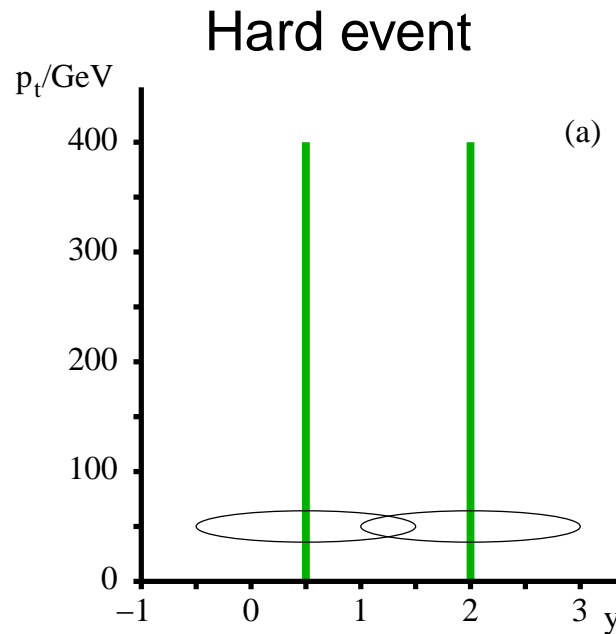
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Jets: ( $f = 0.5$ )

JetClu: {1} & {2}

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**Stable cone missed  $\longrightarrow$  IR unsafety of the JetClu algorithm**



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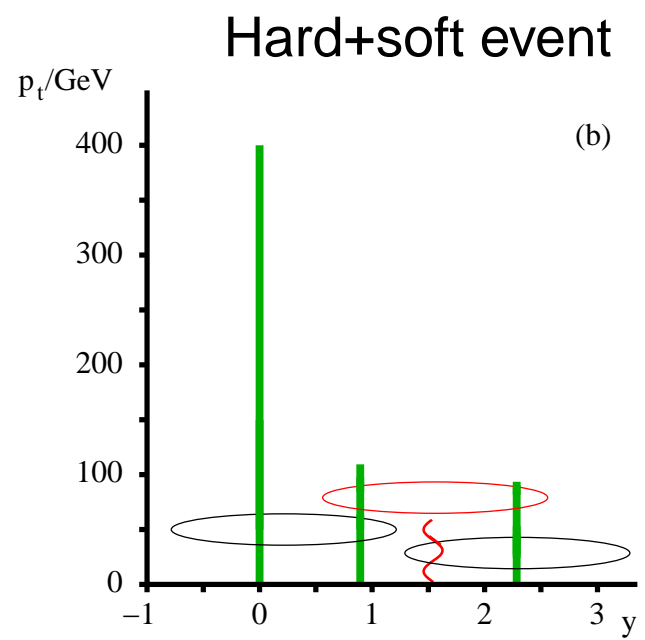
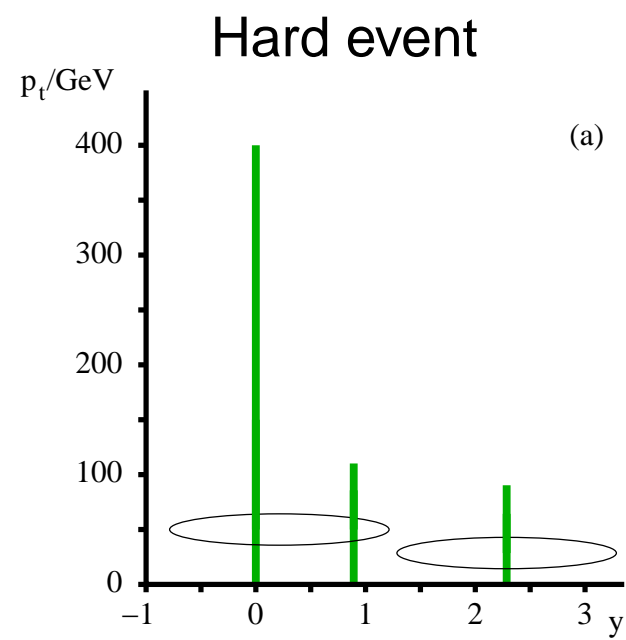
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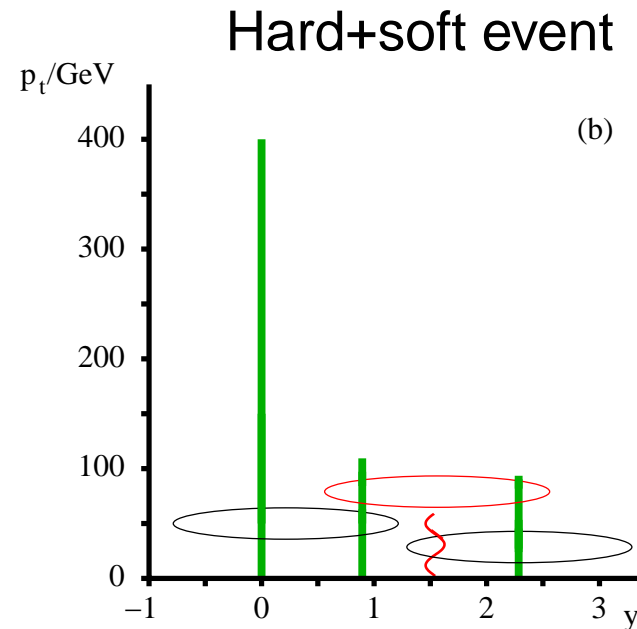
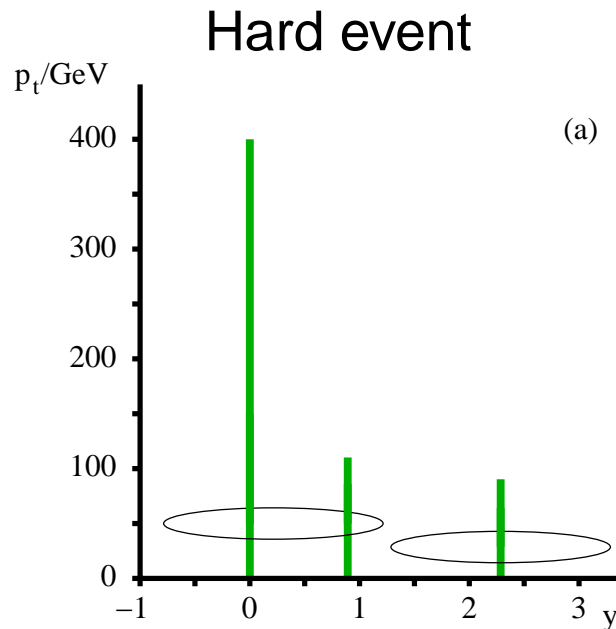


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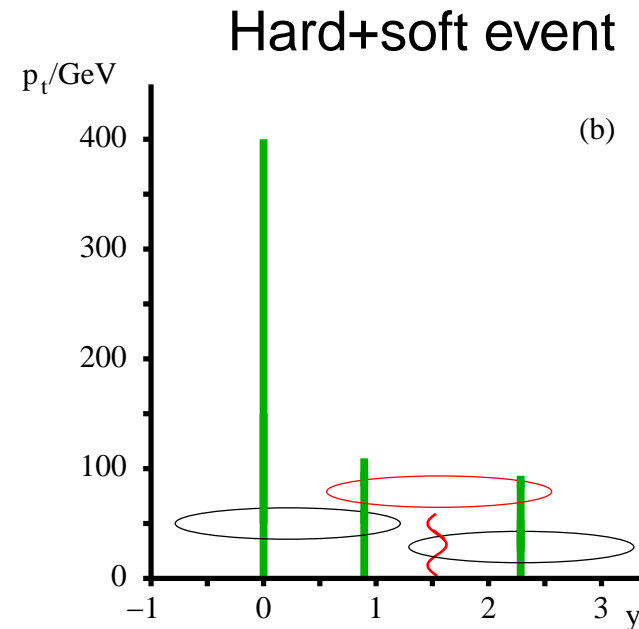
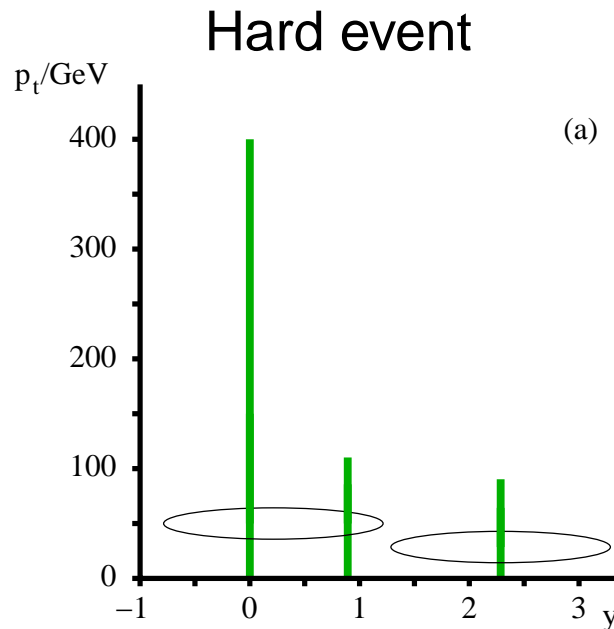
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Stable cones:

Midpoint: {1,2} & {3}

Seedless: {1,2} & {3} & {2,3}

{1,2} & {3} & {2,3}

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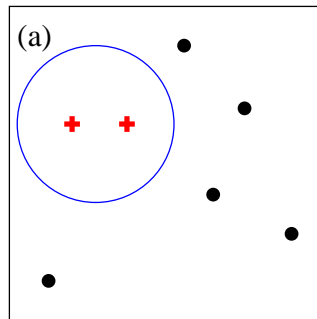


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Complexity is  $\mathcal{O}(N2^N)$   
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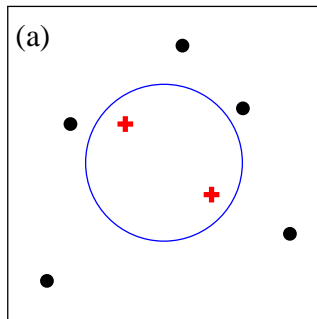
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- Midpoint complexity:
  - For 1 seed: build and check cone content is  $\mathcal{O}(N)$
  - initially  $N$  seeds  $\Rightarrow \mathcal{O}(N)$  stable cones  
 $\Rightarrow \mathcal{O}(Nn)$  new, midpoint, seeds  
 $\Rightarrow$  **midpoint complexity is  $\mathcal{O}(N^2n)$**
  - with  $n \sim N$  the number of points in a circle of radius  $R$
  - Note: the number of stable cones is  $\mathcal{O}(N)$

Idea: use geometric arguments



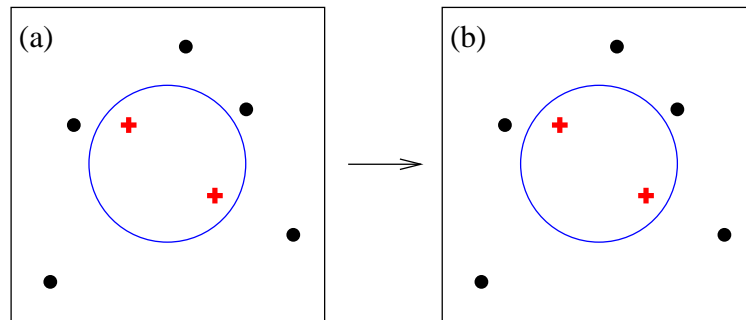
- Enumerate enclosures and check if they are stable

Idea: use geometric arguments



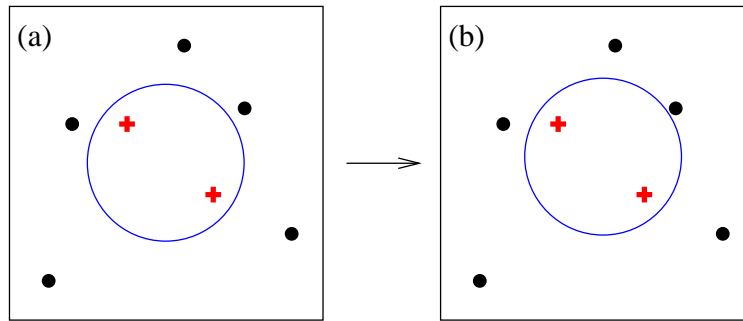
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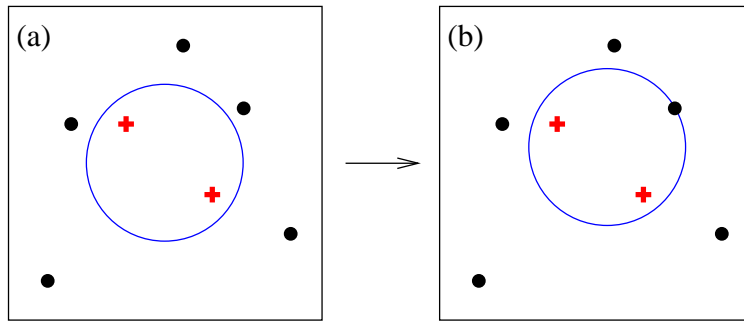
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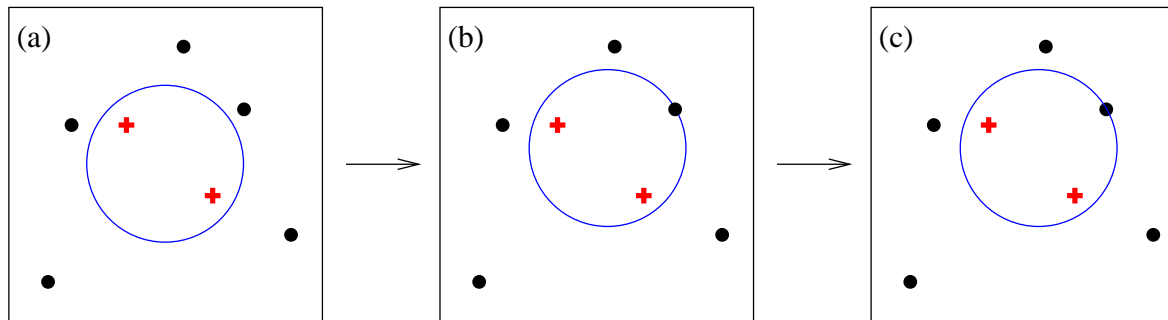
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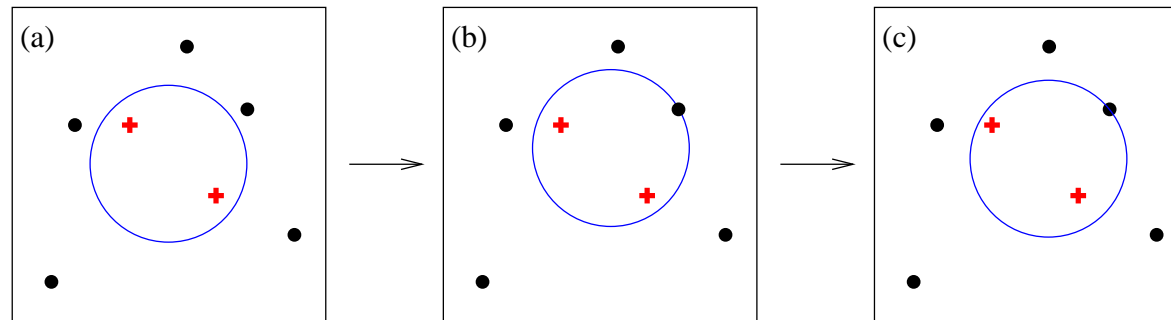


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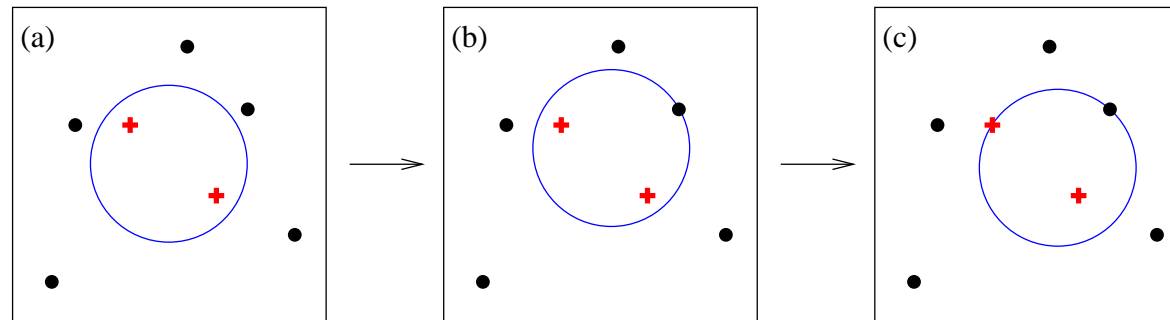
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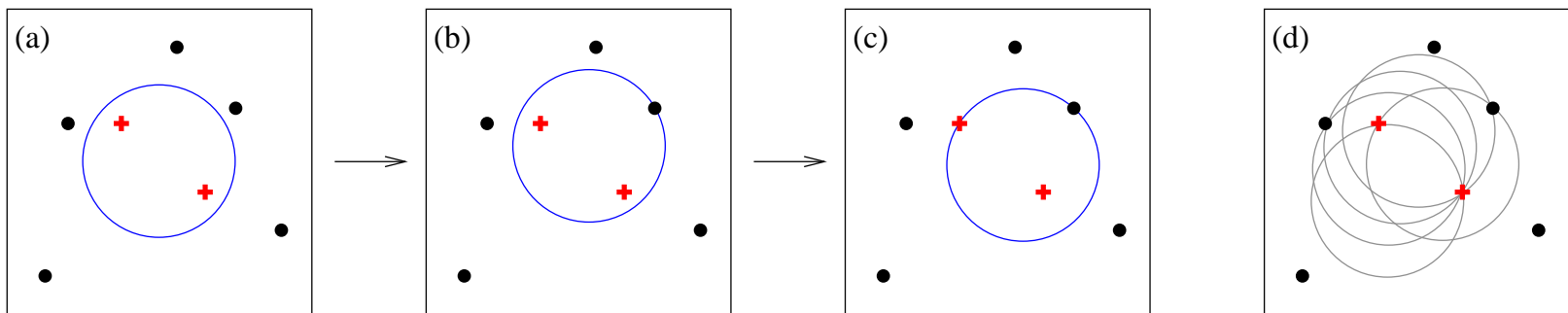
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with 2 circle orientations and 4 possible inclusion/exclusion  
→ find all enclosures

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- Enumerate all pairs of particles:  $\mathcal{O}(Nn)$
- For each, build content and check stability  
⇒  $\mathcal{O}(N^2n)$

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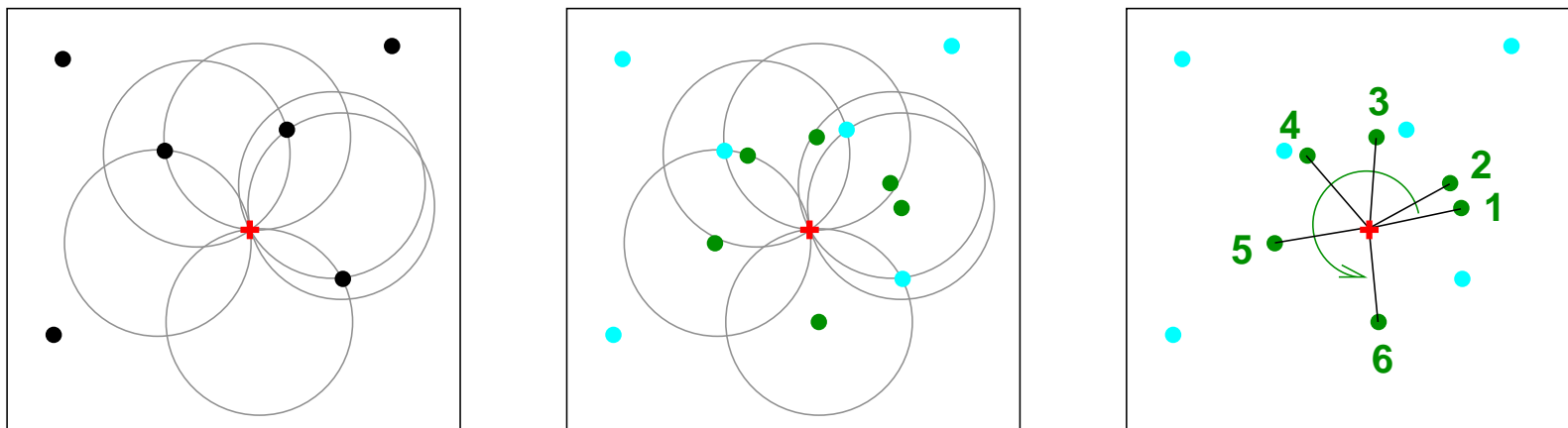
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Same as midpoint... but we'll use more tricks:

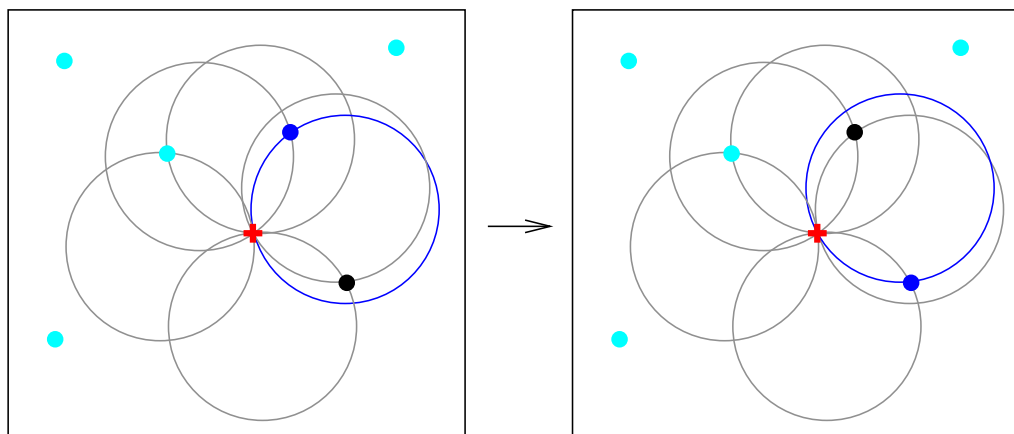
- avoid systematic recomputation of cone contents
- limit complete tests of cone stability

## Tricks:

- For all enclosures around a particle, introduce a **traversal order**



From one cone to the next one, contents only changed by “border” particles



⇒ avoids recomputing the cone contents at each step

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- For all enclosures around a particle, introduce a **traversal order**  
⇒ avoids recomputing the cone contents at each step
- Label the particles using a  **$q$ -bit tag**  
⇒ checkxor to identify distinct cones  
Introduces a potential “collision” problem

$$q = 96 \quad \Rightarrow \quad P(\text{collision}) = 10^{-18}$$



## Tricks:

- For all enclosures around a particle, introduce a **traversal order**  
⇒ avoids recomputing the cone contents at each step
- Label the particles using a  **$q$ -bit tag**  
⇒ checkxor to identify distinct cones
- Only **test “border particles” for stability (cost  $\mathcal{O}(1)$ )**  
⇒ **limits the number of full stability test to  $\mathcal{O}(N)$**   
checkxor → keep trace of stability tests

## How to efficiently determine all stable cones:

- For each particle  $i$ 
  - get “partners” and associated cone centres
  - order them by angle
  - build the first candidate cone contents
  - for all those candidates
    - check stability w.r.t. border particles
      - 4 possible  $\in$  or  $\notin$  & keep track of tested cones
    - move to the next cone
- Full stability test for the  $\mathcal{O}(N)$  not-yet-unstable candidates

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- For each particle  $i$ 
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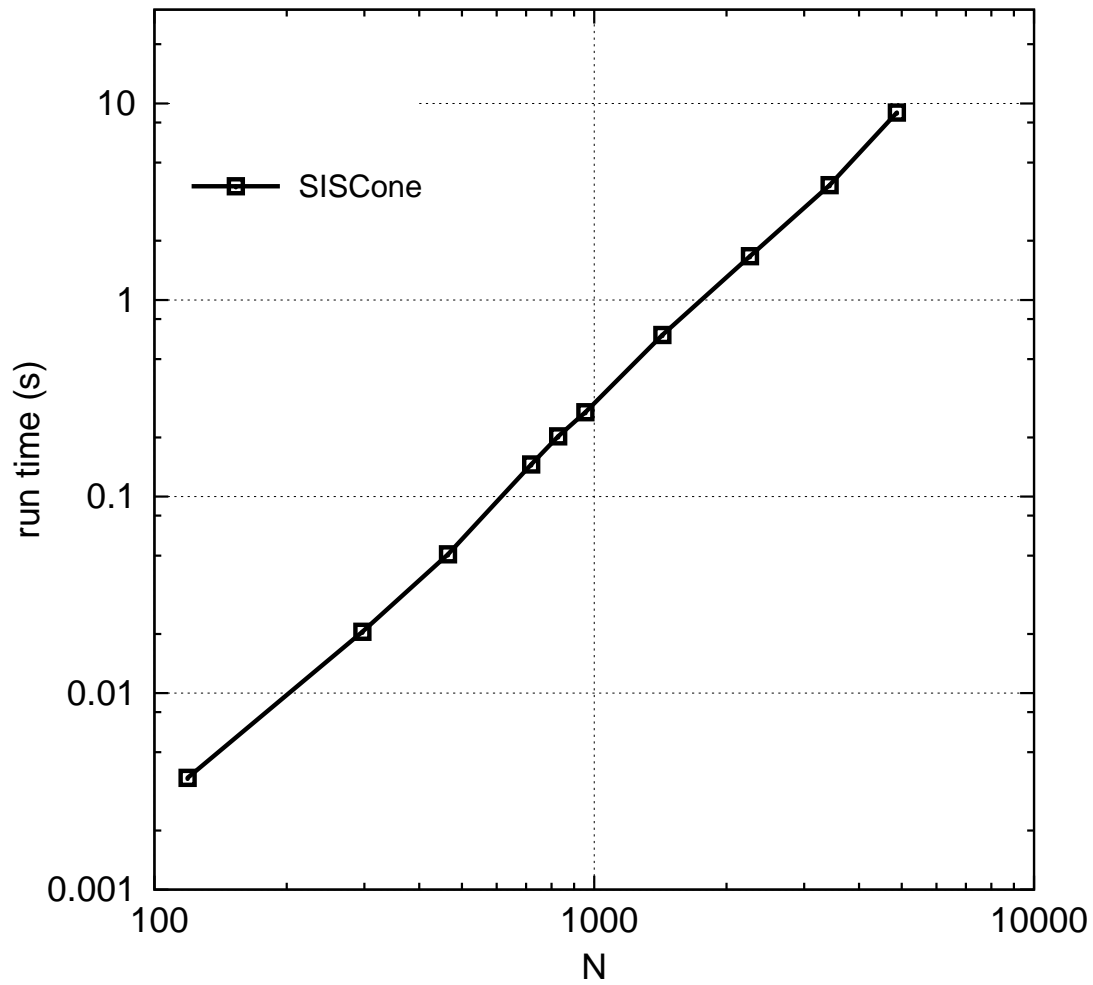
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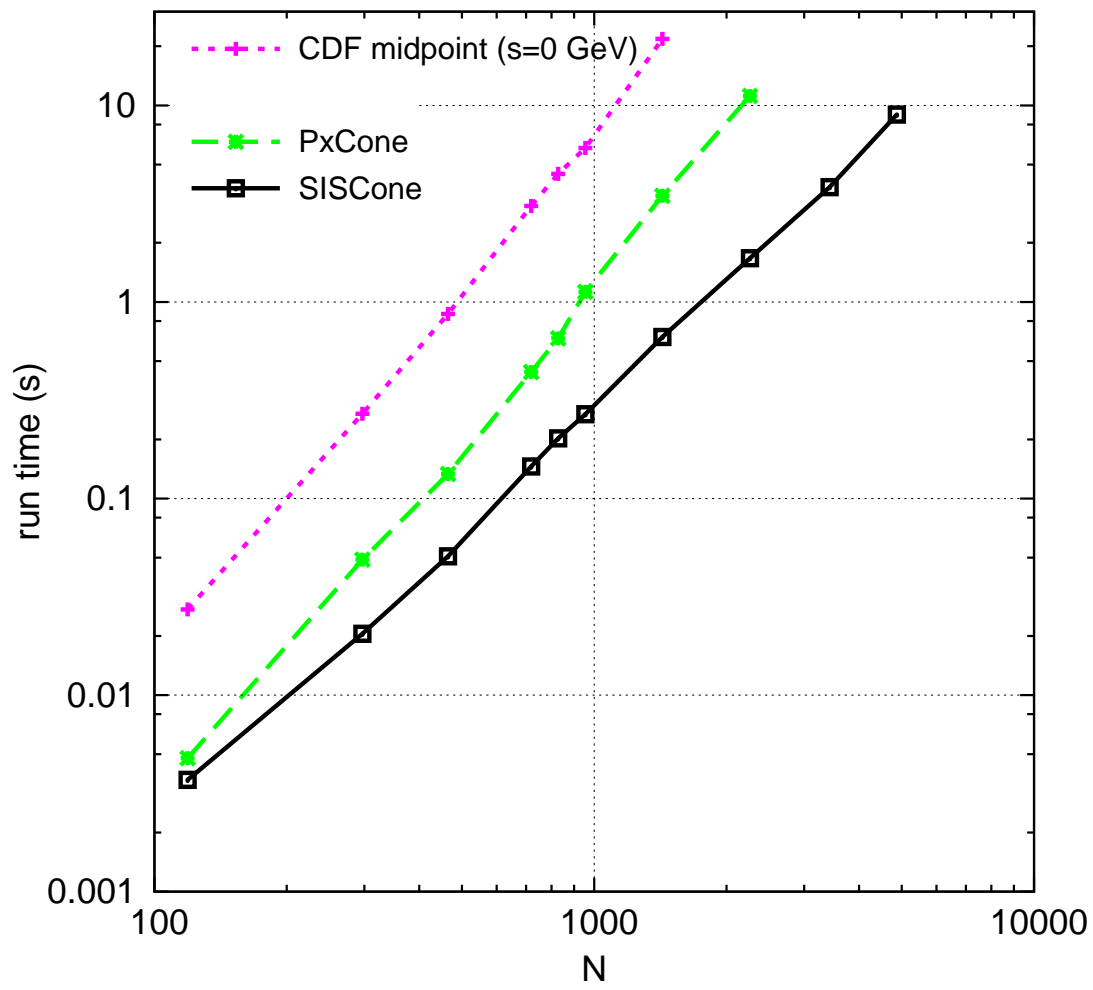
$\mathcal{O}(Nn \log(n))$


All stable cones found in  $\mathcal{O}(Nn \log(n))$

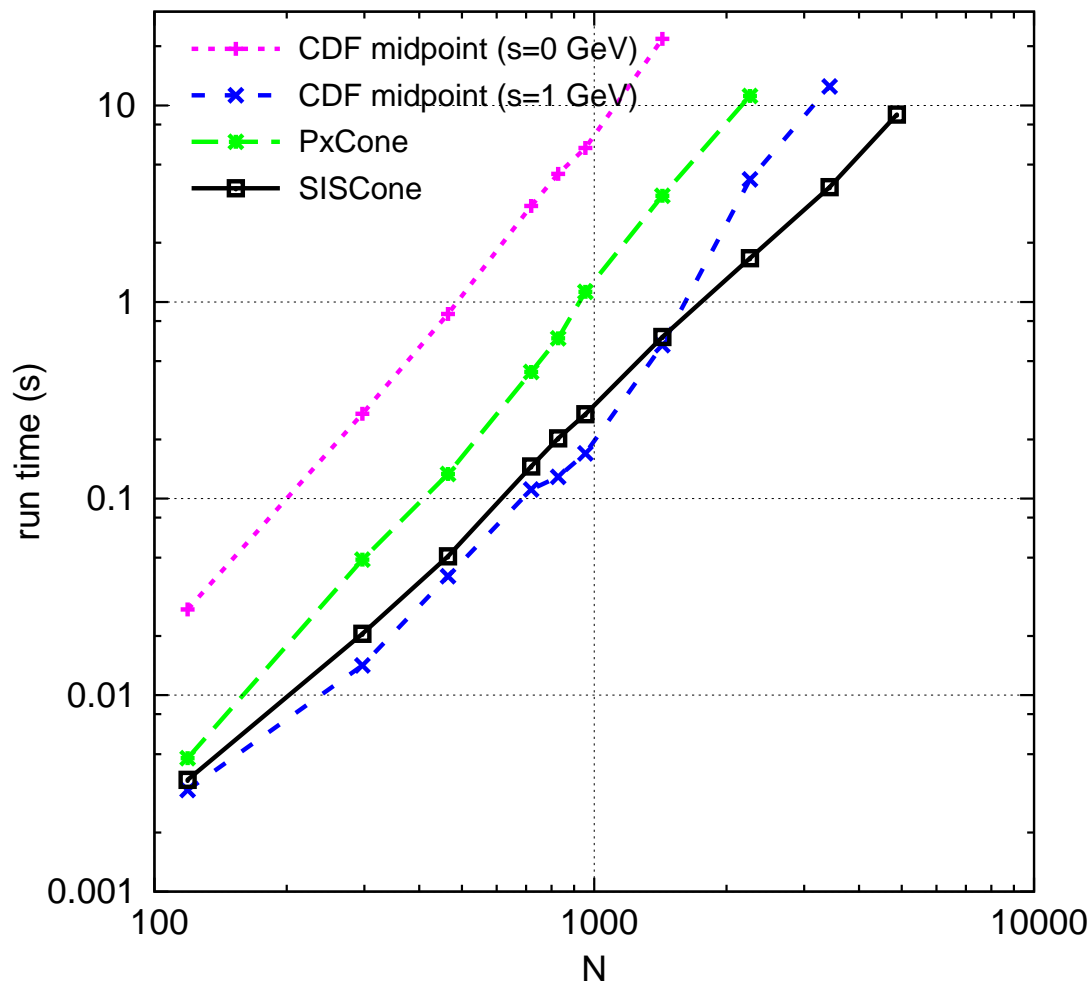
# ***SISCone vs. other cone algorithms***

***implications of a seedless cone***



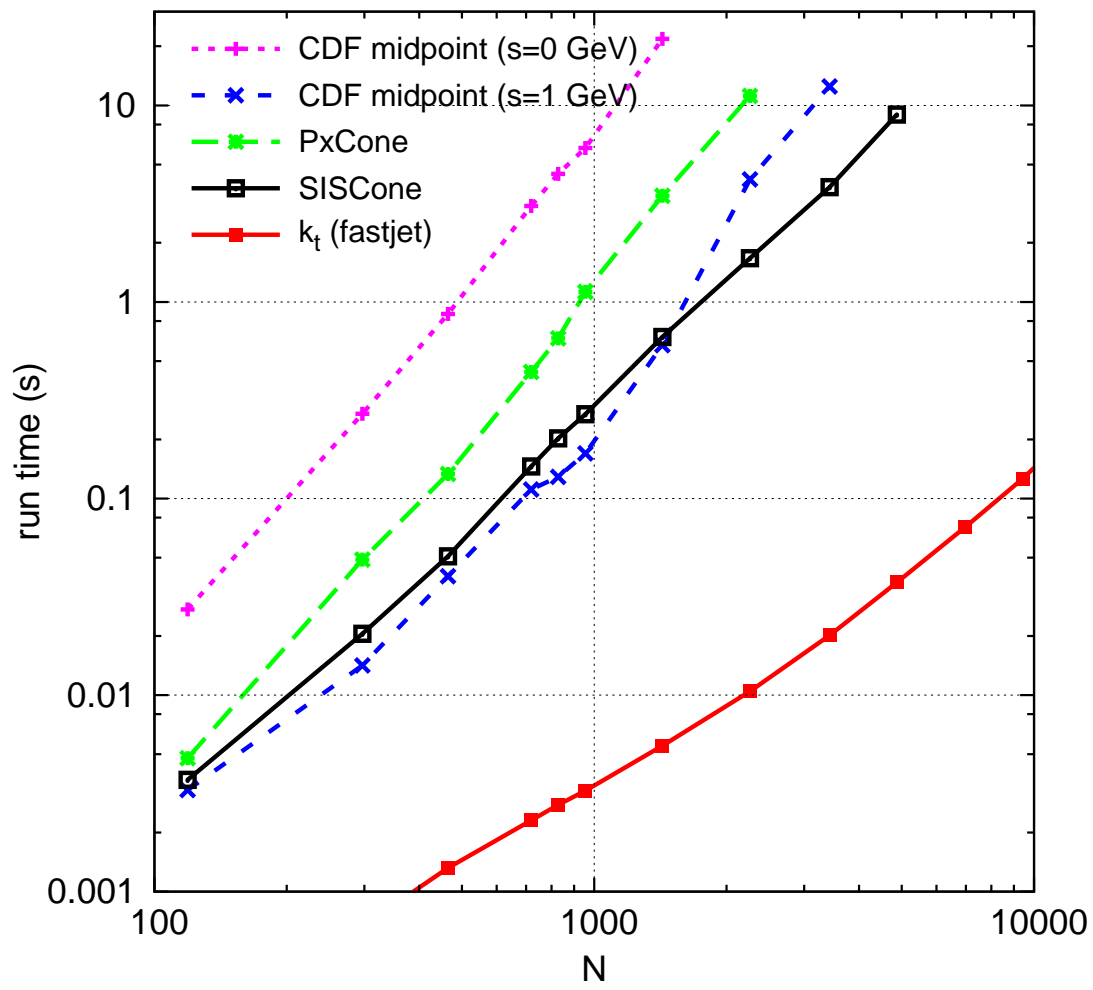


 faster than midpoint  
with no seed threshold  
and IR safe



- faster than midpoint with no seed threshold and IR safe
- same as midpoint with 1 GeV seed and collinear safe



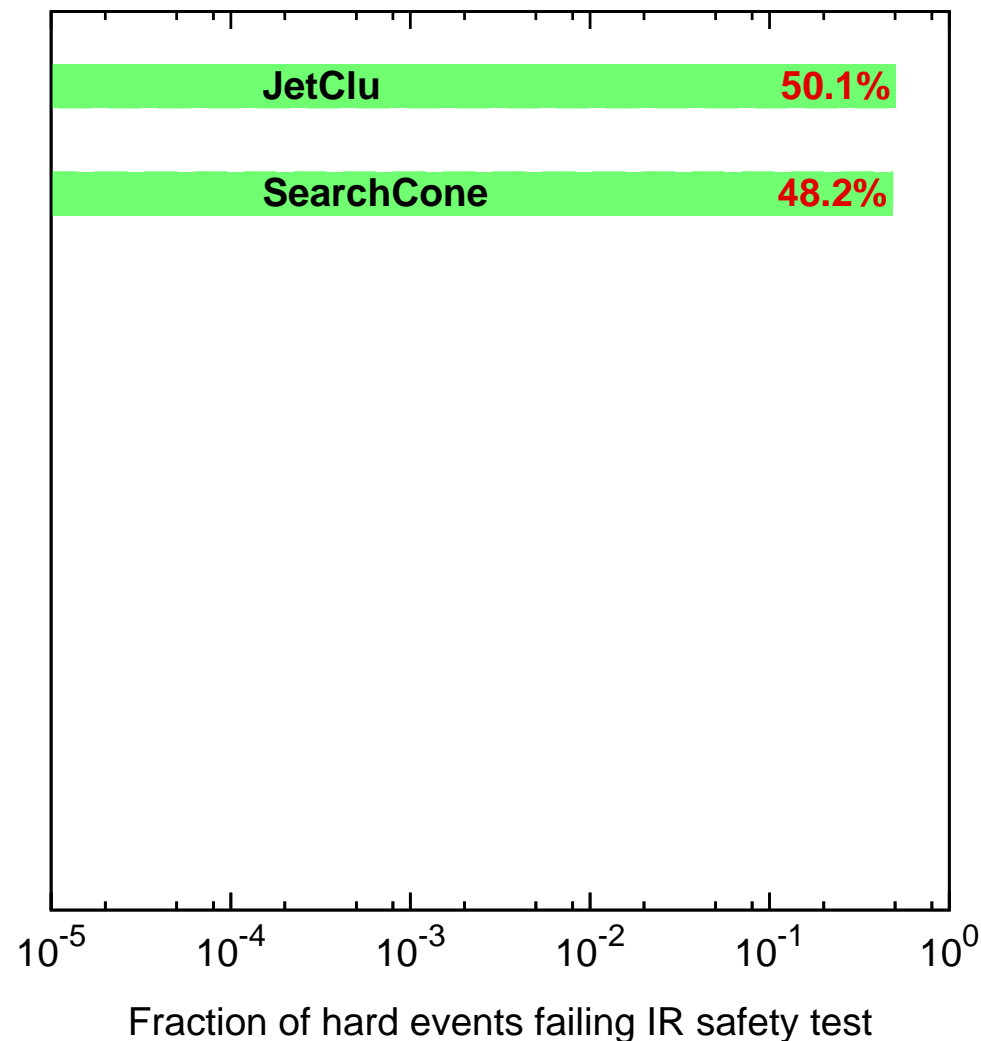


- faster than midpoint with no seed threshold and IR safe
- same as midpoint with 1 GeV seed and collinear safe
- slower than  $k_t$ /FastJet affordable for practical usage e.g. at the LHC

- Hard event: 2-10 particles
- Soft add-on: 1-5 particles
- Run:
  - “hard” only
  - many “hard+soft” trials
  - Search differences

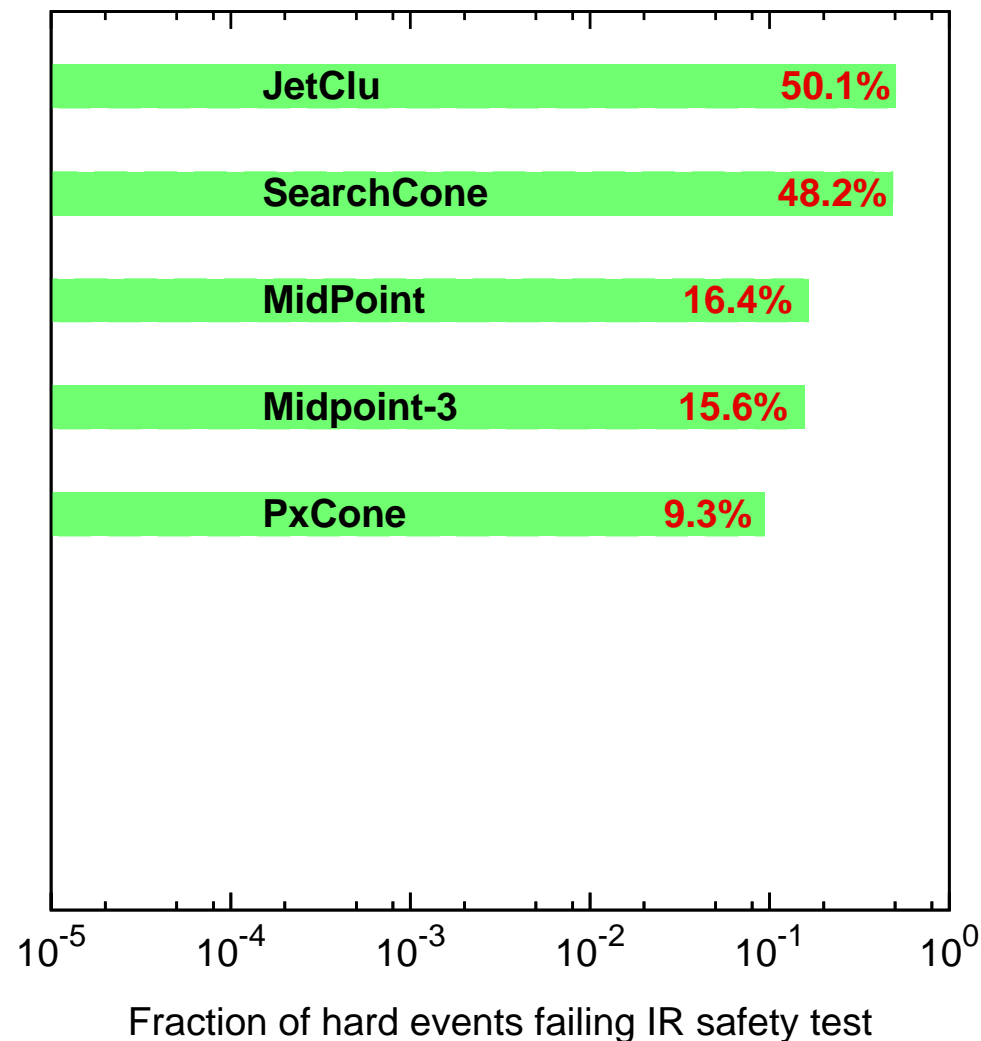
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Unsafety level	failure rate
2 hard + 1 soft	~ 50%



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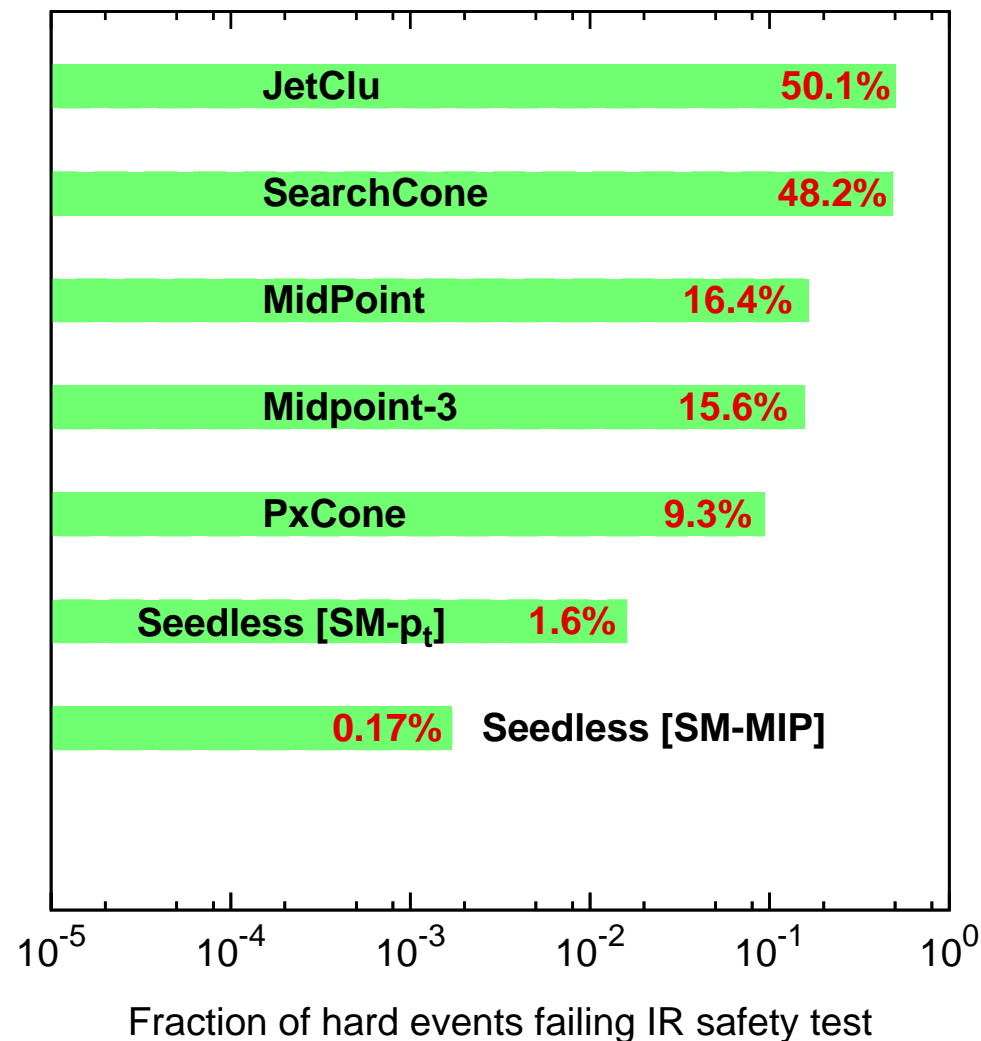
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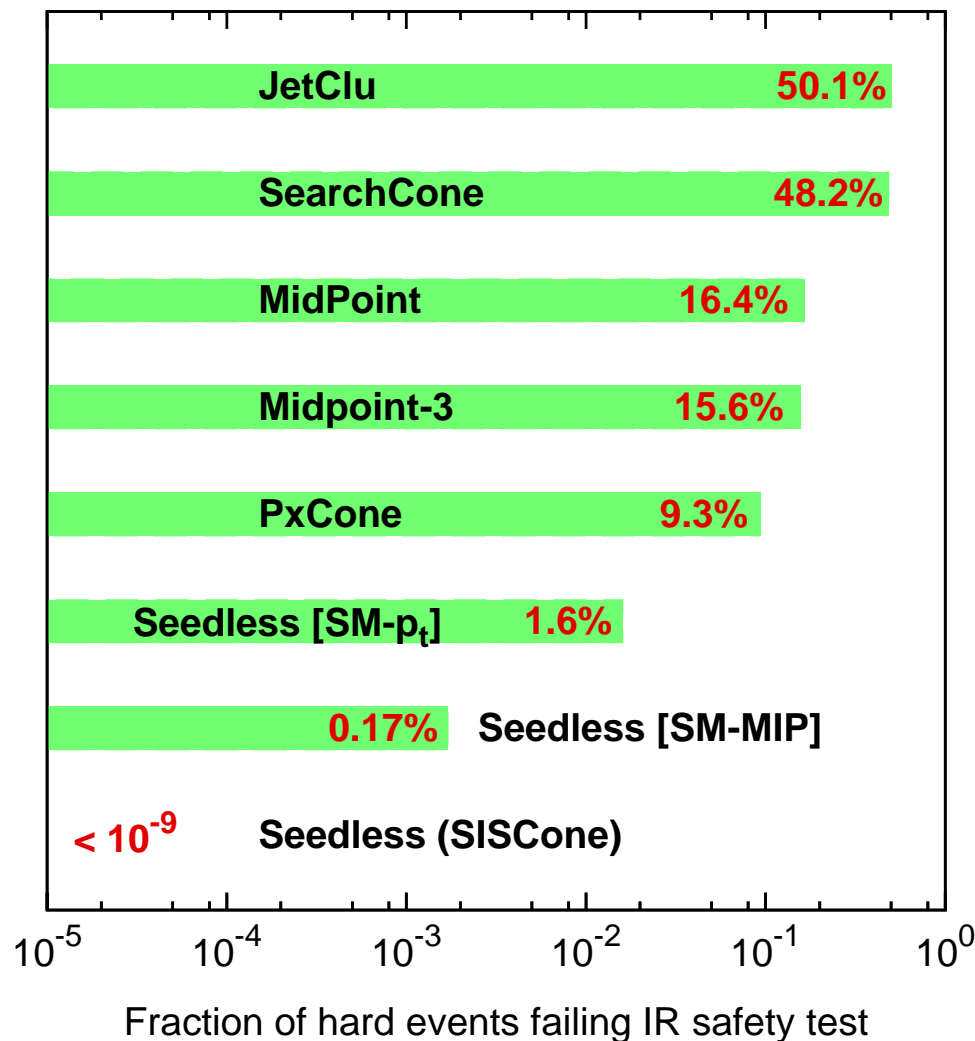
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<b>SISCone</b>	<b>IR safe !</b>

NB: small issues in the split-merge

Physical impact: SISCone vs. midpoint( $s$ ) ?

IR unsafety of midpoint: 3 particles in the same vicinity + 1 to balance  $p_t$   
 $\Rightarrow$  starts at the  $2 \rightarrow 4$  level ( $\mathcal{O}(\alpha_s^4)$ )

Observable	1st miss cones at	Last meaningful order
Inclusive jet cross section	NNLO	NLO
$W/Z/H + 1$ jet cross section	NNLO	NLO
3 jet cross section	NLO	LO
$W/Z/H + 2$ jet cross section	NLO	LO
jet masses in 3 jets	LO	none
masses in $W/Z/H + 2$ jets	LO	none

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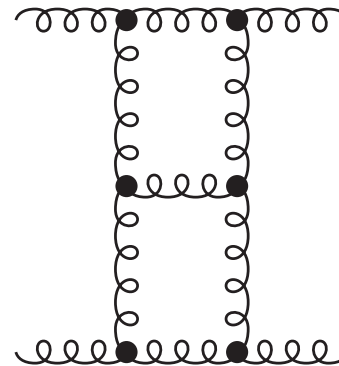
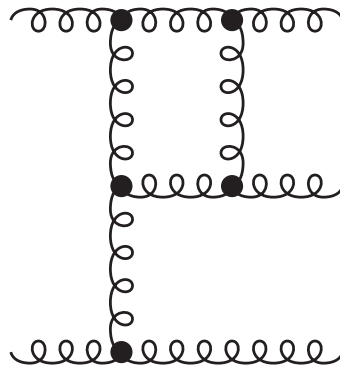
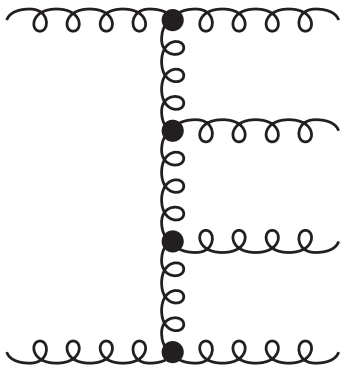
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jet masses in 3 jets	LO	none
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The IR-unsafety issue will matter at LHC



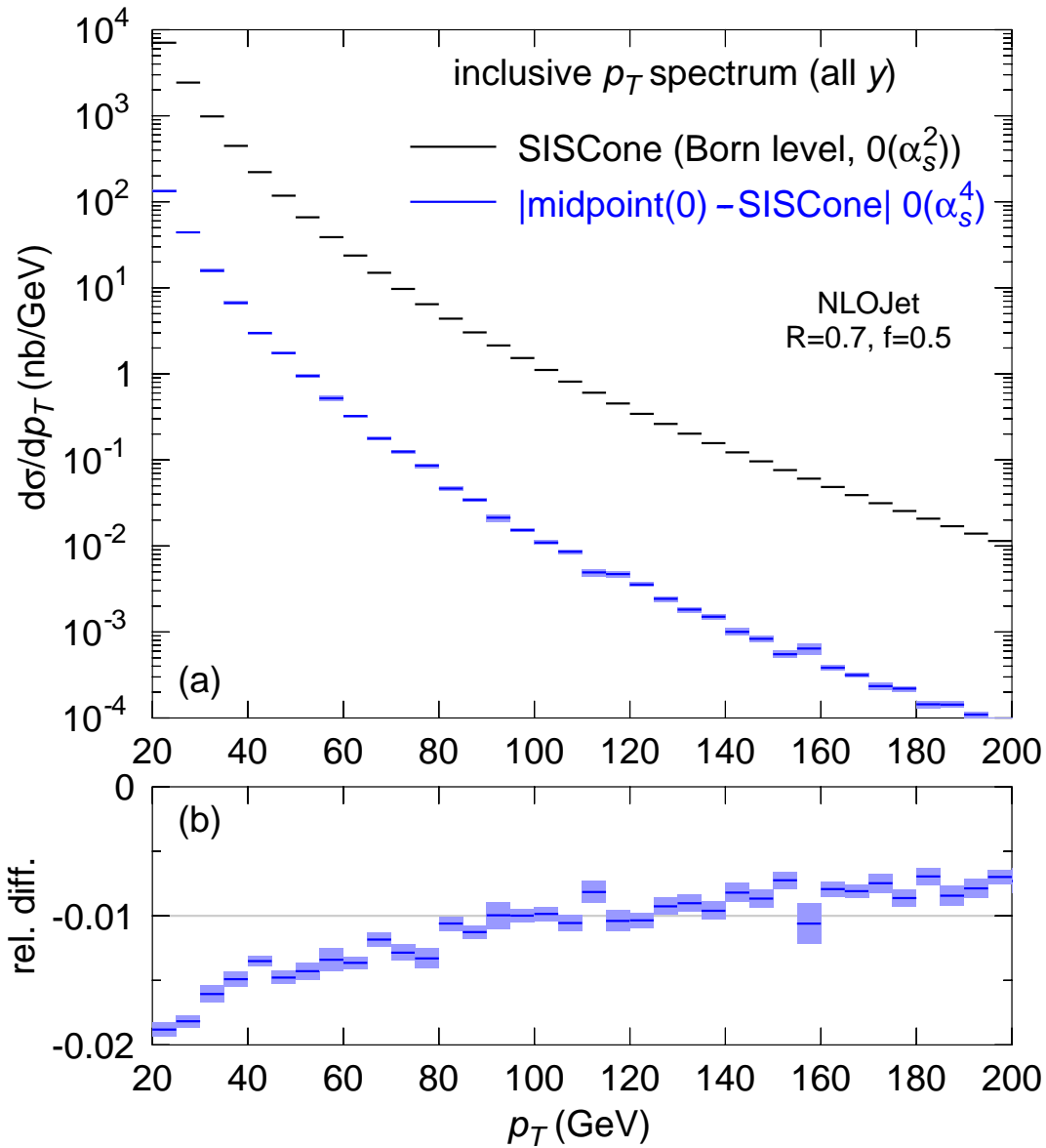
## SISCone vs. midpoint( $s$ ) in inclusive jet spectrum?

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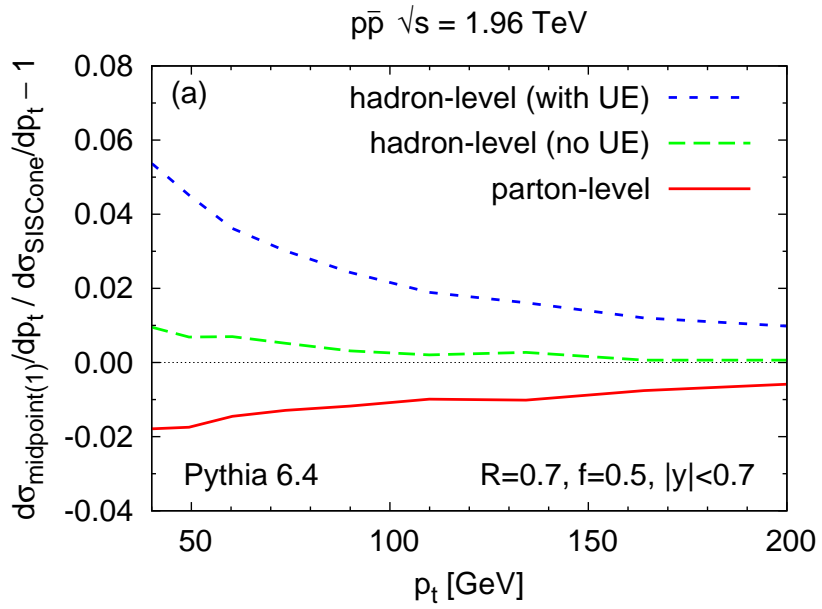
- IR unsafety of midpoint: 3 particles in the same vicinity + 1 to balance  $p_t$   
 $\Rightarrow$  starts at the  $2 \rightarrow 4$  level ( $\mathcal{O}(\alpha_s^4)$ )
  - 3 contributions at this order:  
 $2 \rightarrow 4$  at LO (tree),  $2 \rightarrow 3$  at NLO (1 loop) and  $2 \rightarrow 2$  at NNLO (2 loops)
  - $2 \rightarrow 4$  at LO is IR divergent  
BUT the difference between SISCone and midpoint( $s$ ) is finite since it is 0 at the  $2 \rightarrow 2$  and  $2 \rightarrow 3$  levels
- $\Rightarrow$  compute |SISCone-midpoint( $s$ )| for  $2 \rightarrow 4$  diagrams
- Compare with the  $2 \rightarrow 2$  (LO) spectrum to estimate effect



Differences of order 1-2 %

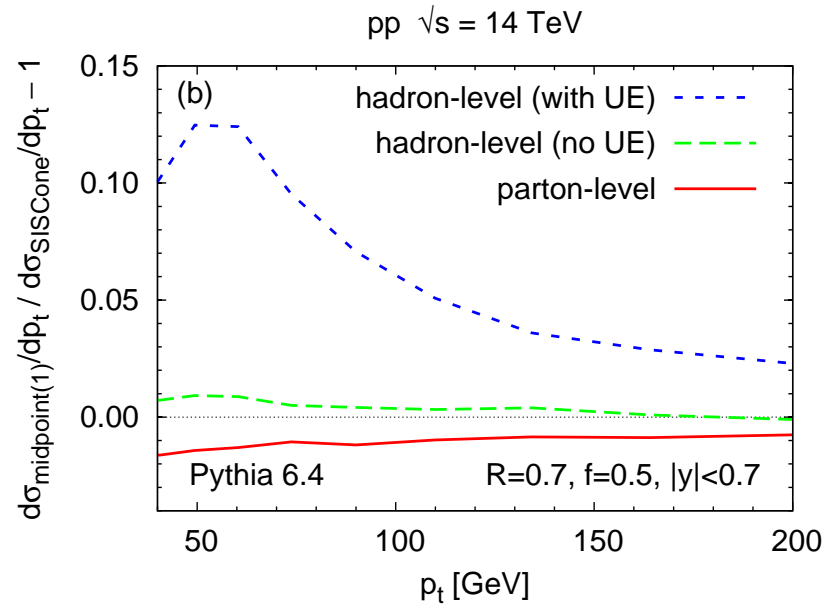
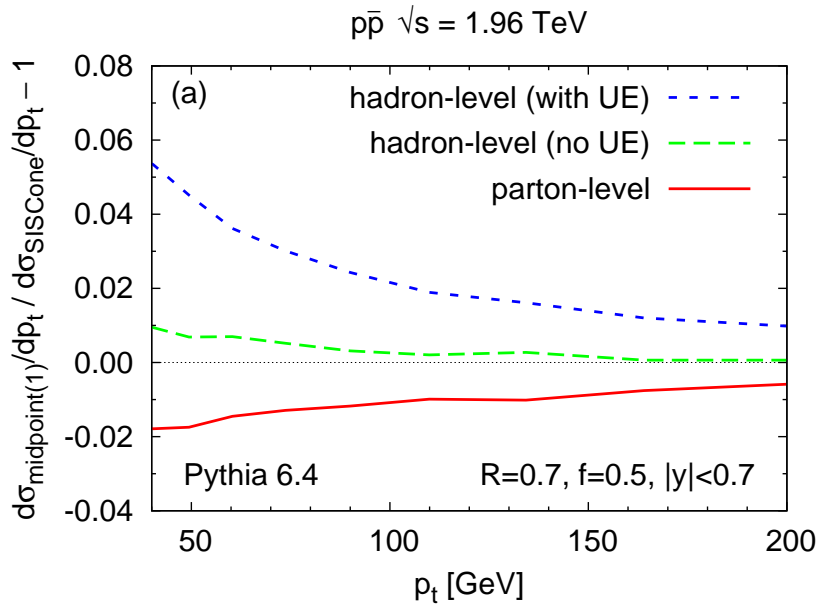
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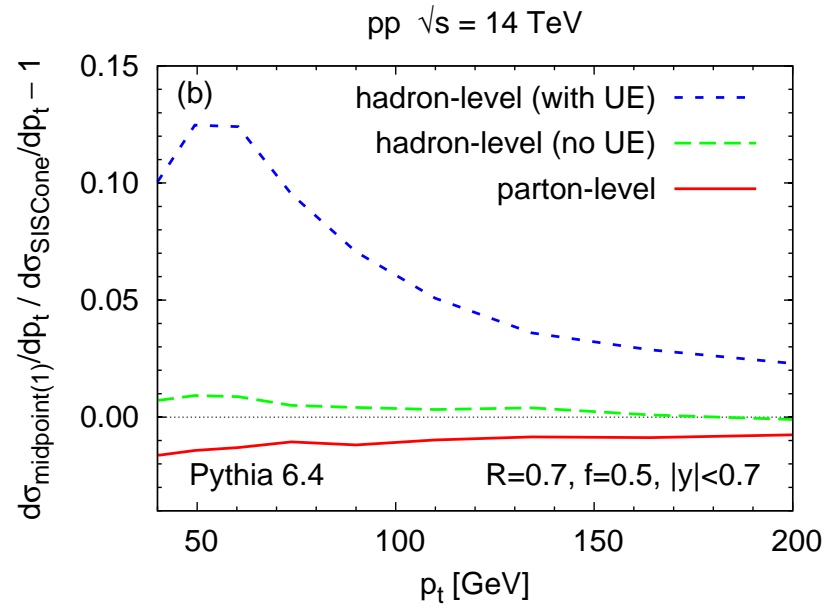
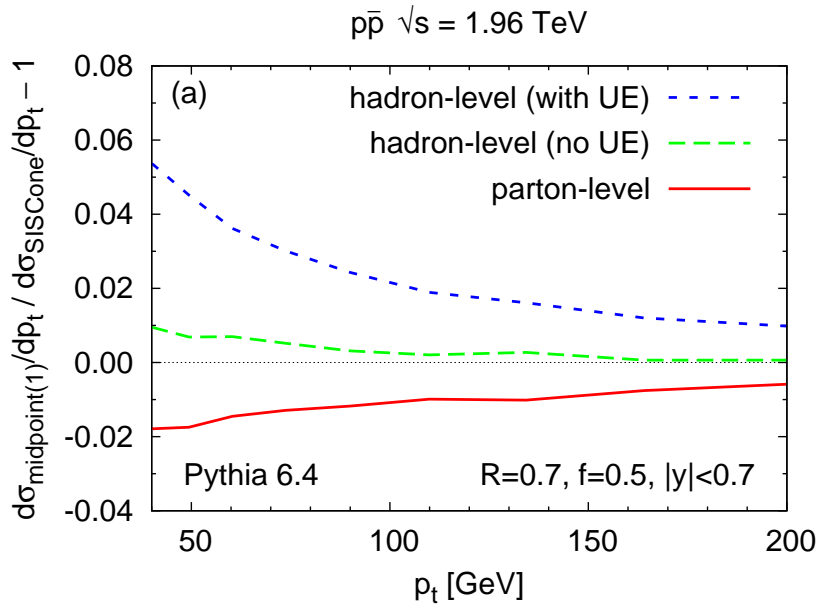
## Ratio midpoint/SISCone-1:



- Differences up to 5% (with a change of sign)
- Raise up to 10% at LHC energy!

Including parton shower, hadronic corrections and/or underlying event:

## Ratio midpoint/SISCone-1:



- Differences up to 5% (with a change of sign)
- Raise up to 10% at LHC energy!
- Less effect from underlying event in SISCone (i.e. better agreement with parton level)

## Inclusive jet spectrum

→ effect at NNLO i.e.  $\mathcal{O}(\alpha_s^2)$  w.r.t. LO

⇒ want to look at more exclusive processes

## Example: mass spectrum in 3-jet events (or W/Z/H+2j)

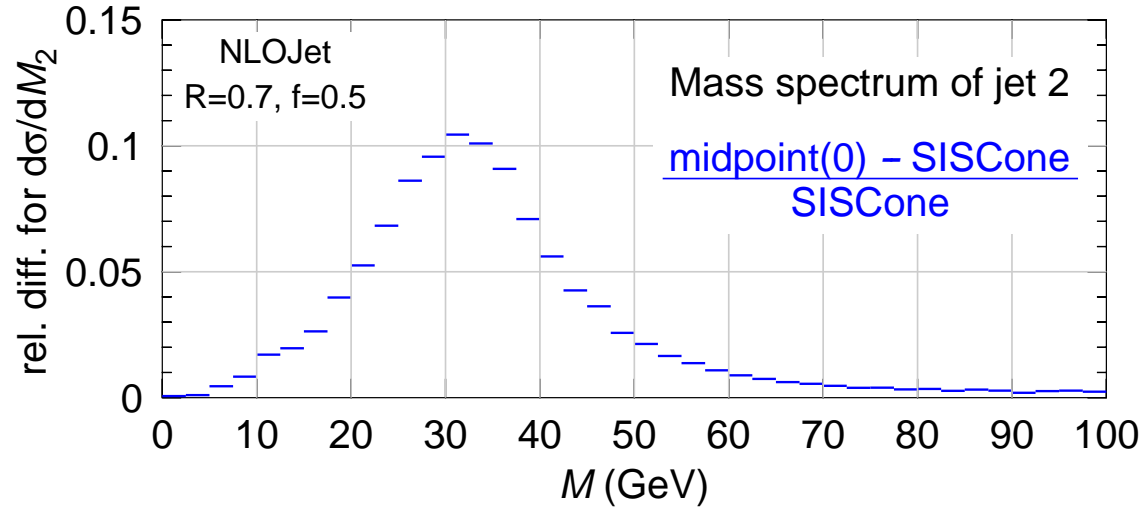
$$\left. \begin{array}{l} 2 \rightarrow 2 \text{ has only 2 jets} \\ 2 \rightarrow 3 \text{ has zero masses} \end{array} \right\} \Rightarrow \text{first contribution from } 2 \rightarrow 4$$

⇒ Expect modifications at LO!

Ratio  $\frac{\text{midpoint-SISCone}}{\text{SISCone}}$  for masses spectra in 3-jet events

cuts:  $p_{t,1} \geq 120 \text{ GeV}$ ,  $p_{t,2} \geq 80 \text{ GeV}$ ,  $p_{t,3} \geq 40 \text{ GeV}$

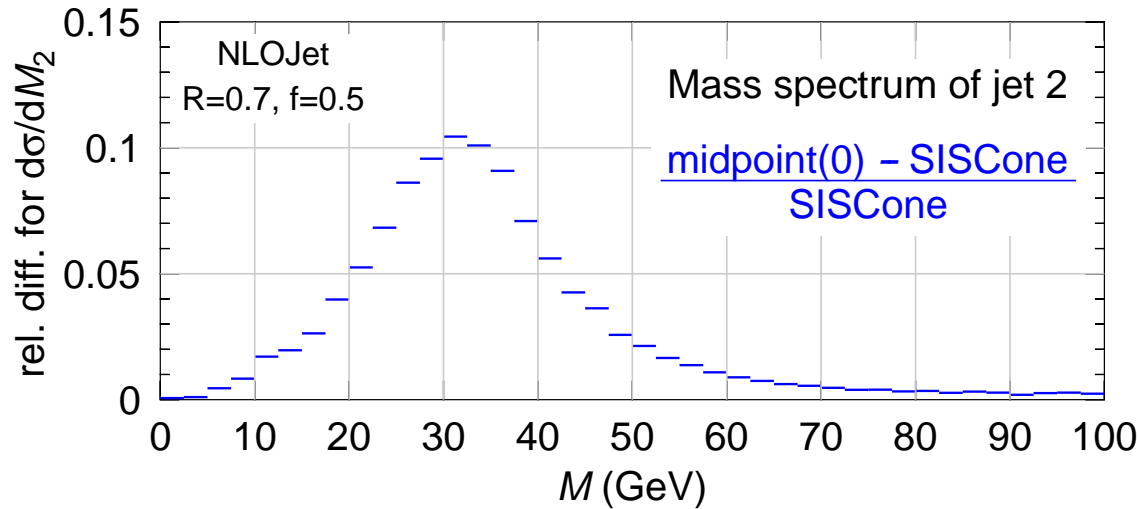
## 1. Fixed order computation (NLOJet, LO, $2 \rightarrow 4$ )



Differences up to 10 %

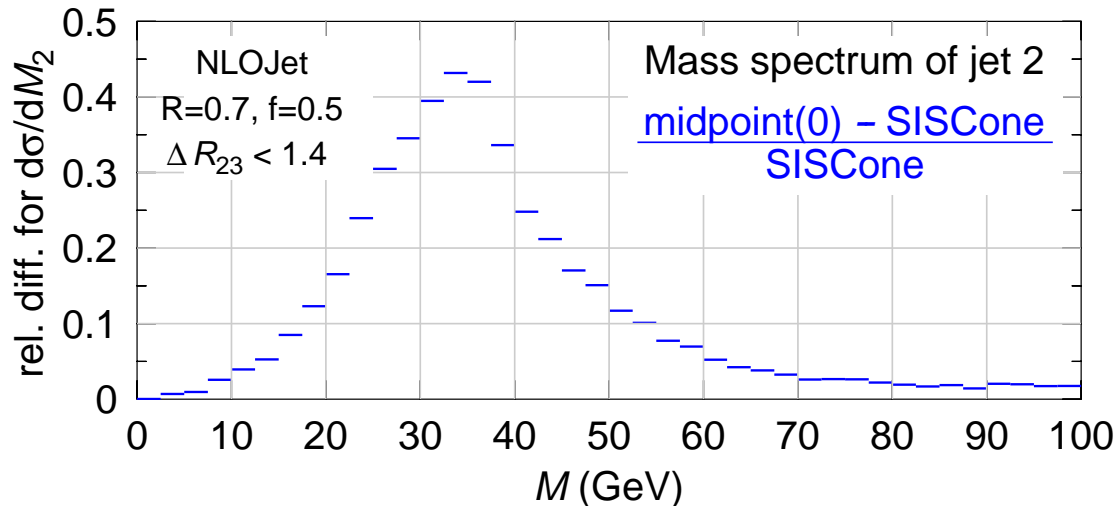


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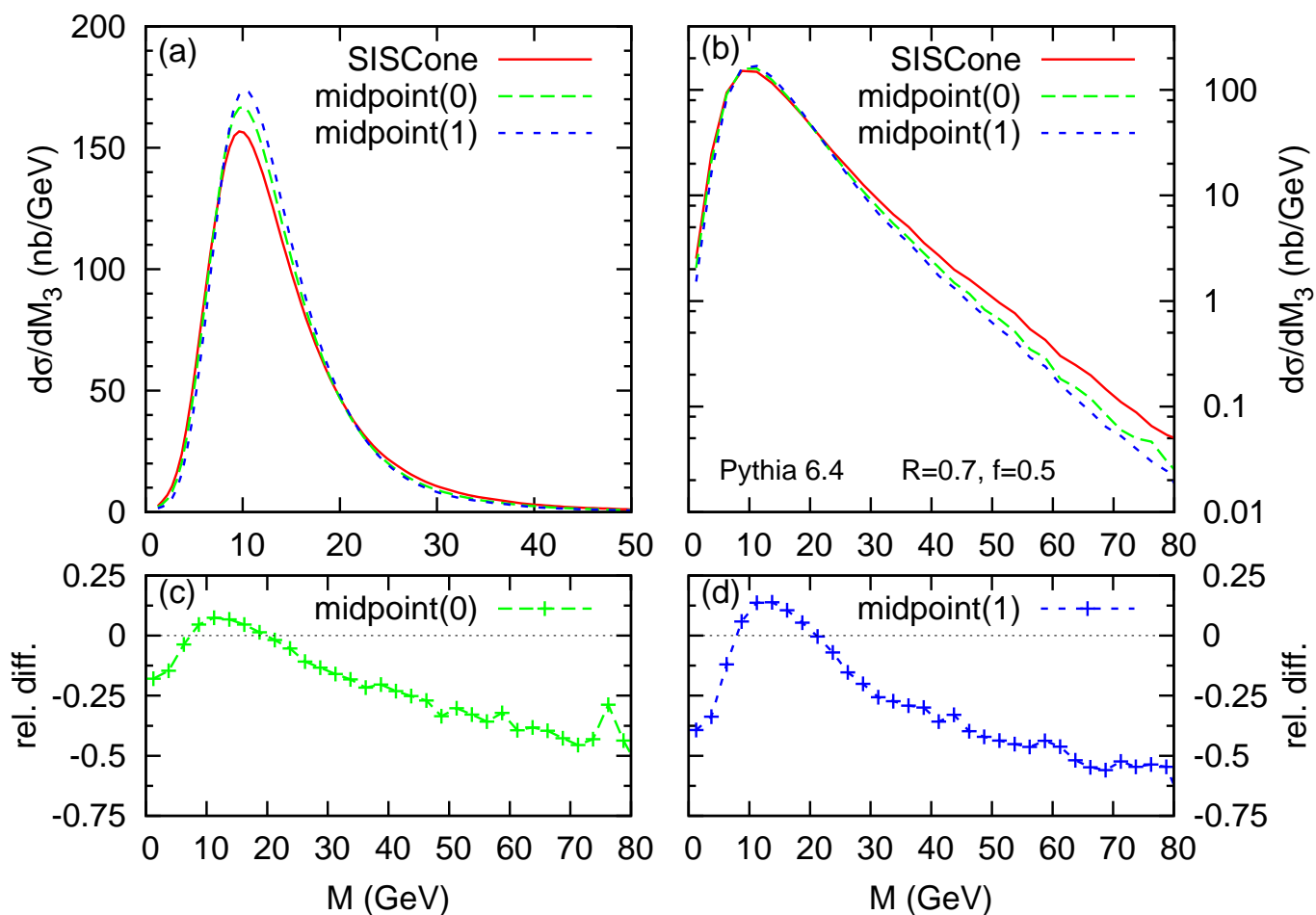
Differences up to 10 %

## 2. Also require jets 2 and 3 within distance $\leq 2R$



Differences up to 40 %

## 3. At hadron level (PYTHIA)



- ▷ Differences of order 10 %
- ▷ Larger effects in the tail
- ▷ seed threshold even worse

- Jets are present everywhere:  $k_t$  and cone are widely used
- seeded implementations are **IR unsafe** (sometimes **collinear unsafe**)  
IR safety is a prerequisite for perturbative QCD to make sense

We propose a [new cone algorithm](#) (SISCone):

- **IR safe** (and **collinear safe**)
- as **fast** as available cone implementations
- has **10% impact on jet mass spectra** (can be up to 40%)
- is **less affected by underlying events**

# *Jet area*

*Everyone has an idea of what a jet area is  
but can we define that properly?*

[M. Cacciari, G. Salam, G.S., in preparation]

[M. Cacciari, G. Salam, arXiv:0707.1378]

- Idea: add soft particle (**ghosts**)
  - with IR-safe algorithms such as  $k_t$ , **Aachen/Cambridge and SISCone**, clustering is unchanged
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add one ghost and look where it ends. repeat to cover the  $(y, \phi)$  plane

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also gives purely ghosted jets

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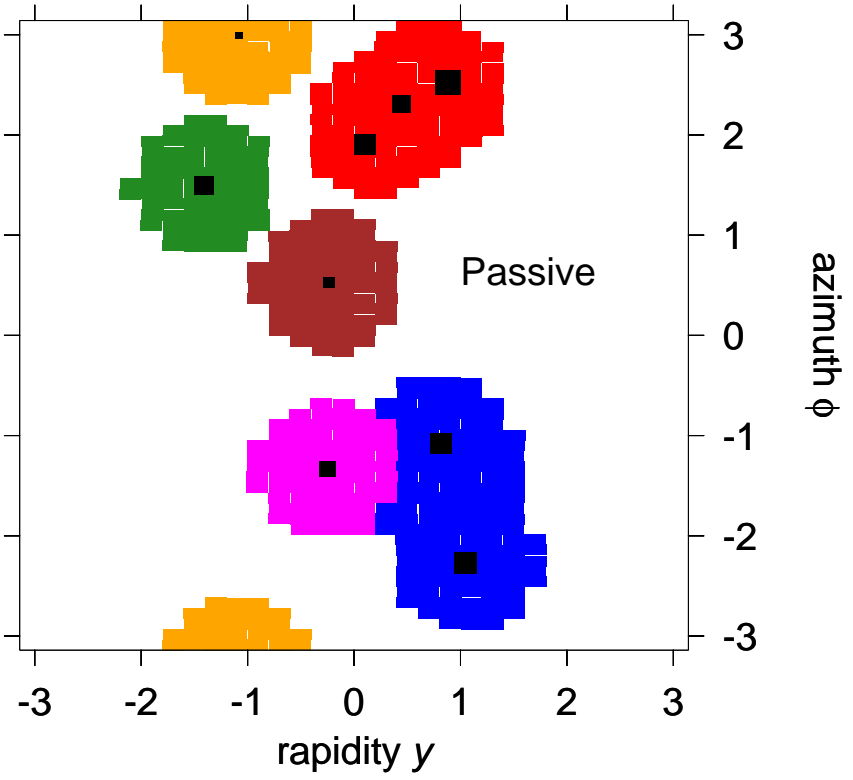
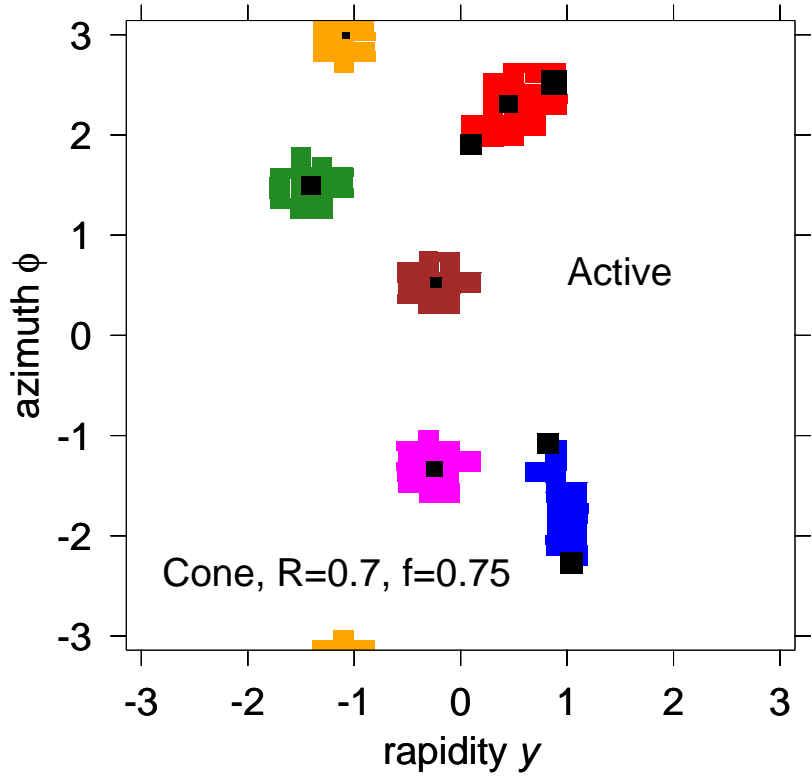
add one ghost and look where it ends. repeat to cover the  $(y, \phi)$  plane
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add a large amount of ghosts and cluster everything  
also gives purely ghosted jets
- Voronoi area

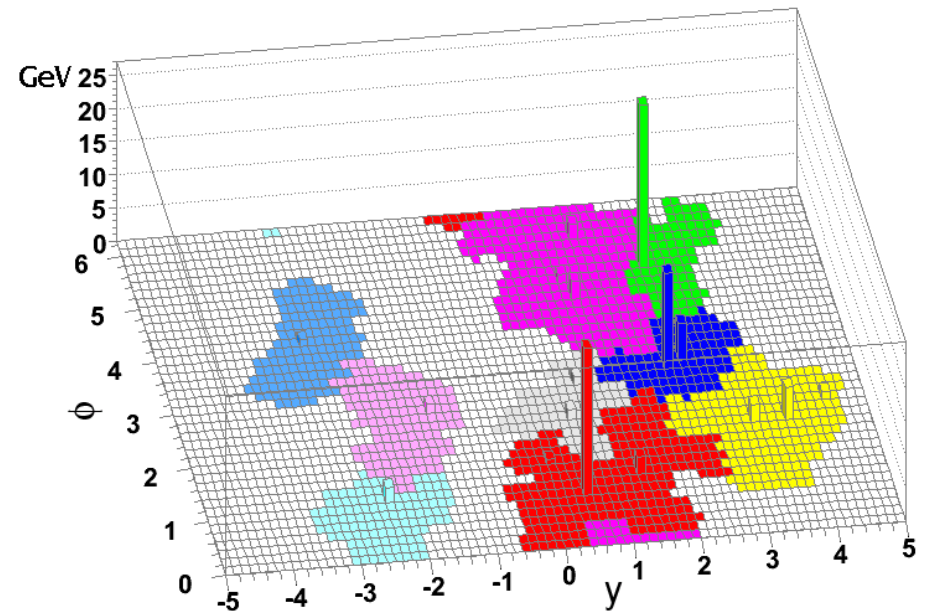
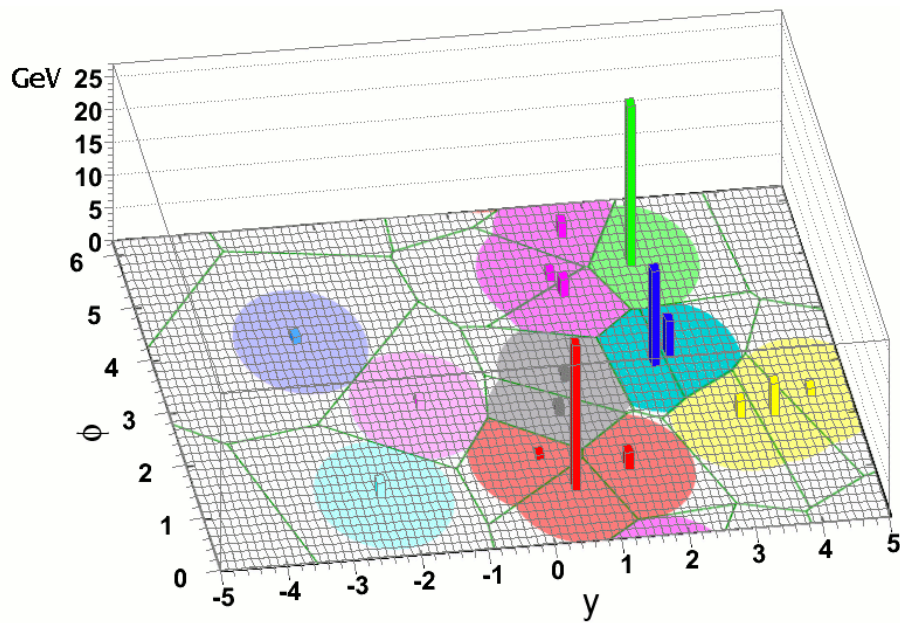
~ Area of the Voronoi cells



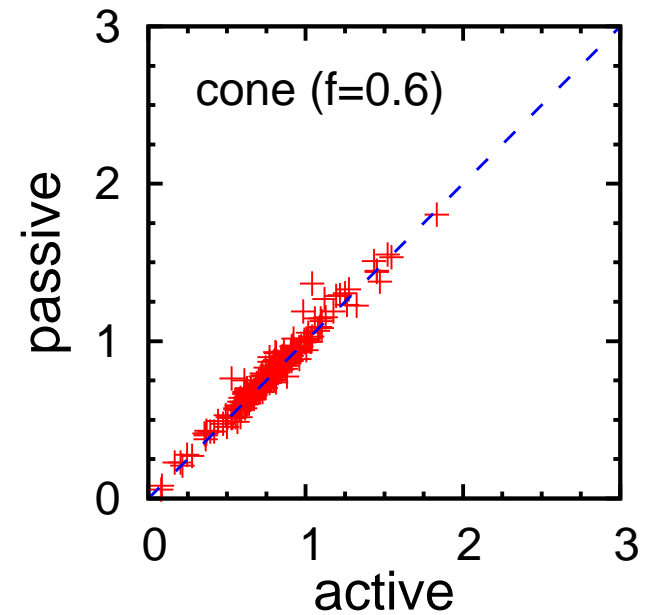
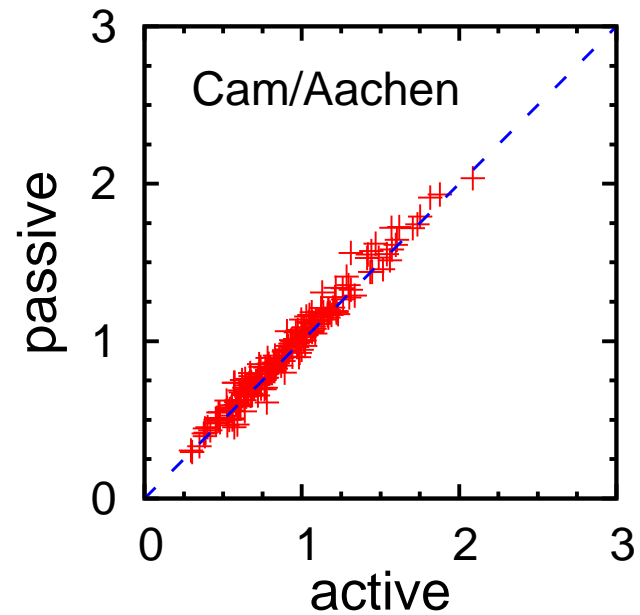
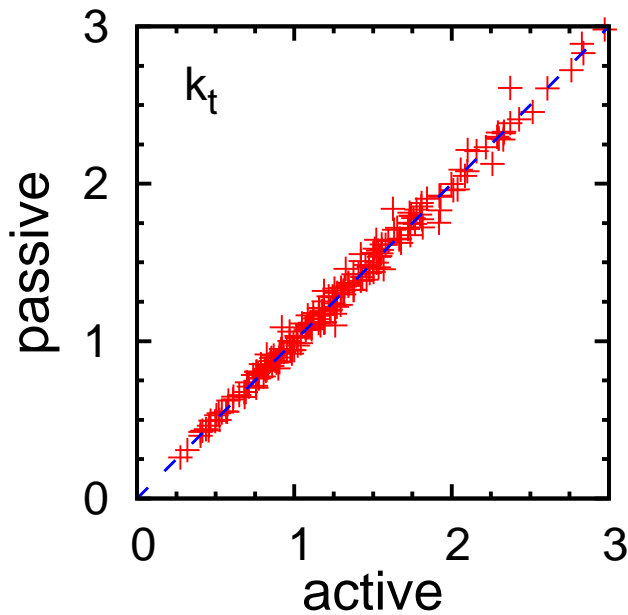
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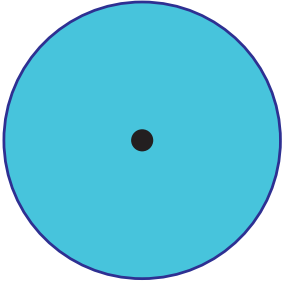
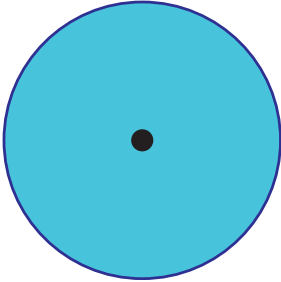
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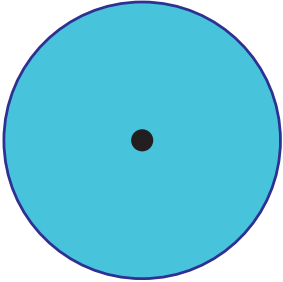
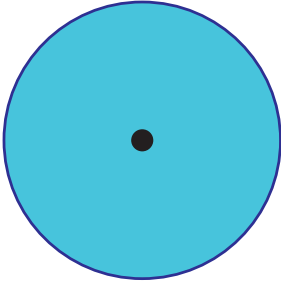
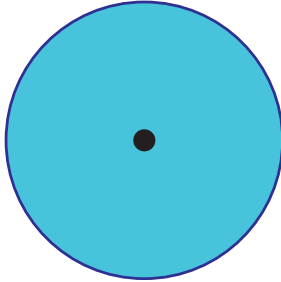
# Examples: 1-particle cases

	$k_t$	Aac/Cam	cone
Passive			
Active			

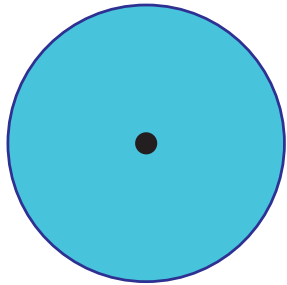
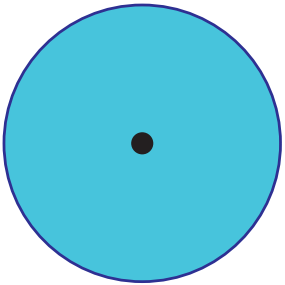
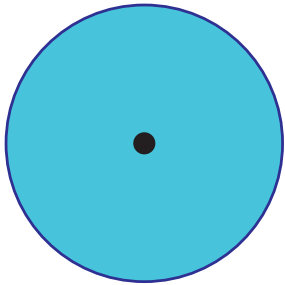
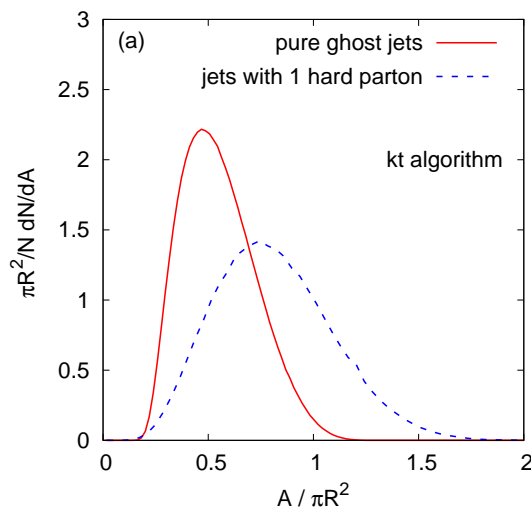
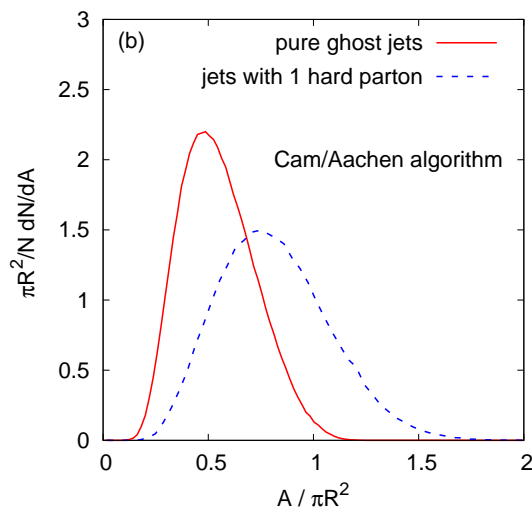
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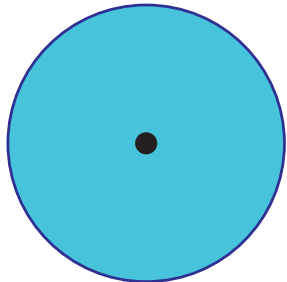
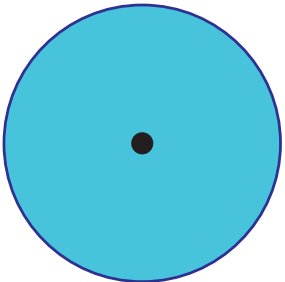
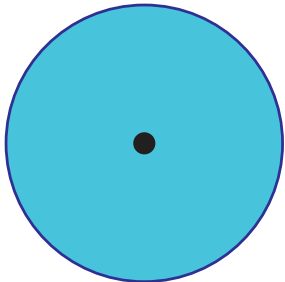
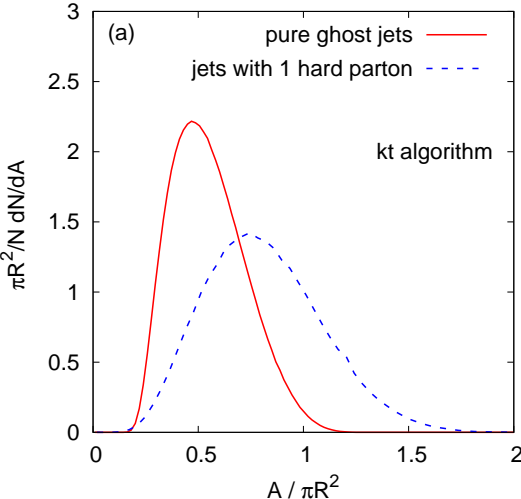
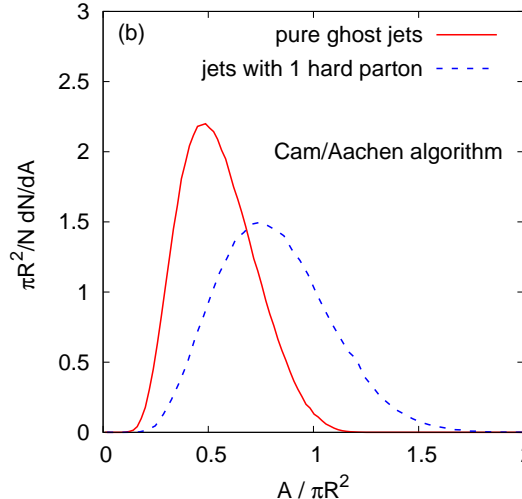
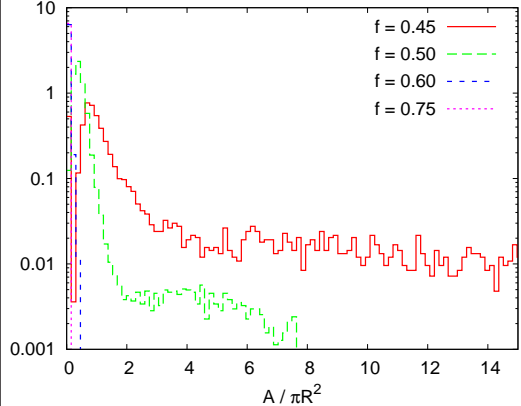
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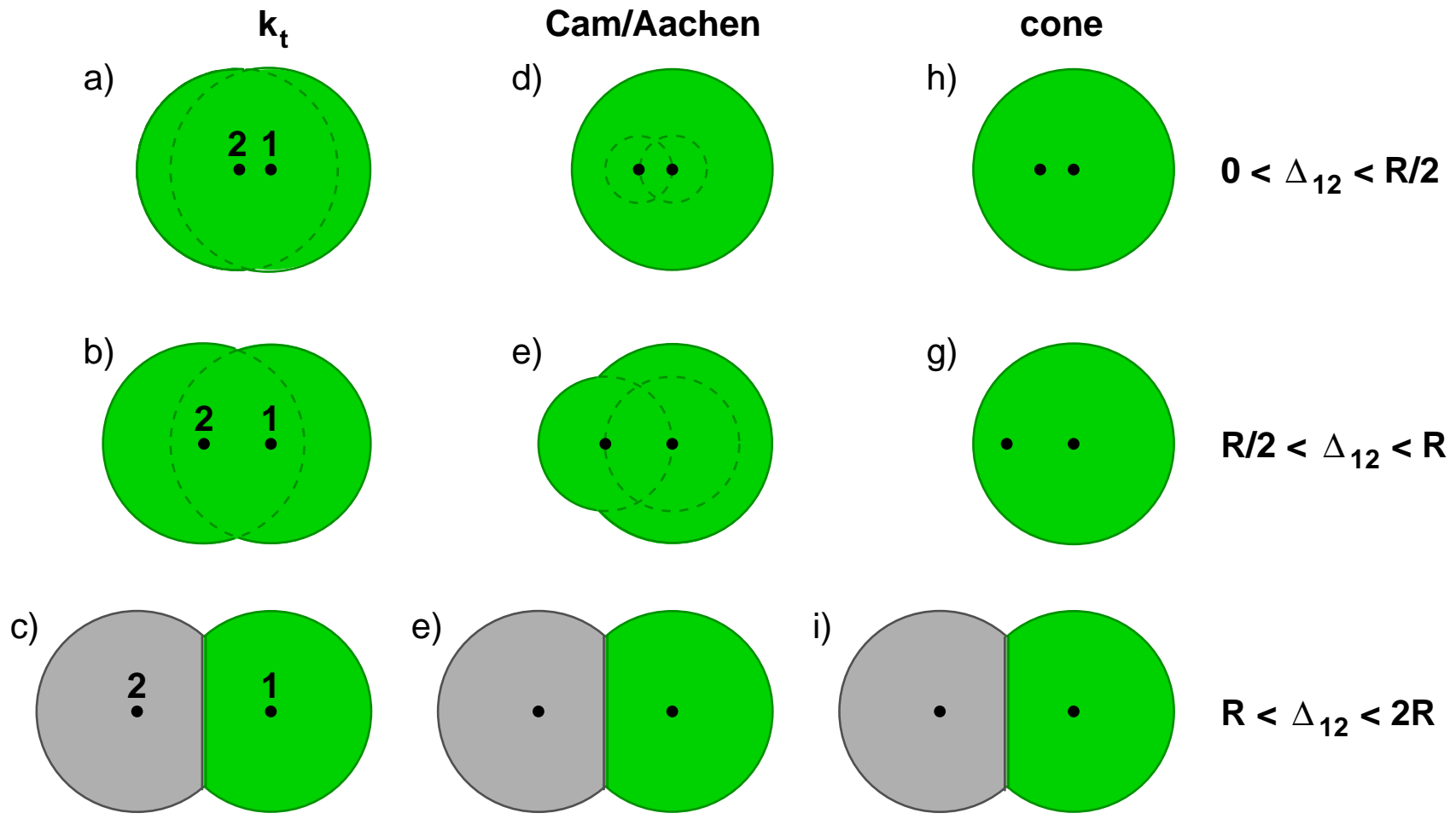
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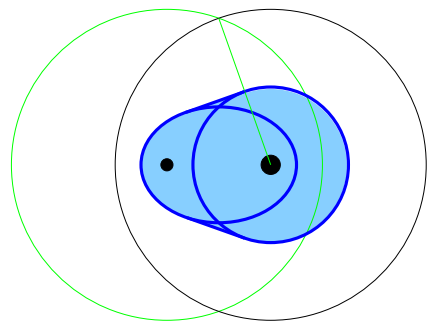
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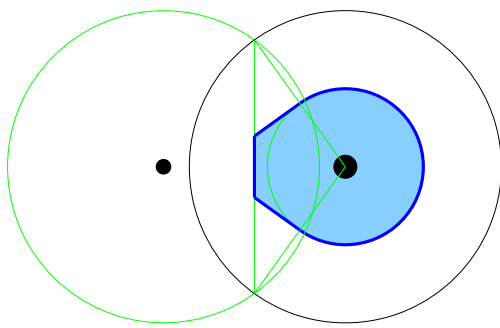
## Passive area: 1 hard particle + 1 soft



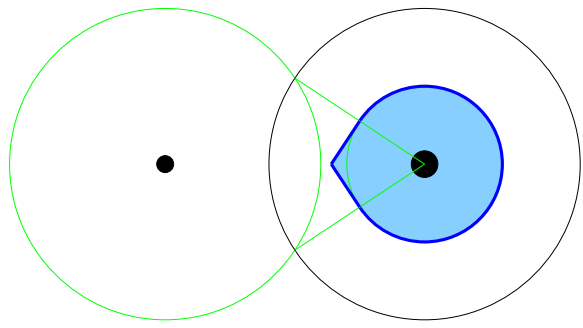
Active area: 1 hard particle + 1 soft: **analytic result for cone only**



$d < R$

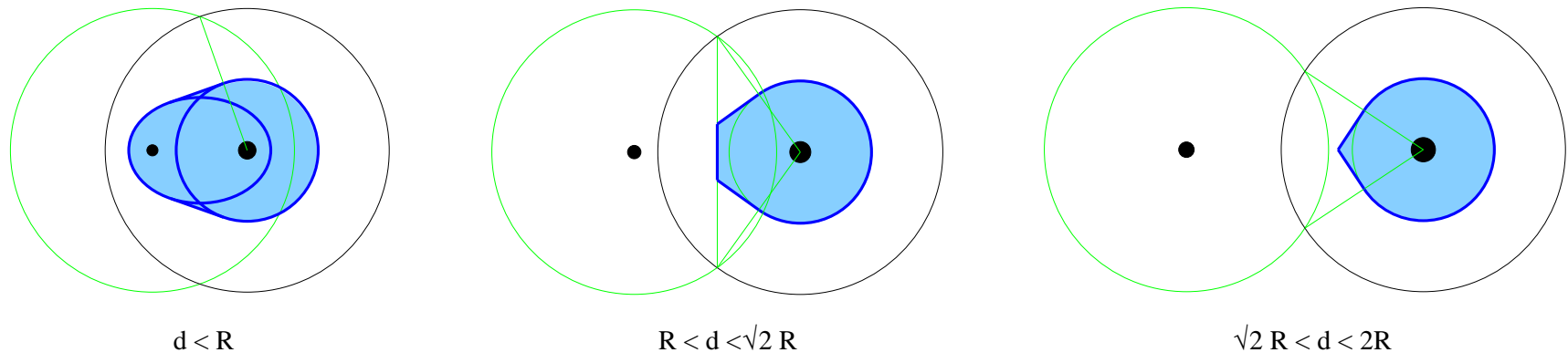


$R < d < \sqrt{2} R$



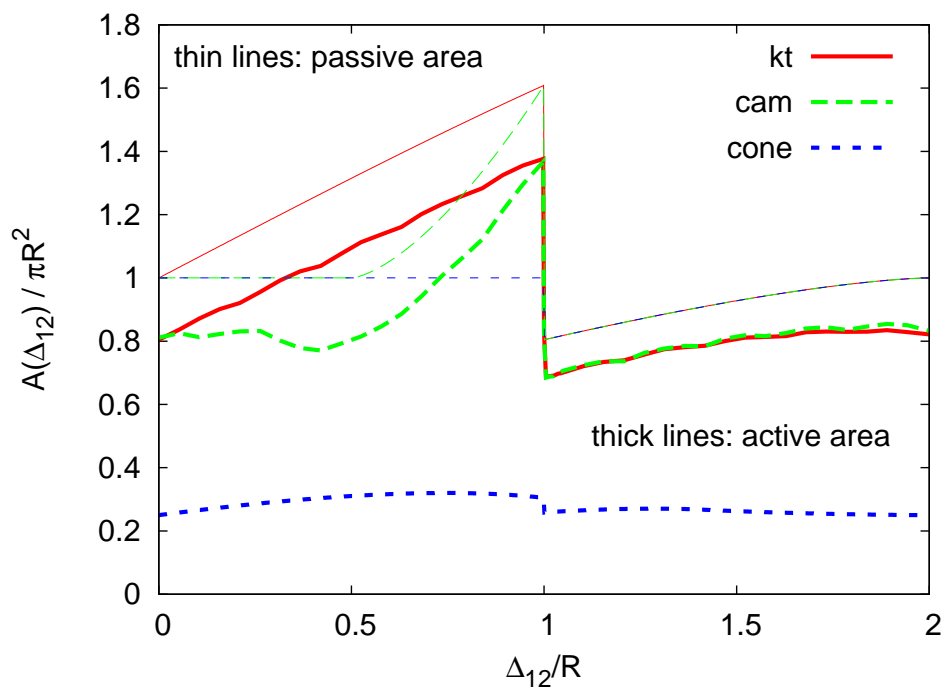
$\sqrt{2} R < d < 2R$

Active area: 1 hard particle + 1 soft: **analytic result for cone only**



Alltogether, we have:

- Area  $\neq$  cst.  $\pi R^2$
- $\Delta_{12}$  dependence under control



QCD probability of emitting a small-angle soft gluon:

$$\frac{dP}{d\Delta_{12} dp_{t,2}} = C_{F,A} \frac{2\alpha_s}{\pi} \frac{1}{\Delta_{12}} \frac{1}{p_{t,2}}$$

Hence the average area is

$$\langle \mathcal{A}(p_{t,1}, R) \rangle = \mathcal{A}_{\text{hard}}(R) + \int d\Delta dp_{t,2} \frac{dP}{d\Delta_{12} dp_{t,2}} [\mathcal{A}_{\text{hard}+1 \text{ soft}}(\Delta, R) - \pi R^2]$$

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Hence the average area is

$$\begin{aligned} \langle \mathcal{A}(p_{t,1}, R) \rangle &= \mathcal{A}_{\text{hard}}(R) + \int d\Delta dp_{t,2} \frac{dP}{d\Delta_{12} dp_{t,2}} [\mathcal{A}_{\text{hard}+1 \text{ soft}}(\Delta, R) - \pi R^2] \\ &= \frac{C_{F,A}}{\pi b_0} \log \left( \frac{\alpha_s(\Lambda)}{\alpha_s(Rp_t)} \right) \pi R^2 d \end{aligned}$$

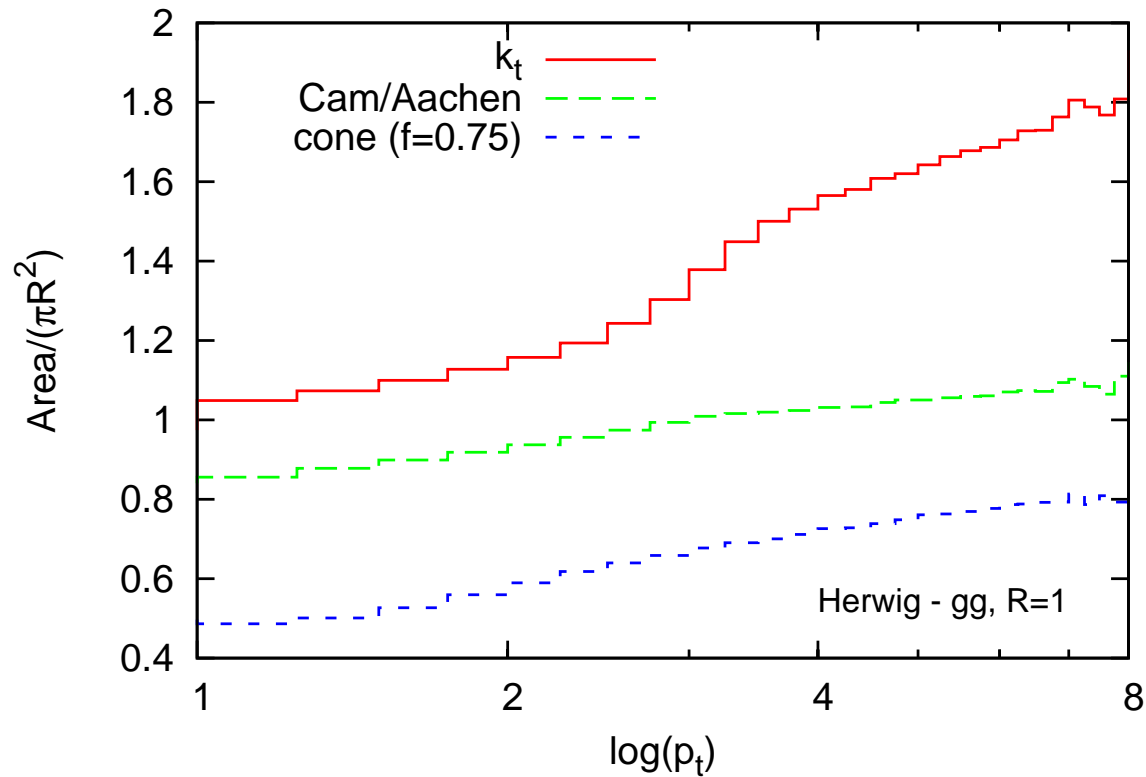
- Scaling violation
- gluon > quark
- with known LO anomalous dimension

$d$	passive	active
$k_t$	0.5638	0.519
Cam	0.07918	0.0865
Cone	-0.06378	0.1246

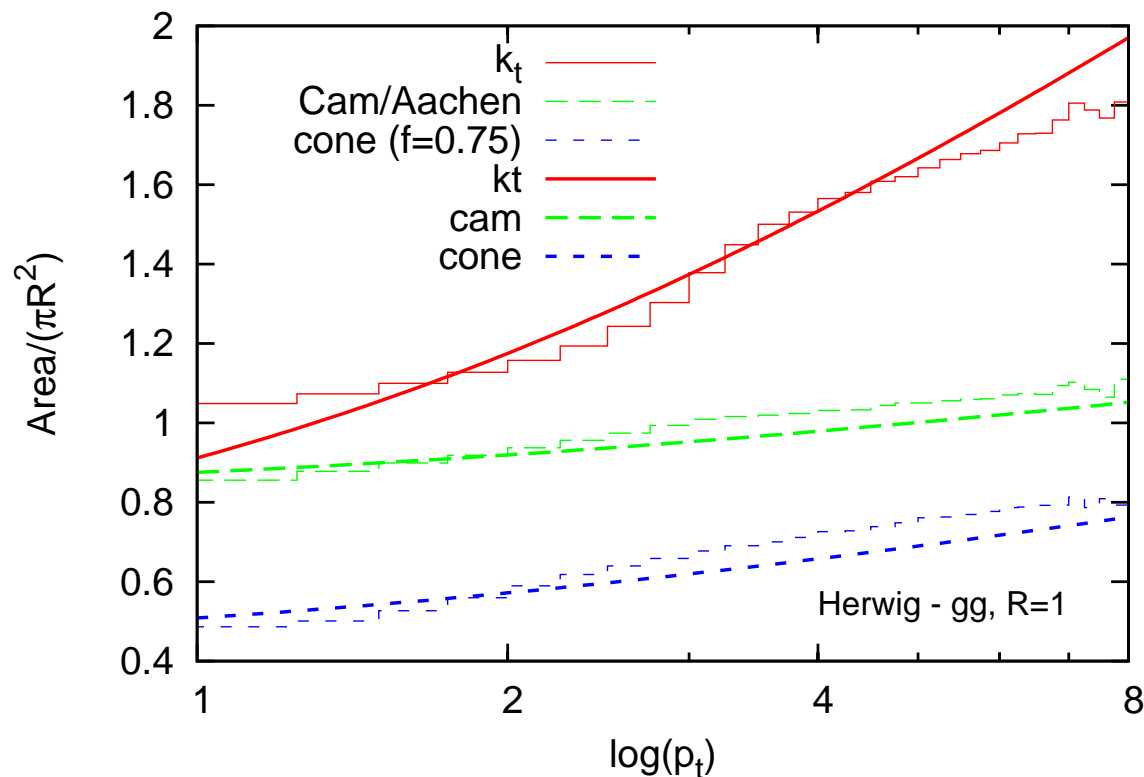


Herwig simulations of  $qq$  or  $gg$  processes at hadron level with underlying event:  
area vs.  $p_t$  of the jet

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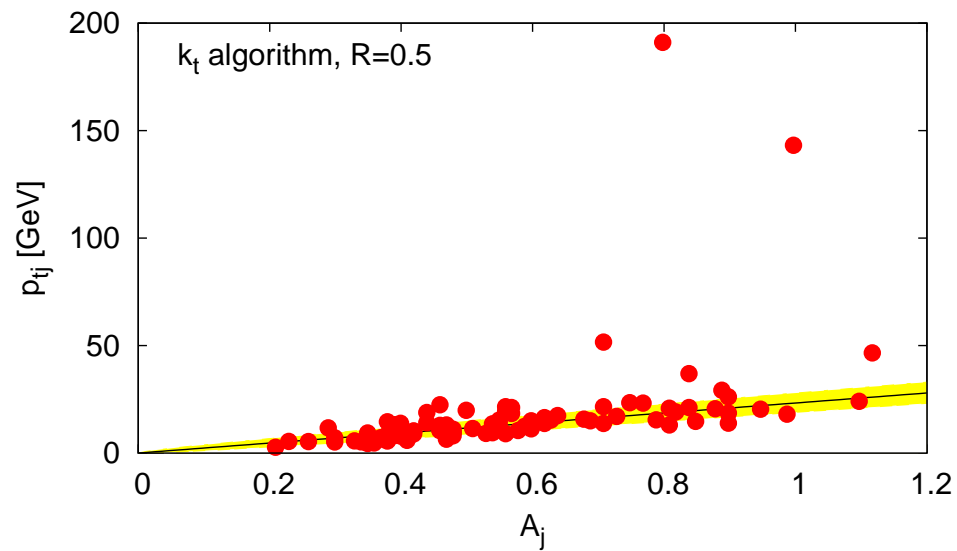


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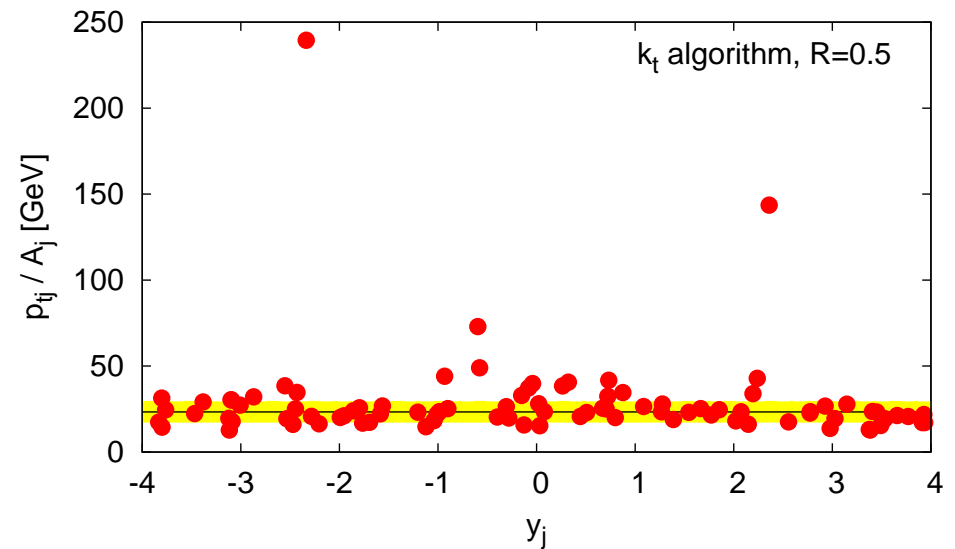
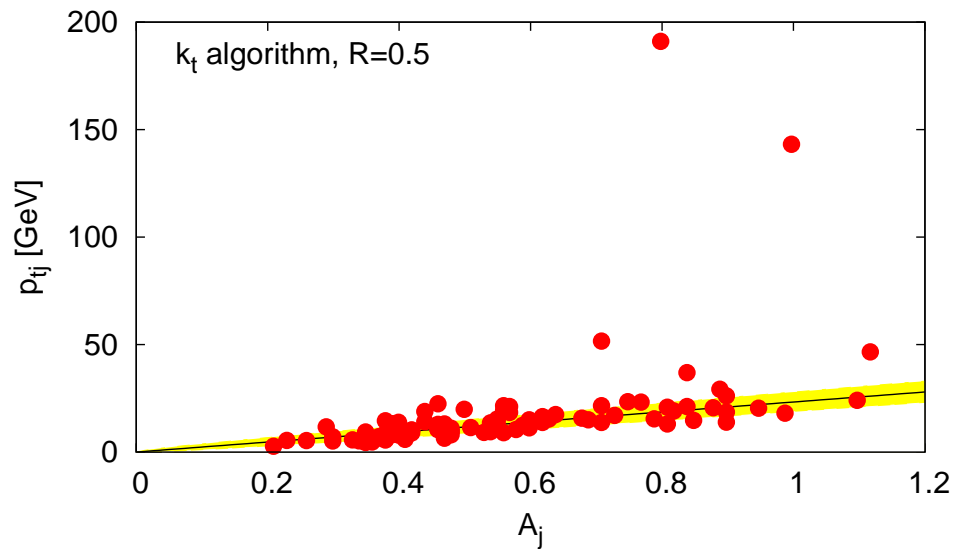


- good agreement with LO predictions
- $k_t$  bigger  $\Rightarrow$  NLO?

## Dense event with pile-up:

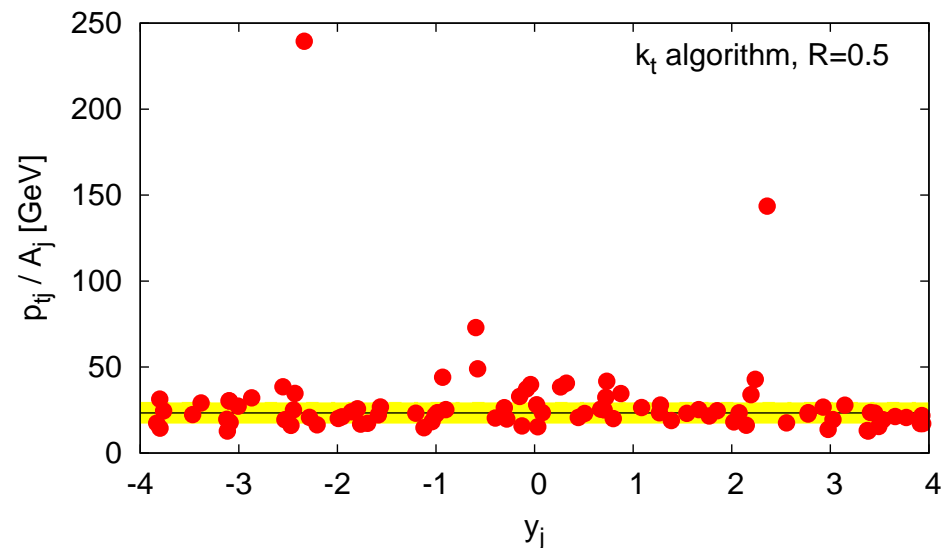
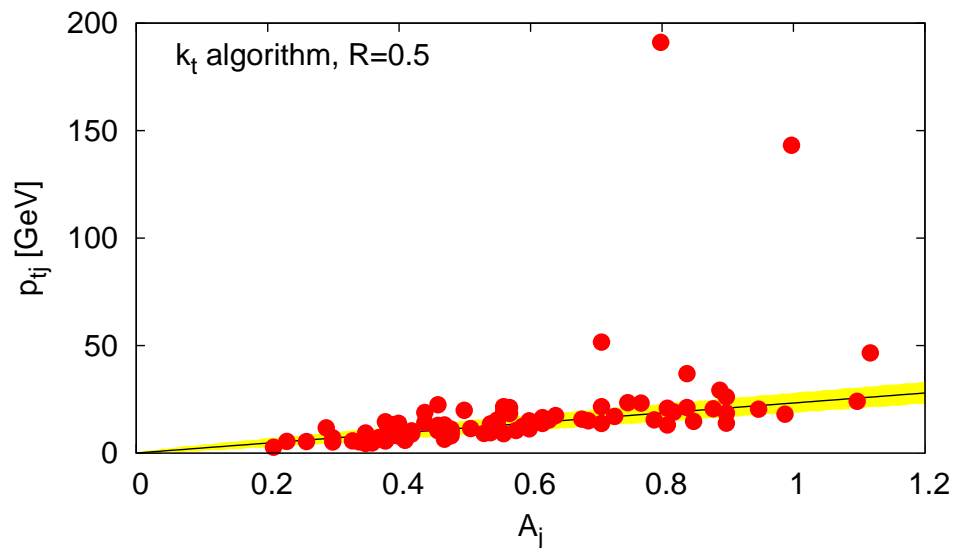


Dense event with pile-up:



- Area  $\propto p_t$  of the jet
- $p_t$ /area is constant  $\rightarrow \rho = \text{median } p_t$ /area

Dense event with pile-up:



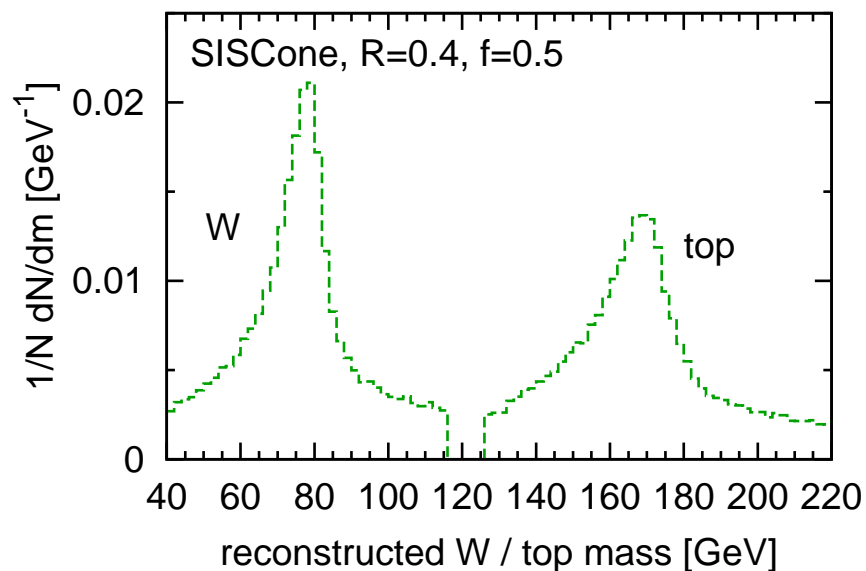
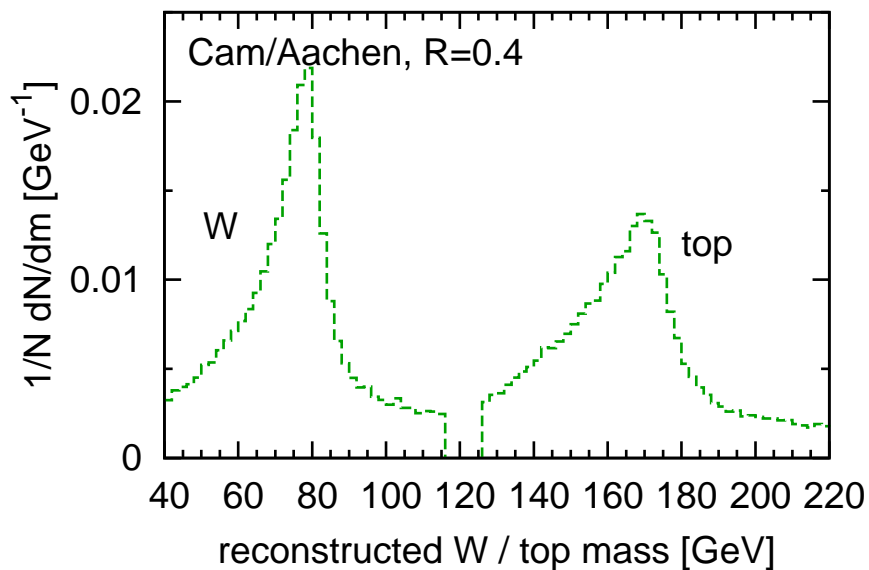
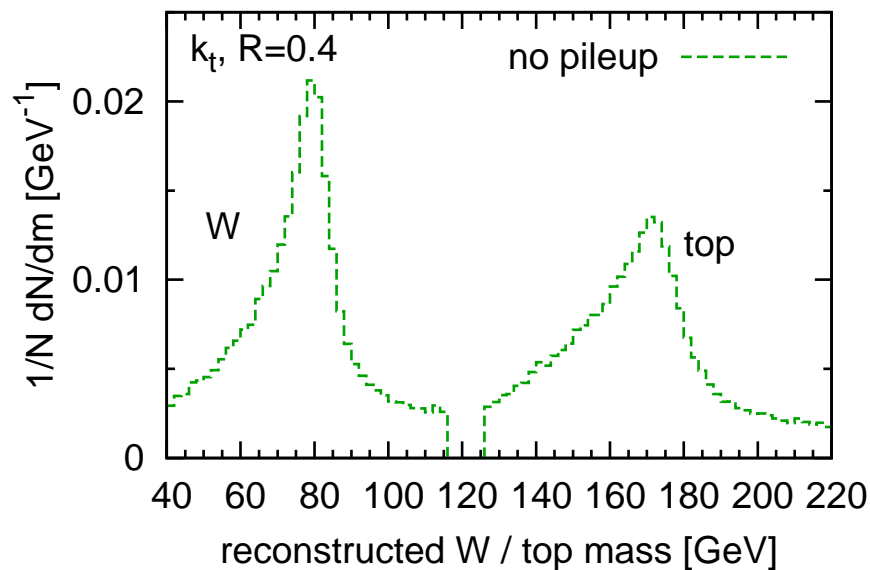
- Area  $\propto p_t$  of the jet
- $p_t/\text{area}$  is constant  $\rightarrow \rho = \text{median } p_t/\text{area}$

Area can be used to remove pileup pollution  
e.g. by removing  $\rho \cdot \text{area}$

$t\bar{t} + W$

$(t\bar{t} \rightarrow \ell^+ \nu_{\ell} b + q\bar{q}b)$

$(W \rightarrow q\bar{q})$



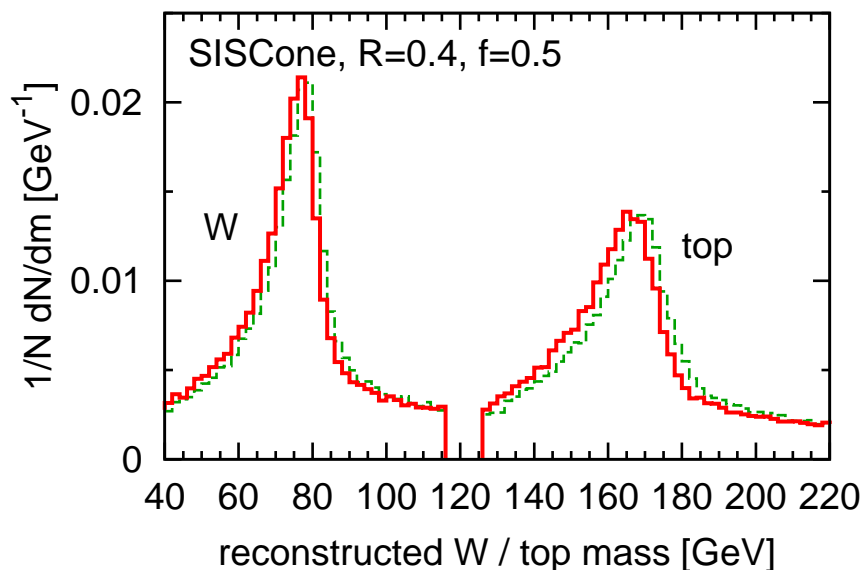
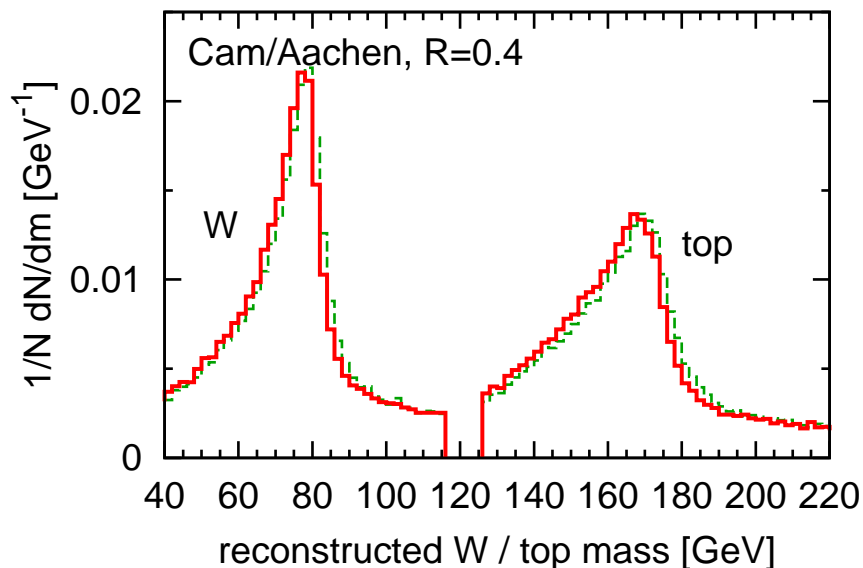
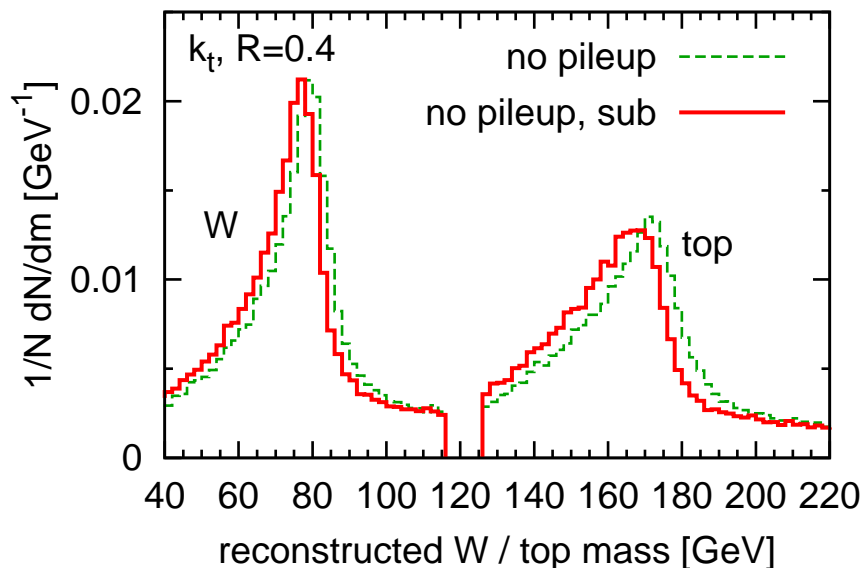
LHC at high lumi

no pileup  $\Rightarrow$  good result

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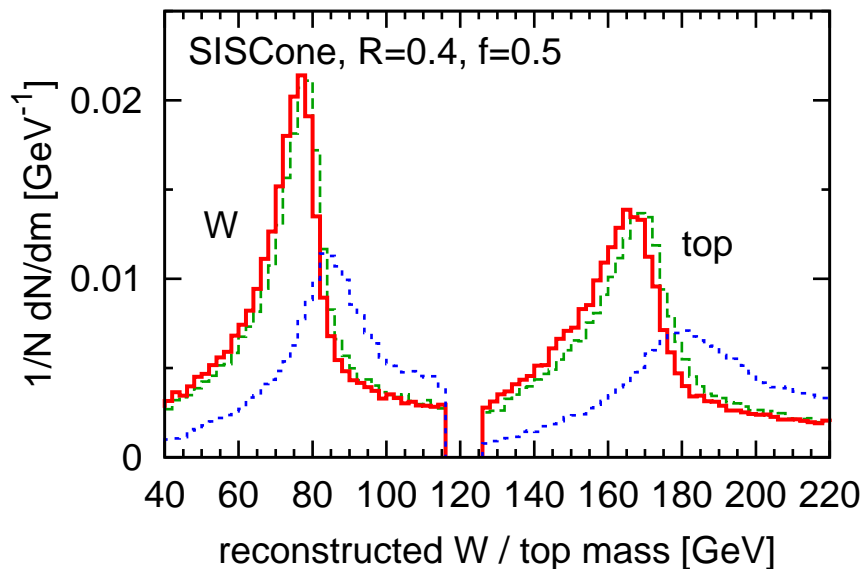
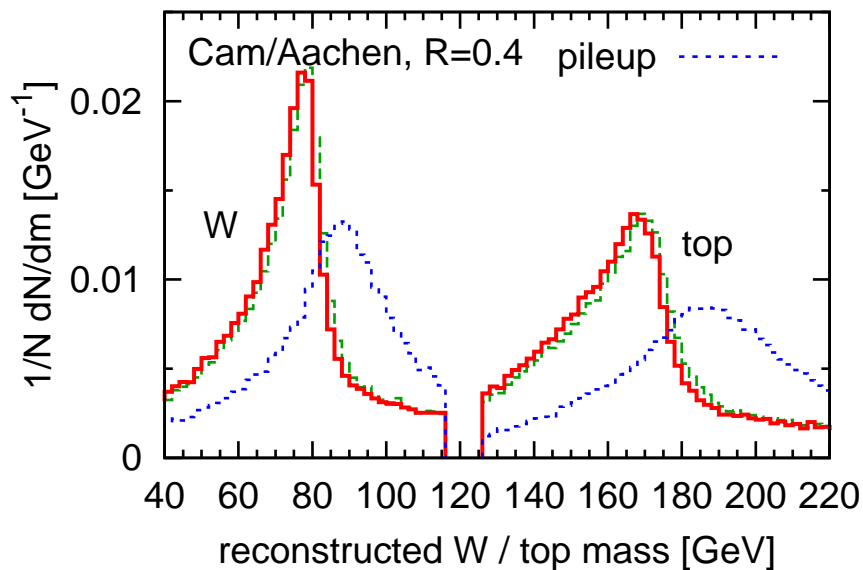
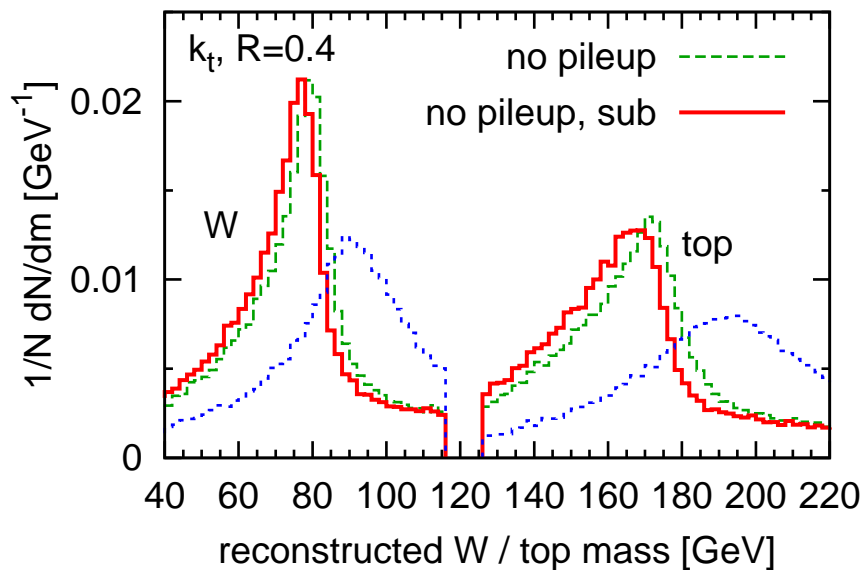
$\Rightarrow$  no subtraction effect



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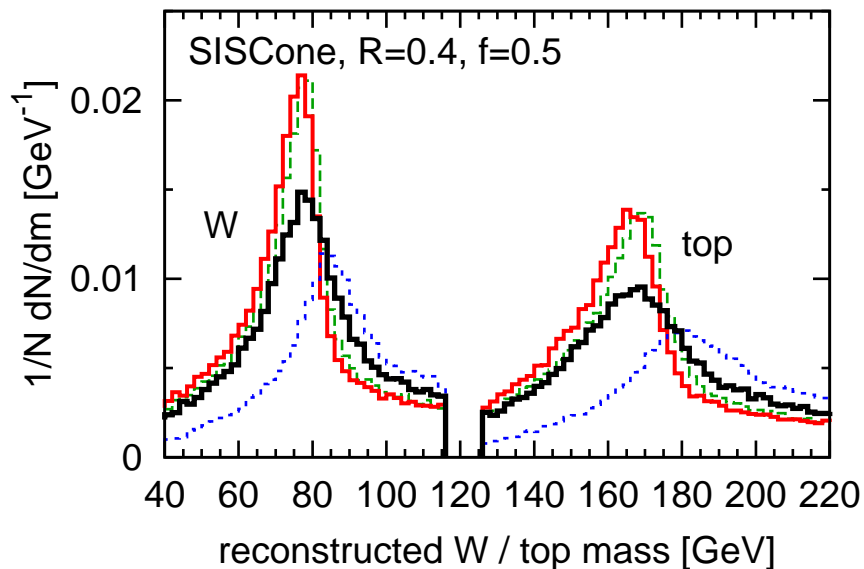
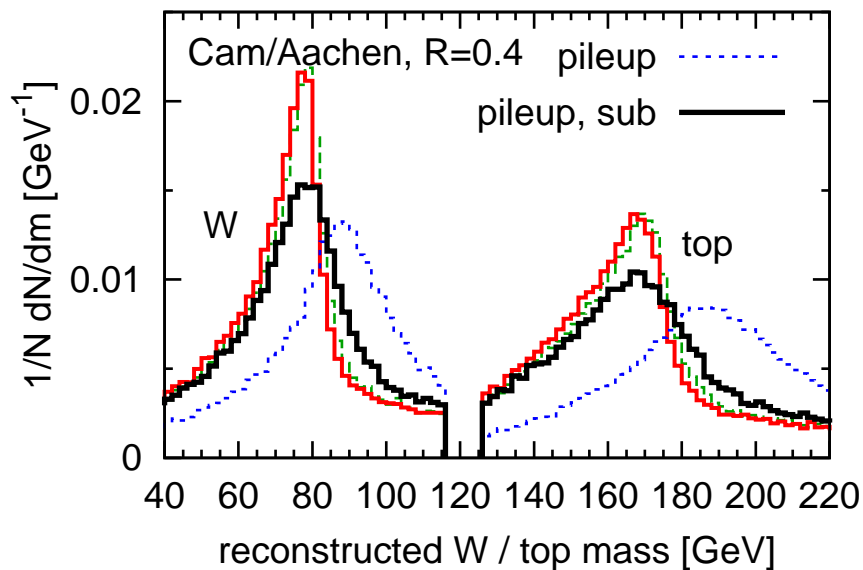
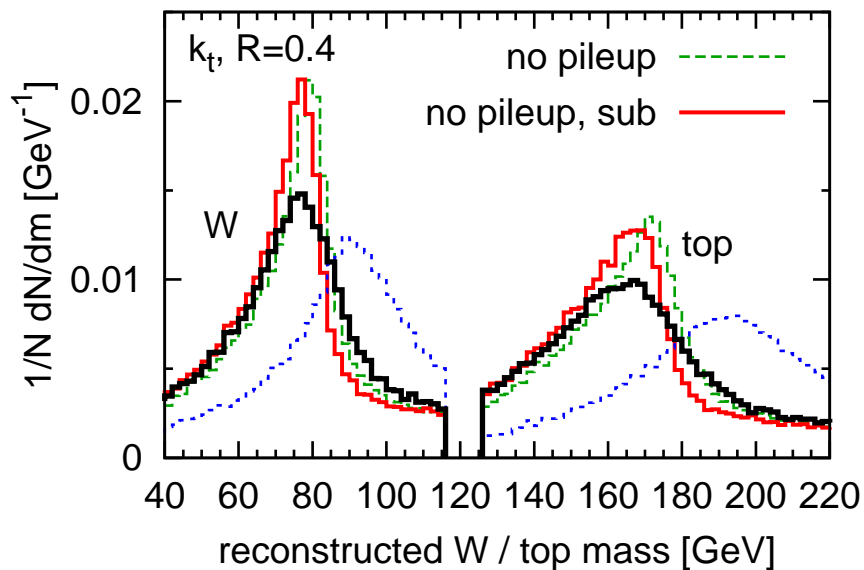
$\Rightarrow$  no subtraction effect

pileup  $\Rightarrow$  poor result

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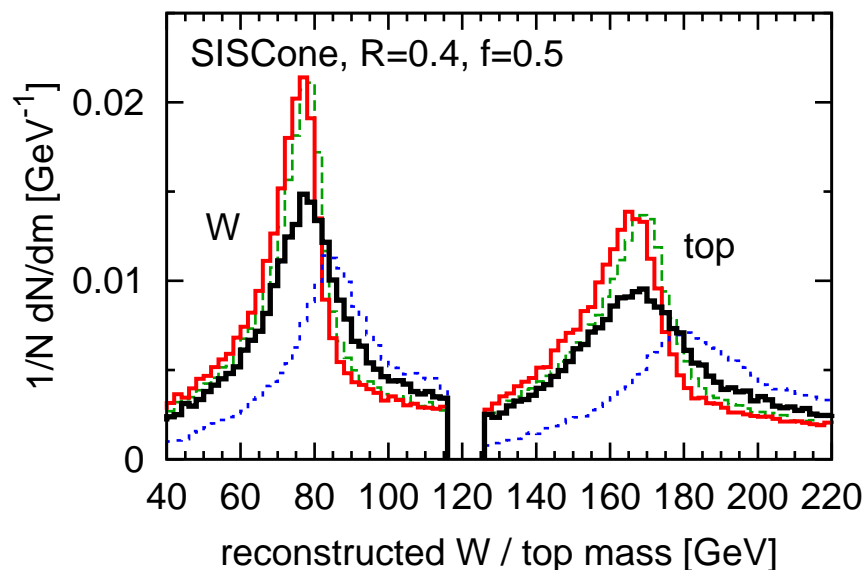
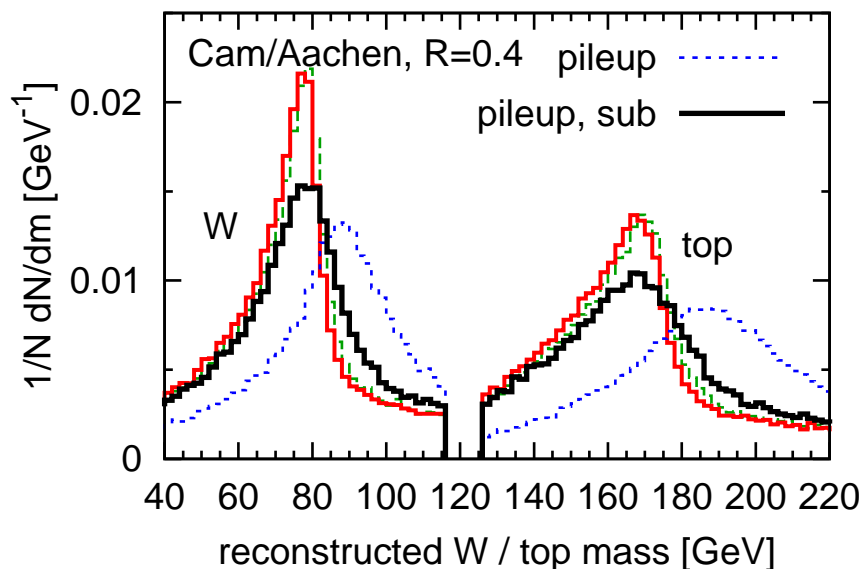
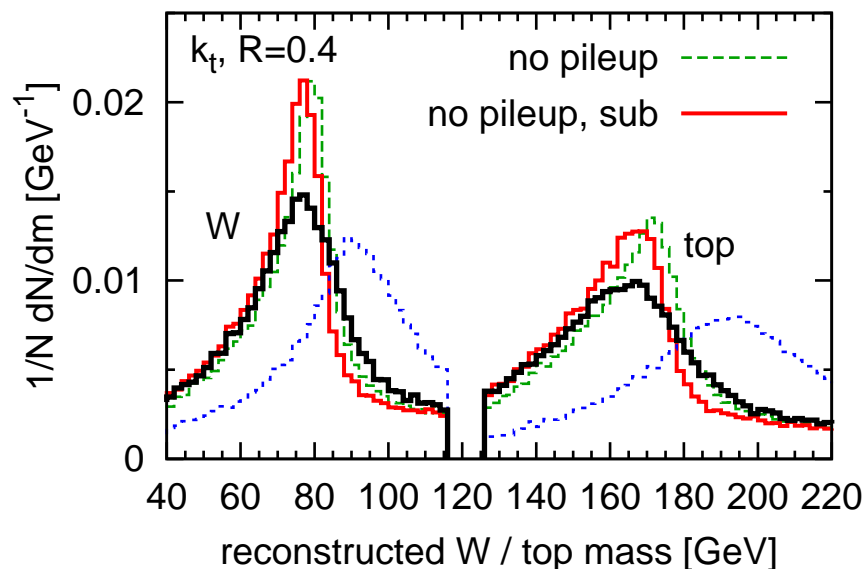
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LHC at high lumi

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Background suppression in heavy ions!

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  - first to satisfy requirements of the 90's!
  - mandatory for LHC
  - Get it at <http://projects.hepforge.org/siscone>  
or <http://www.lpthe.jussieu.fr/~salam/fastjet>

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  - only the beginning...